



# VIS 2023

Melbourne, Australia

## A Comparative Study of the Perceptual Sensitivity of Topological Visualizations to Feature Variations

Tushar M. Athawale  
Oak Ridge National Laboratory

Bryan Triana  
University of South Florida

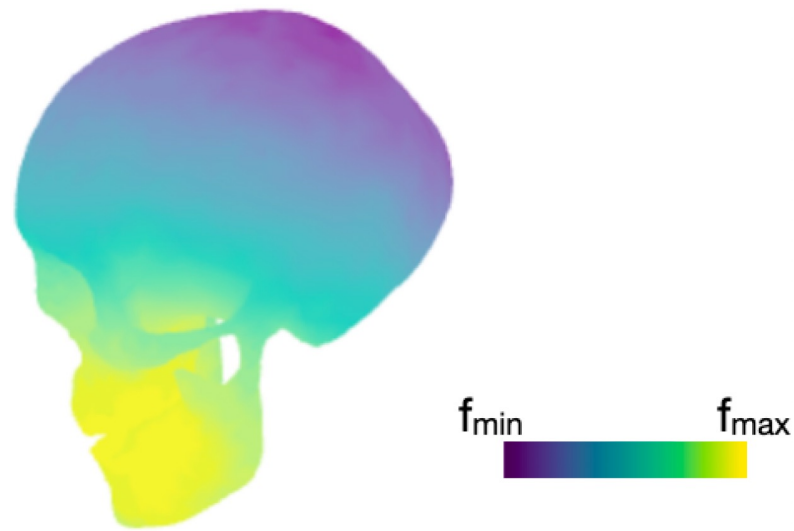
Tanmay Kotha  
University of South Florida

David Pugmire  
Oak Ridge National Laboratory

Paul Rosen  
University of Utah



# Color Maps Vs. Topological Visualizations

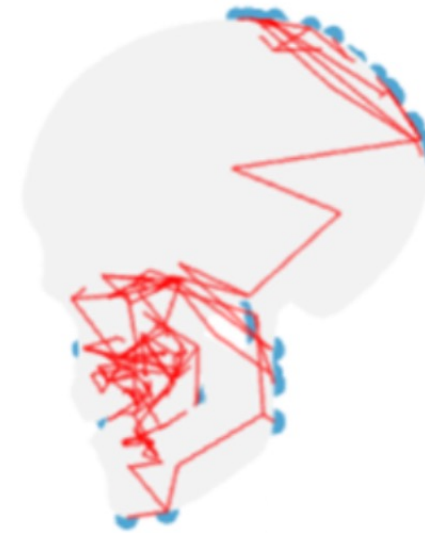


Color map

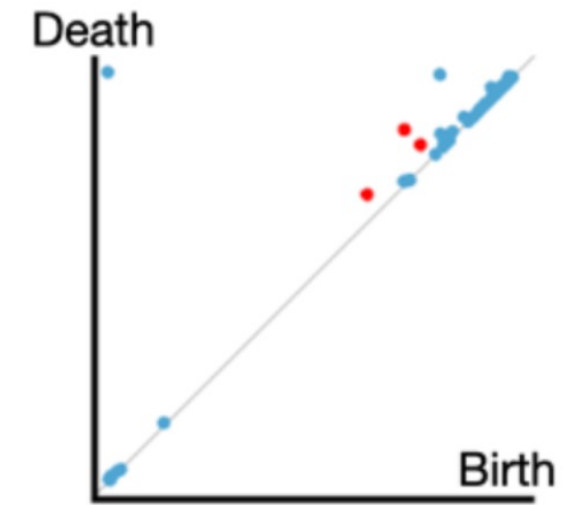
Implicit portrayal of data features



Isocontours



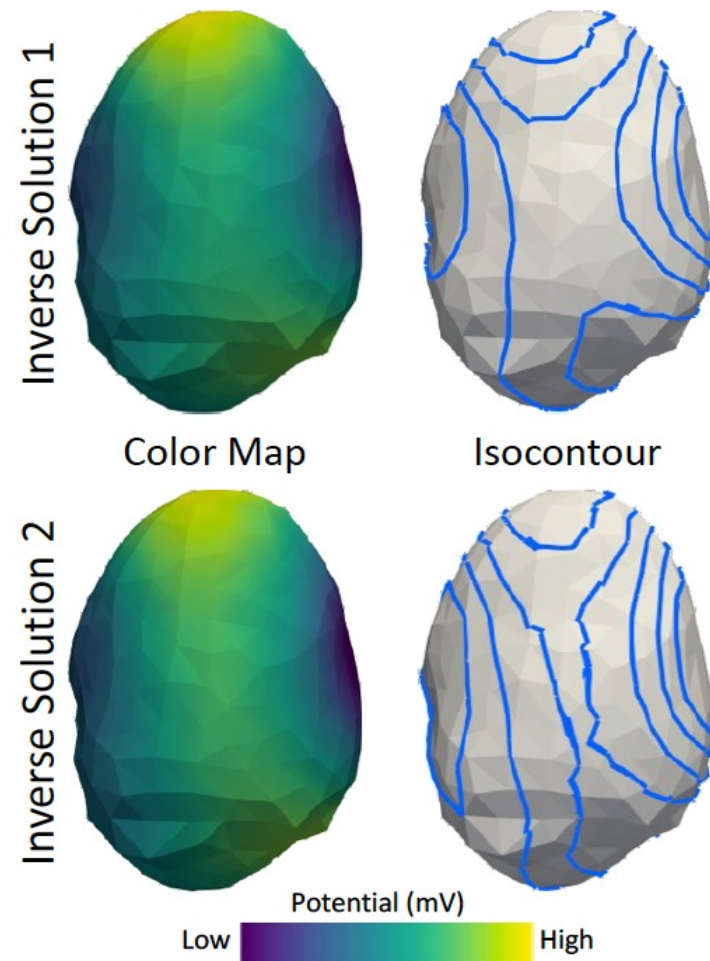
Reeb graph



Persistence diagram

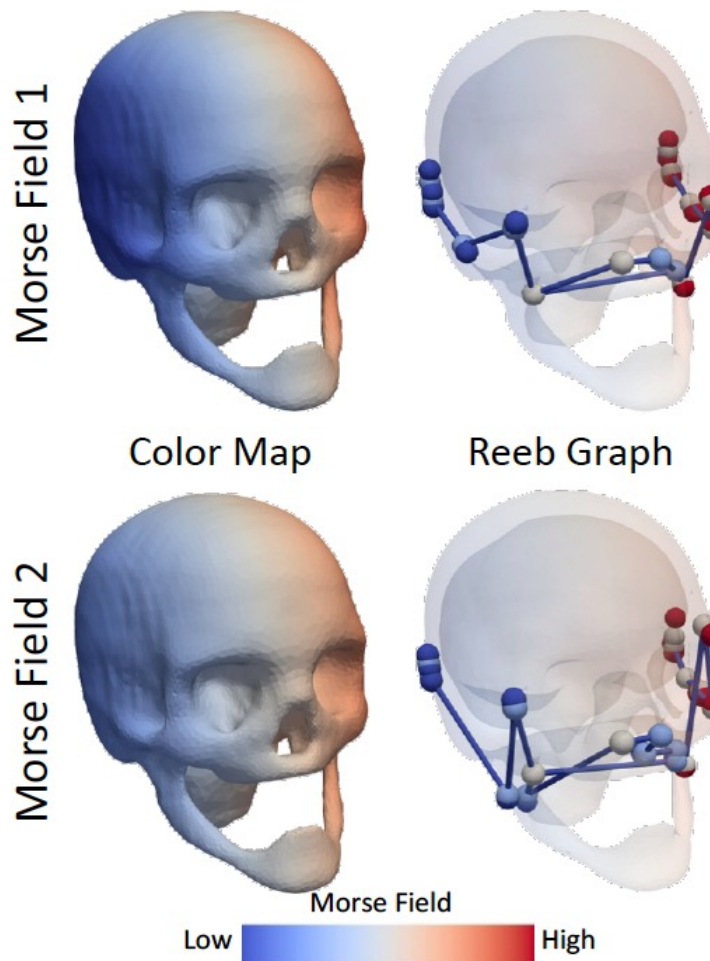
Explicit portrayal of data features

# Application of Visualization Comparisons



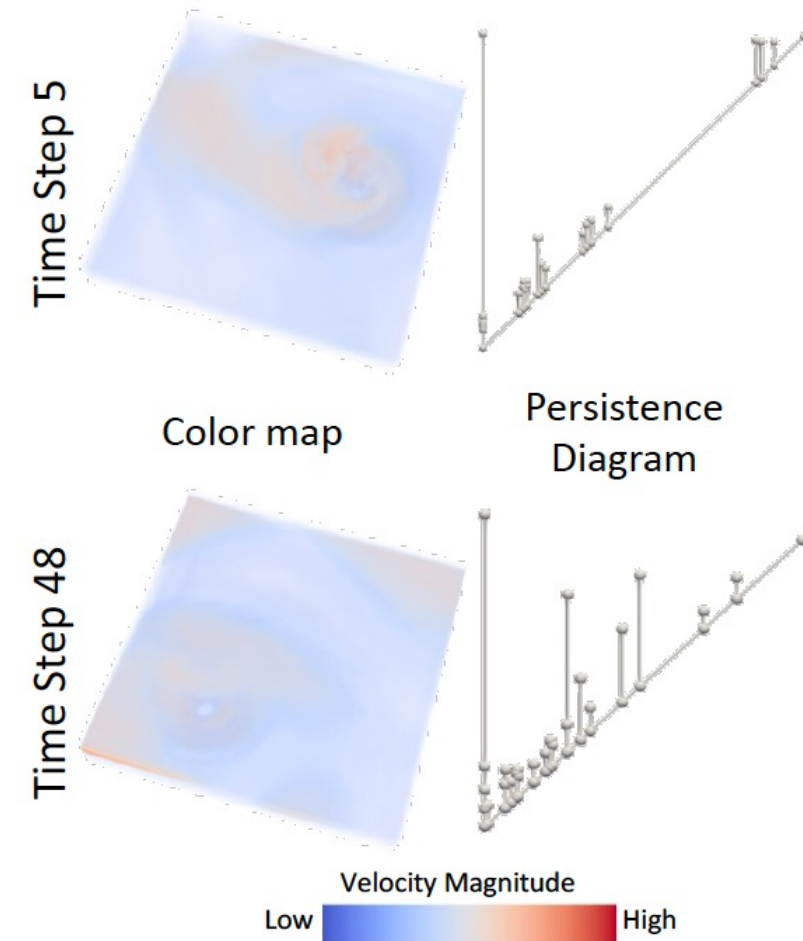
(a) Potentials on heart surface  
[Njeru et al., 2022]

Ensemble simulations



(b) Patient-specific cephalometric landmarks  
[Makram and Kamel, 2014]

Observational data



(c) Time-varying simulations of a hurricane  
[Vidal et al., 2020]

Time-varying data



# Provocation

**It is not clear how good humans are at perceiving features in a visualization!**



Color Map



Potential (mV)  
Low High

(a) Potentials on heart surface  
[Njeru et al., 2022]

Ensemble simulations



Morse Field 1



Morse Field 2

Morse Field  
Low High

(b) Patient-specific cephalometric landmarks  
[Makram and Kamel, 2014]

Observational data



Time Step 5



Time Step 6

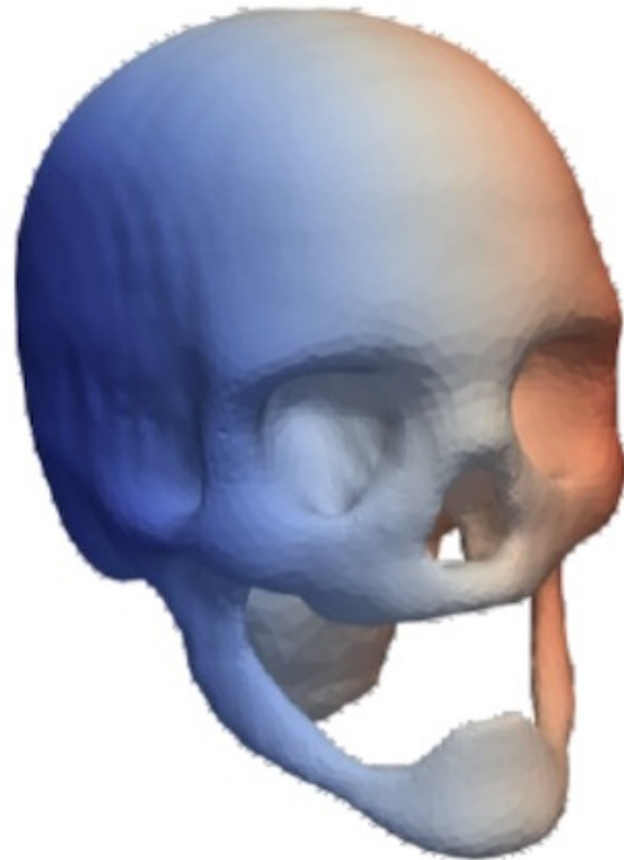
Velocity Magnitude  
Low High

(c) Time-varying simulations of a hurricane  
[Vidal et al., 2020]

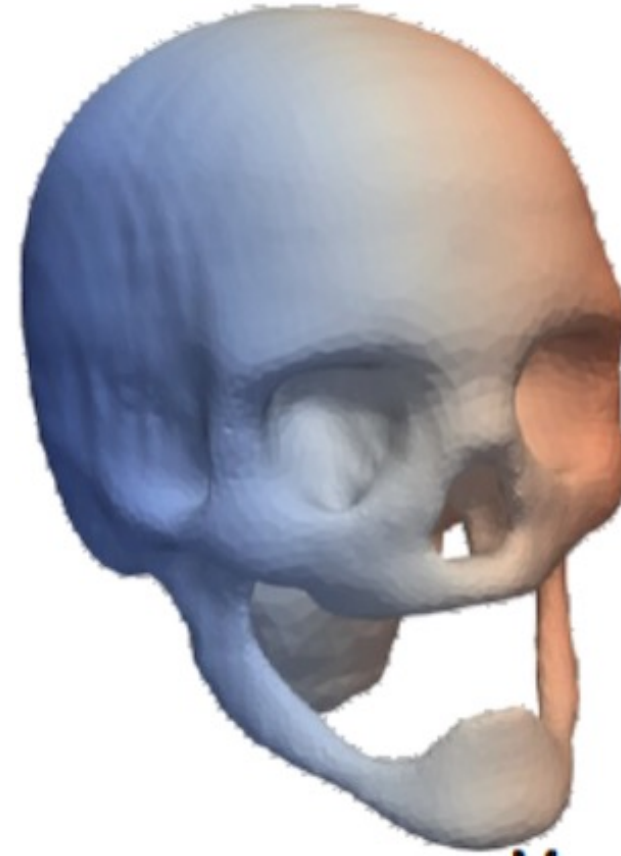
Time-varying data

# Can You Tell Where and How Much the Following Visualizations are Different?

Dataset 1



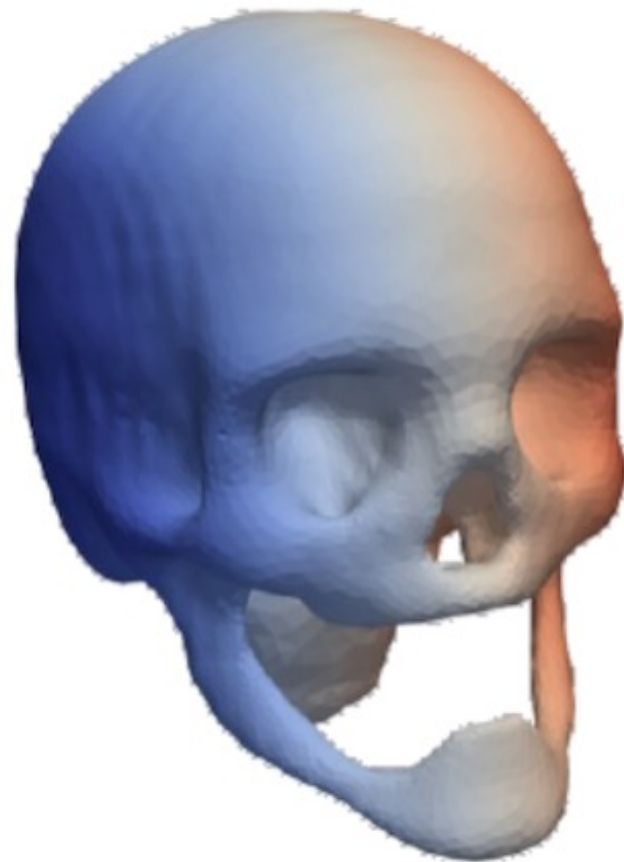
Dataset 2



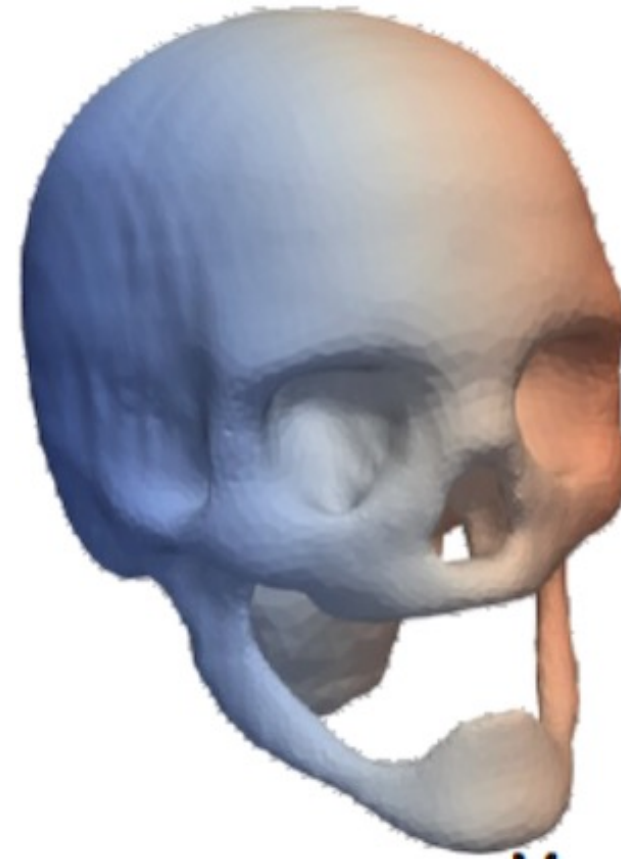
Color Map

# Can You Tell Where and How Much the Following Visualizations are Different?

Dataset 1



Dataset 2

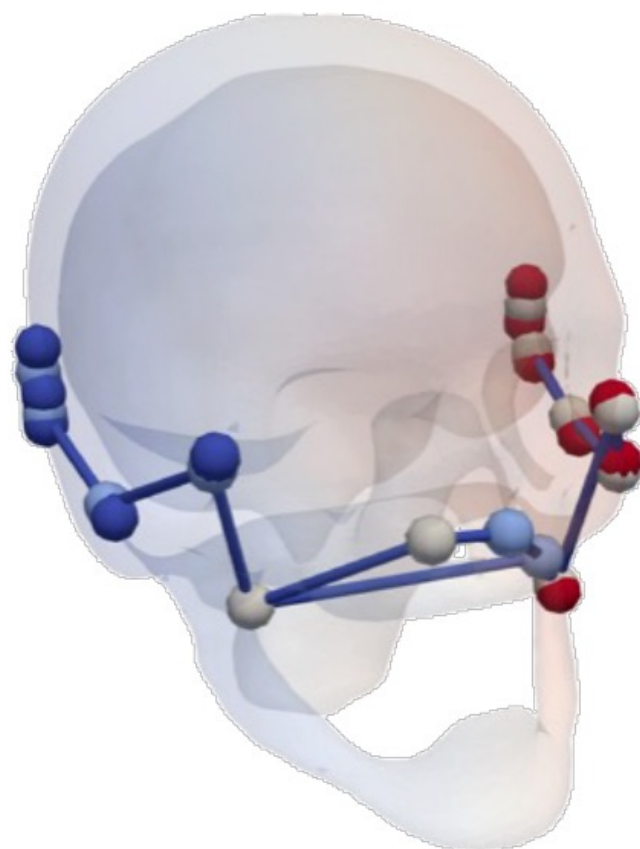


Perhaps it is difficult to notice differences!

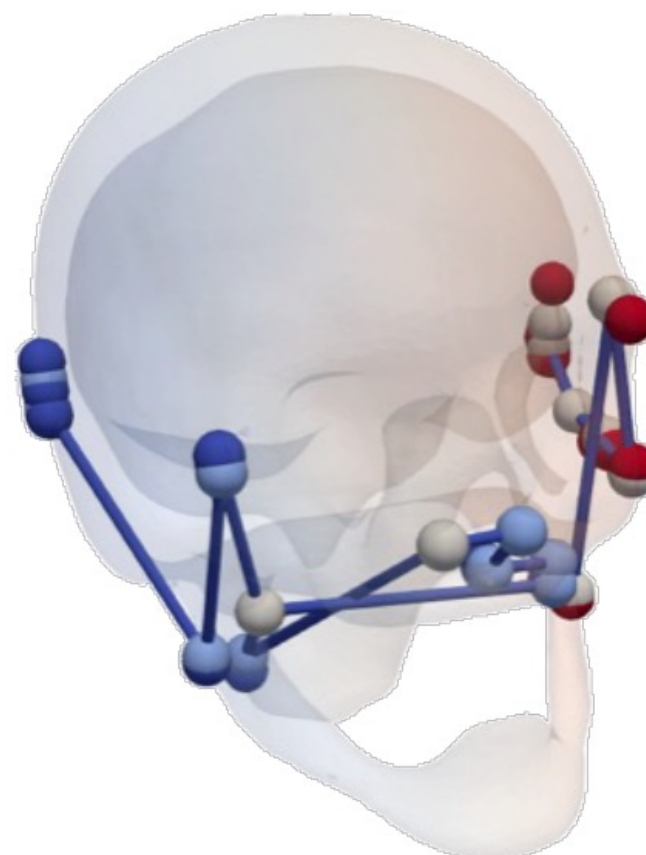
Color Map

# Can You Tell Where and How Much the Following Visualizations are Different?

Dataset 1



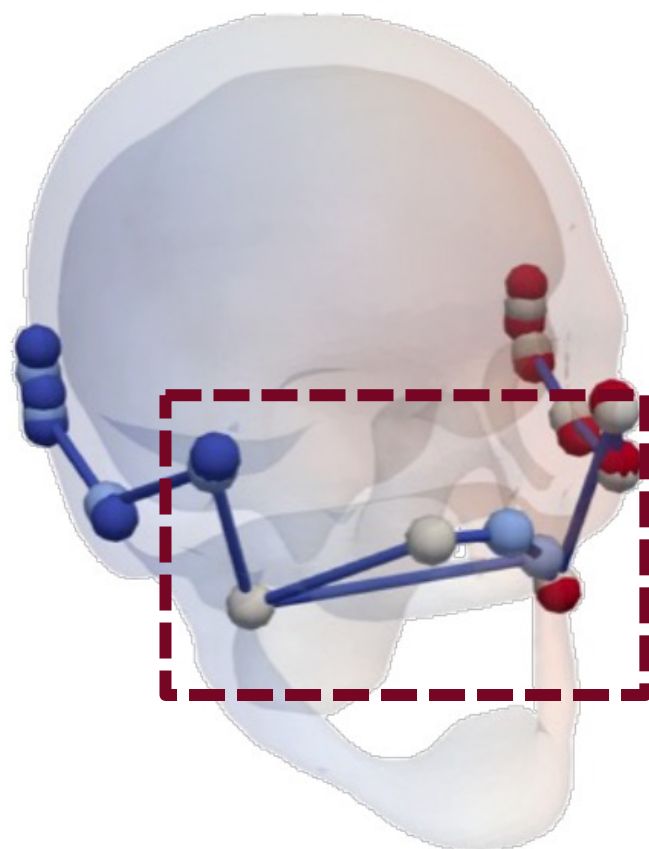
Dataset 2



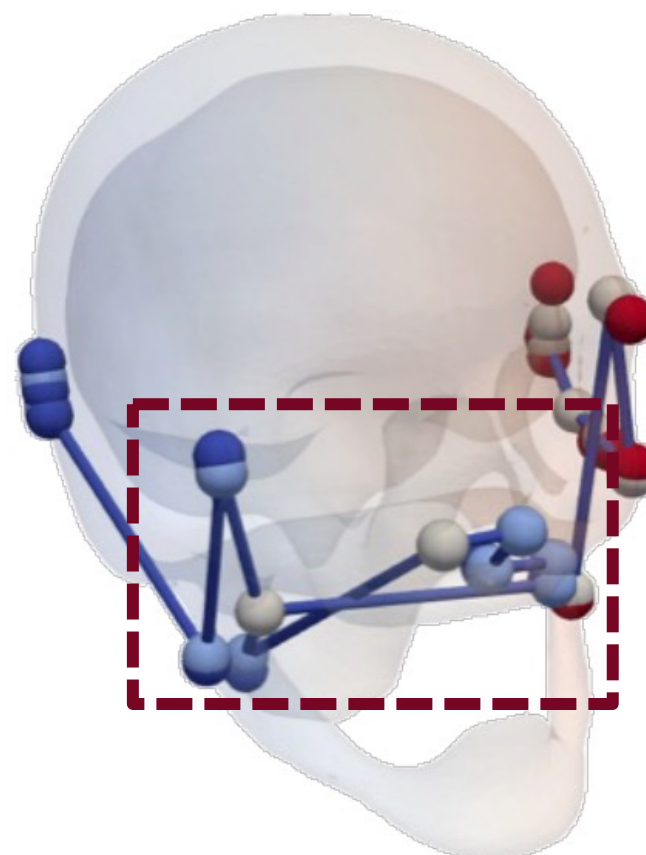
Reeb graph (topological skeleton of a scalar field)

# Can You Tell Where and How Much the Following Visualizations are Different?

Dataset 1



Dataset 2



Perhaps it is easier to notice differences!

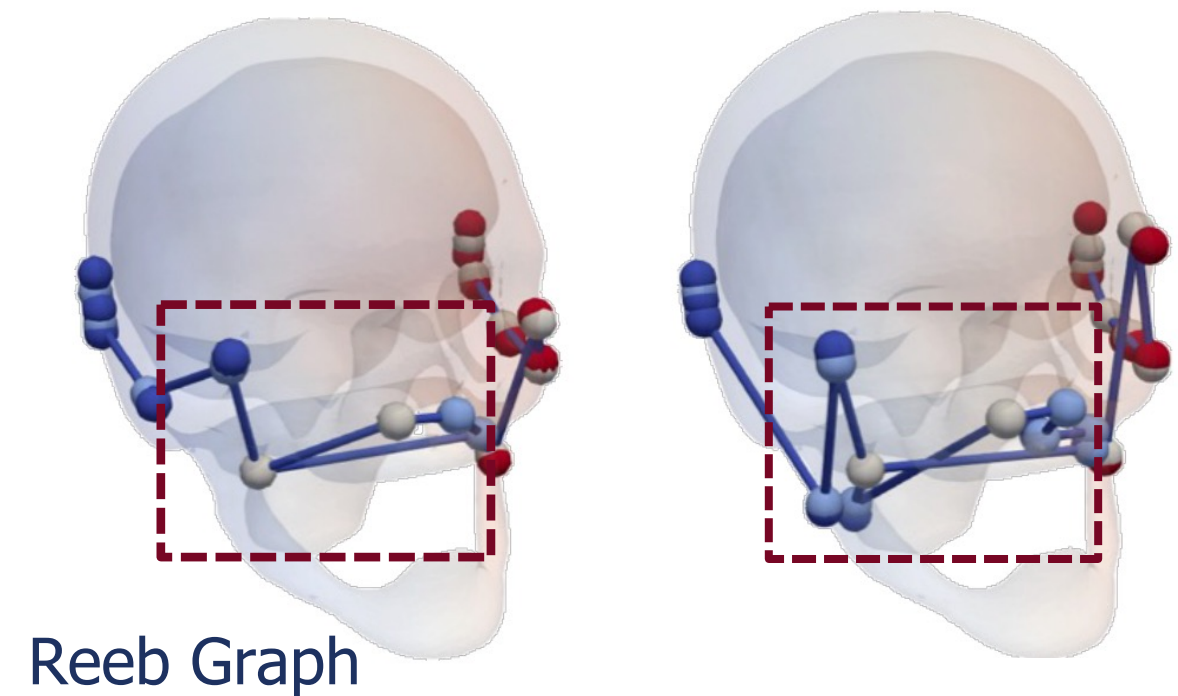
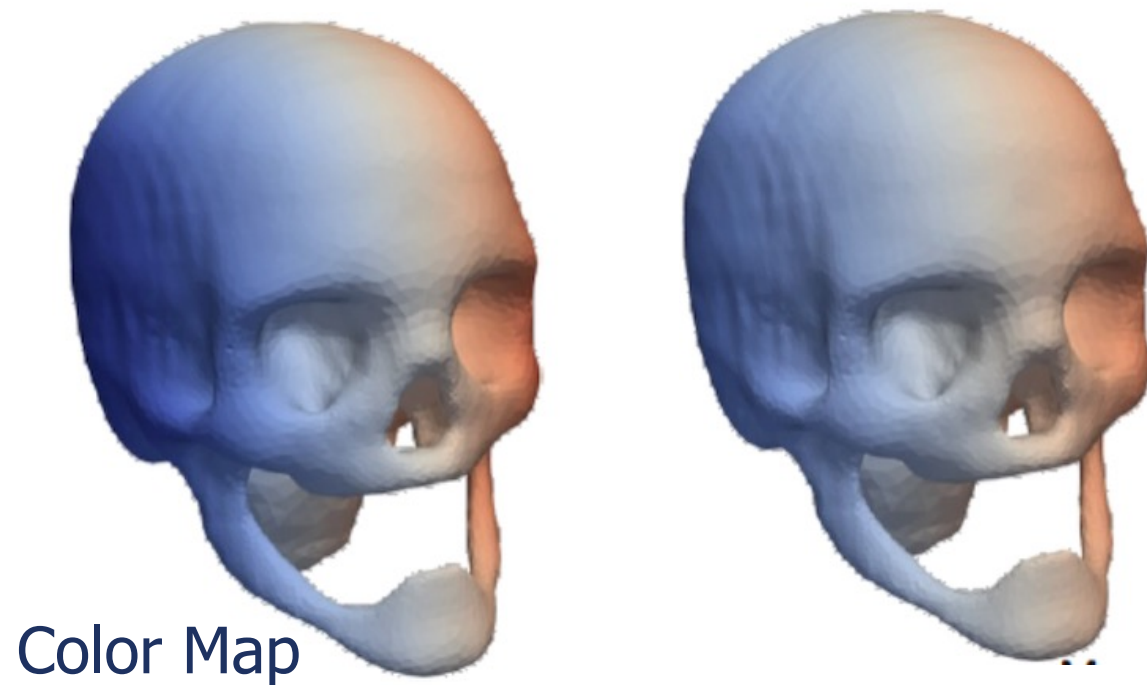
Reeb graph (topological skeleton of a scalar field)



# We Investigate What Features Users Perceive When Comparing Visualizations

Studying perceptual sensitivity of visualizations is crucial to:

- gaining insight into limitations of visualization types
- enhancing visualization design
- choosing optimal visualization type



# Related Work

- Factors contributing to effective visualization  
[Kosara et al., 2003], [Wijk, 2005], [North, 2006], [Munzner, 2009], [Quadri and Rosen, 2022]
- Perception  
[Rogowitz et al., 1996], [Liu and Heer, 2009], [Moreland, 2009], [Zhou and Hansen, 2016], [Cooper et al., 2021], [Laidlaw et al., 2005], [Forsberg et al., 2009]
- Quantitative comparison of topological visualizations  
[Cohen-Steiner et al., 2007], [Edelsbrunner and Harer, 2010], [Morozov et al., 2013], [Sridharamurthy et al., 2020], [Pont et al., 2022], [Bollen et al., 2023], [Lan et al., 2023]
- Sensitivity analysis of functions and visualizations  
[Cacuci et al., 2005], [Saltelli et al., 2008], [Liu et al., 2014], [Chan et al., 2010], [Brecheisen et al., 2009]

# Related Work

- Factors contributing to effective visualization  
[Kosara et al., 2003], [Wijk, 2005], [North, 2006], [Munzner, 2009], [Quadri and Rosen, 2022]
- Perception  
[Rogowitz et al., 1996], [Liu and Heer, 2009], [Moreland, 2009], [Zhou and Hansen, 2016], [Cooper et al., 2021], [Laidlaw et al., 2005], [Forsberg et al., 2009]
- Quantitative comparison of topological visualizations  
[Cohen-Steiner et al., 2007], [Edelsbrunner and Harer, 2010], [Morozov et al., 2013], [Sridharamurthy et al., 2020], [Pont et al., 2022], [Bollen et al., 2023], [Lan et al., 2023]
- Sensitivity analysis of functions and visualizations  
[Cacuci et al., 2005], [Saltelli et al., 2008], [Liu et al., 2014], [Chan et al., 2010], [Brecheisen et al., 2009]

To our understanding, no prior work has evaluated feature perception sensitivity for topological visualizations



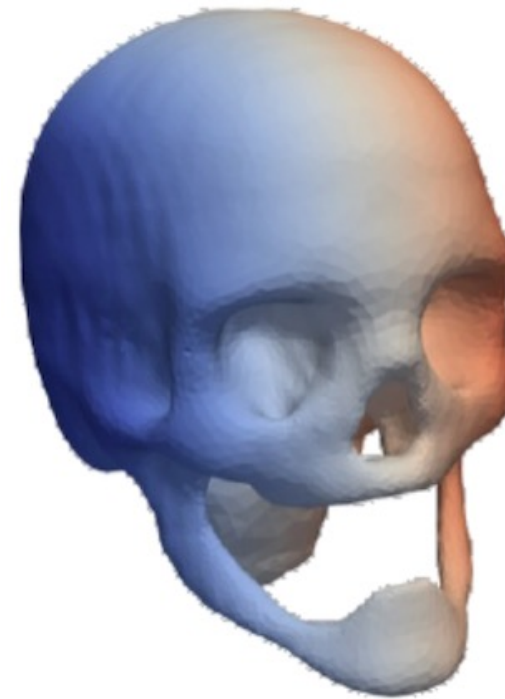
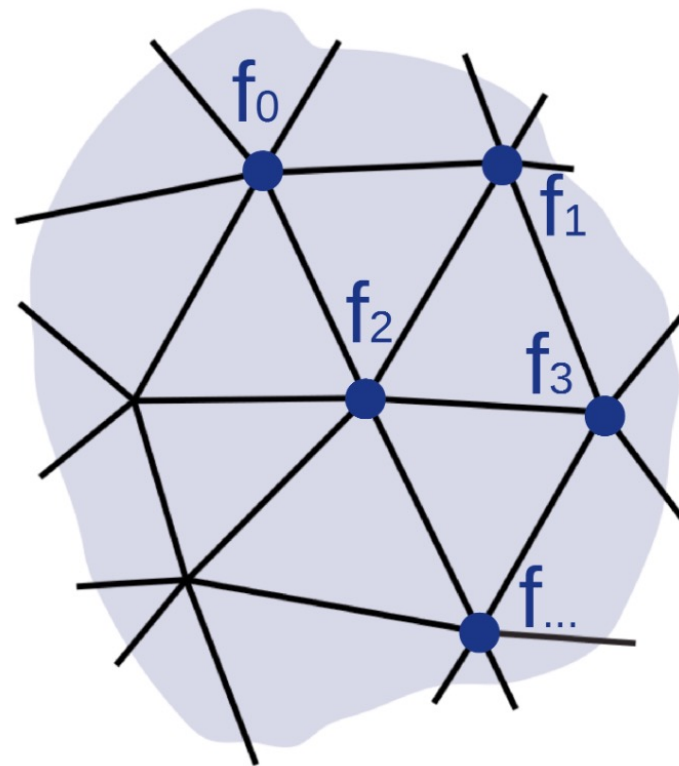
**Evaluated Data and Techniques  
and Hypothesis**



# Data

Scalar fields sampled on 2D manifolds embedded in 3D

$$f : \mathcal{M} \rightarrow \mathbb{R}$$



# Data

## Scalar field is represented as a mixture of Gaussians

[Vidal et al., 2020] [Yan et al., 2021]

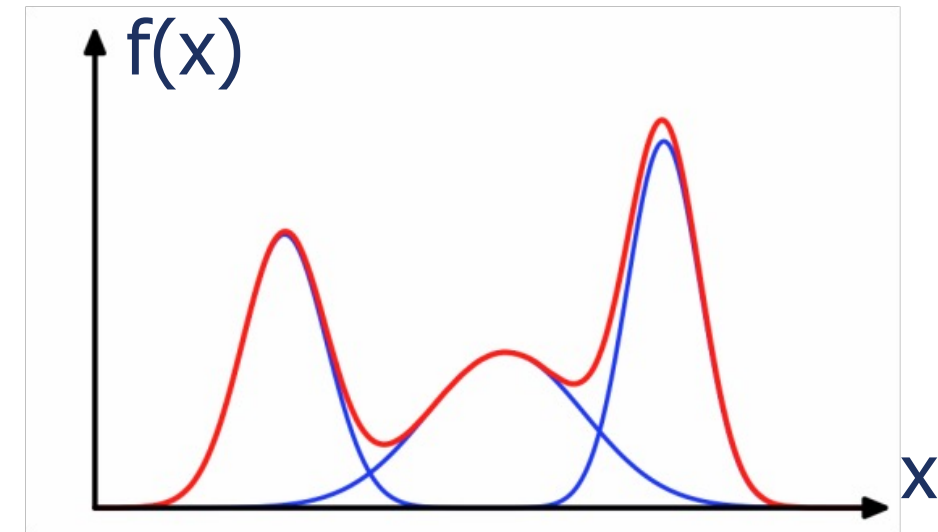
$$f(x, y, z) = \mathcal{N}(x, y, z) + \sum_i^{NOF} \mathcal{G}_i(x, y, z),$$

Perlin noise (pointing to  $\mathcal{N}$ )      Gaussian function (pointing to  $\mathcal{G}_i$ )

$(x_i, y_i, z_i)$ : Mean of a Gaussian

$$\mathcal{G}_i(x, y, z) = a_i \cdot \exp\left(-\left(\frac{(x-x_i)^2 + (y-y_i)^2 + (z-z_i)^2}{2\sigma^2}\right)\right)$$

Amplitude (pointing to  $a_i$ )      Standard deviation (pointing to  $\sigma^2$ )



# Data

## Scalar field is represented as a mixture of Gaussians

[Vidal et al., 2020] [Yan et al., 2021]

$$f(x, y, z) = \mathcal{N}(x, y, z) + \sum_i^{NOF} \mathcal{G}_i(x, y, z),$$

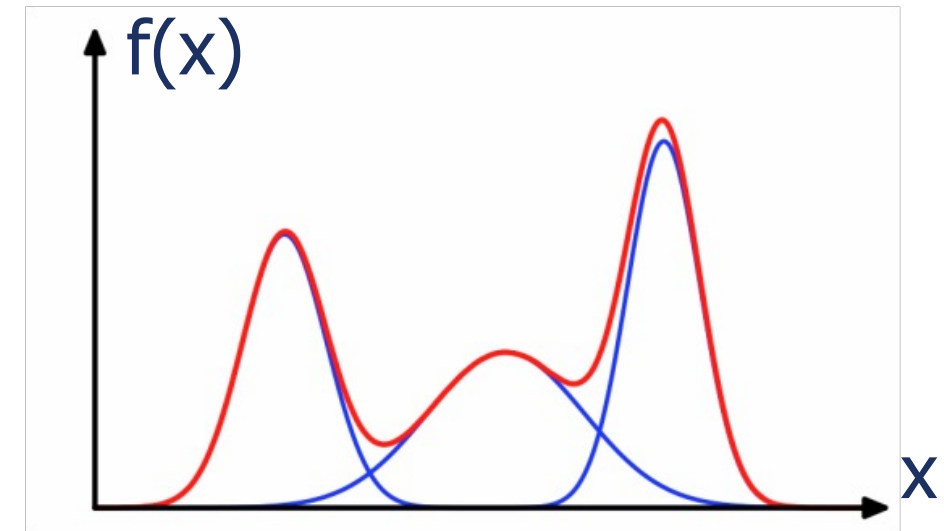
Perlin noise (pointing to  $\mathcal{N}$ )      Gaussian function (pointing to  $\mathcal{G}_i$ )

$(x_i, y_i, z_i)$ : Mean of a Gaussian

$$\mathcal{G}_i(x, y, z) = a_i \cdot \exp\left(-\left(\frac{(x-x_i)^2 + (y-y_i)^2 + (z-z_i)^2}{2\sigma^2}\right)\right)$$

Amplitude (pointing to  $a_i$ )

Standard deviation (pointing to  $\sigma^2$ )

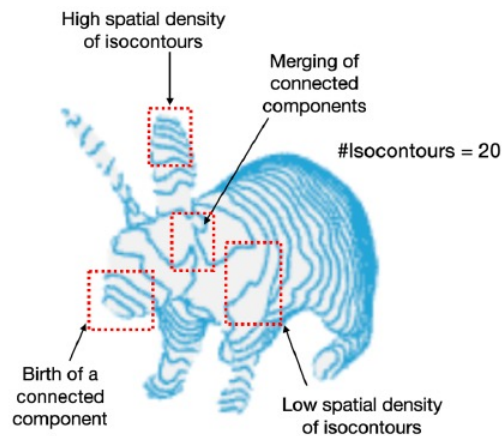
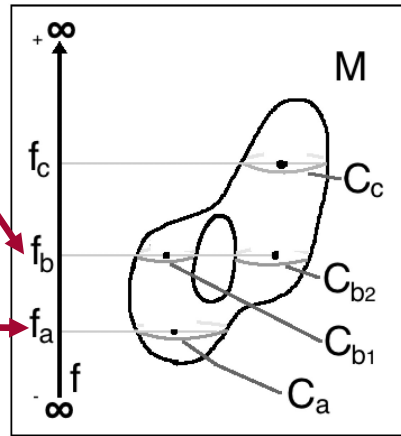


How much visualization is sensitive to changes in amplitude and mean of a Gaussian?

# Evaluated Topological Visualizations

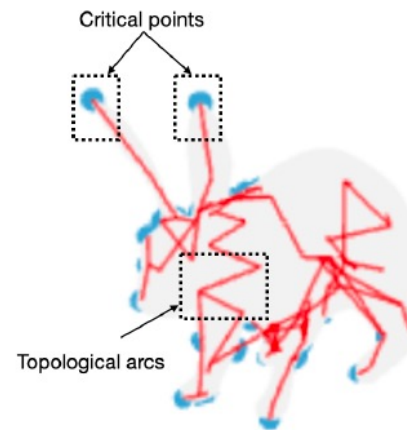
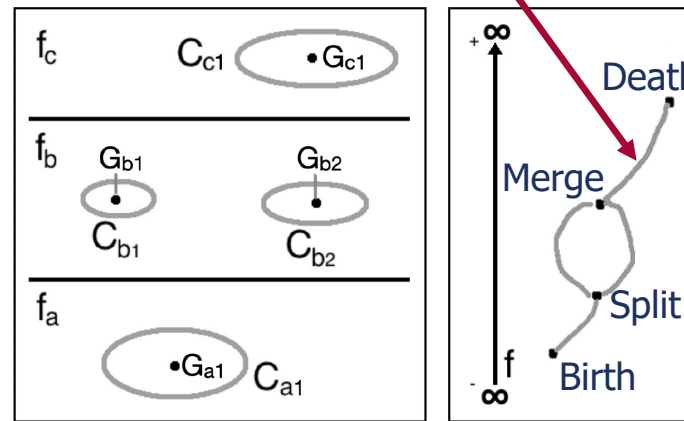
Isovalue  $f_b$  generates isocontour with two connected components  $C_{b1}$  and  $C_{b2}$

Isovalue  $f_a$  generates isocontour with single connected component  $C_a$



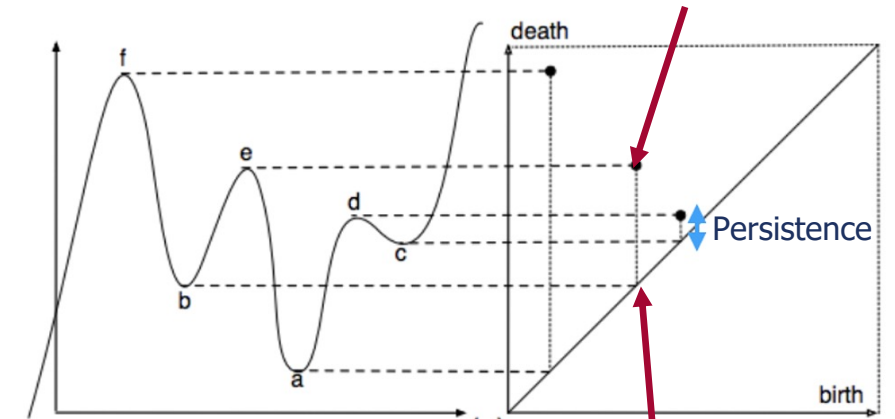
(a) Isocontours  
[Lorenson and Cline, 1987]

A point on arc indicates a connected component

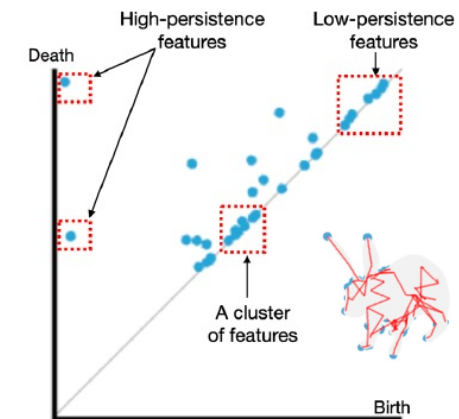


(b) Reeb graphs  
[Edelsbrunner and Harer, 2010]

Non-diagonal points represent death of a connected component



Diagonal corresponds to the birth time connected component



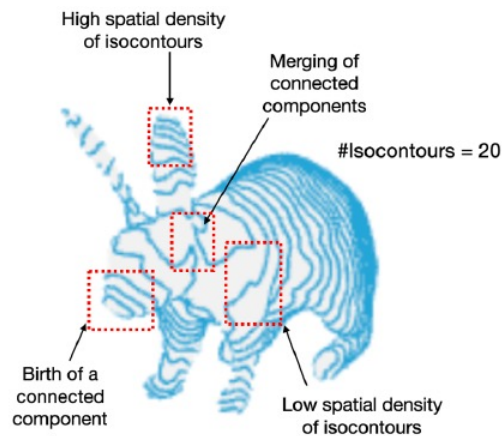
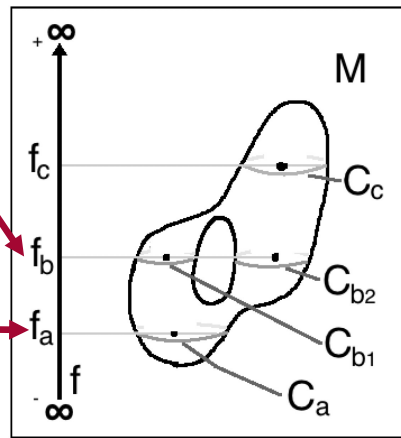
(c) Persistence diagram  
[Cohen-Steiner et al., 2005]



# Evaluated Topological Visualizations

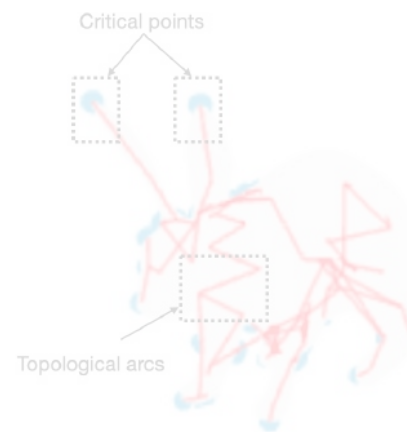
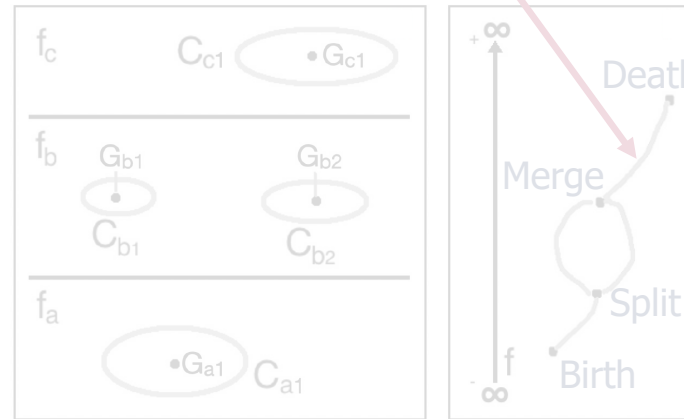
Isovalue  $f_b$  generates isocontour with two connected components  $C_{b1}$  and  $C_{b2}$

Isovalue  $f_a$  generates isocontour with single connected component  $C_a$



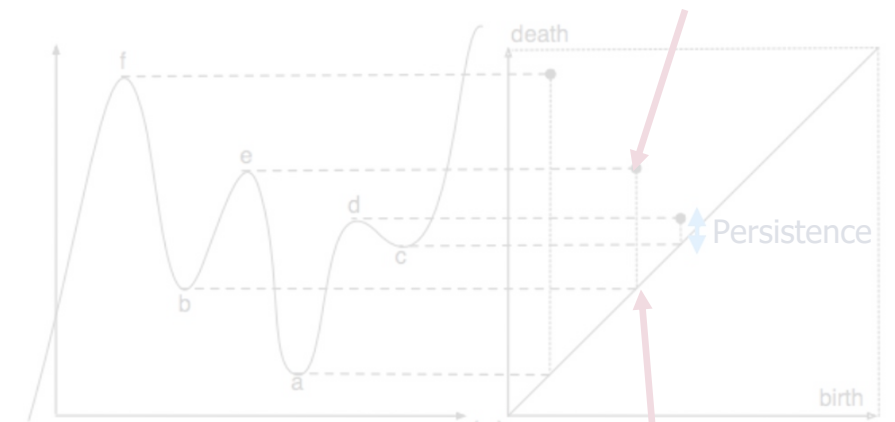
(a) Isocontours  
[Lorenson and Cline, 1987]

A point on arc indicates a connected component

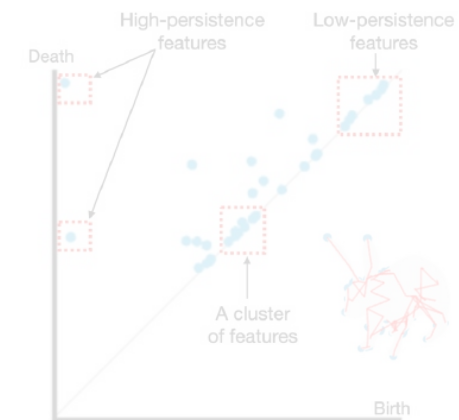


(b) Reeb graphs  
[Edelsbrunner and Harer, 2010]

Non-diagonal points represent death of a connected component



Diagonal corresponds to the birth time connected component

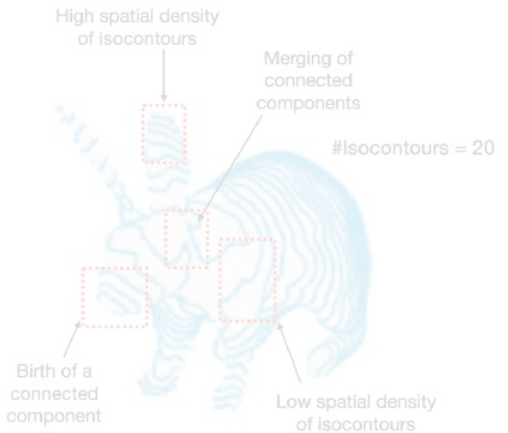
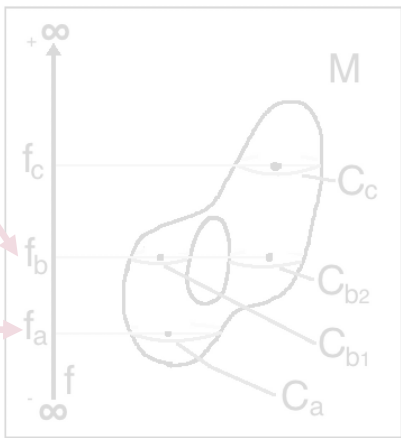


(c) Persistence diagram  
[Cohen-Steiner et al., 2005]

# Evaluated Topological Visualizations

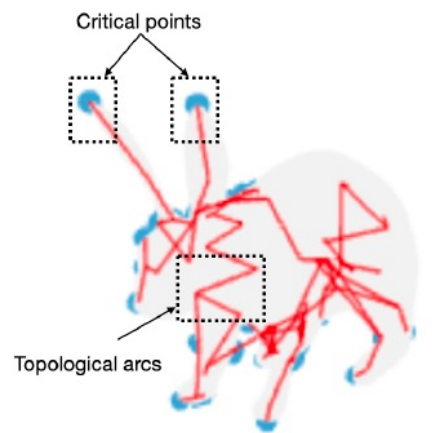
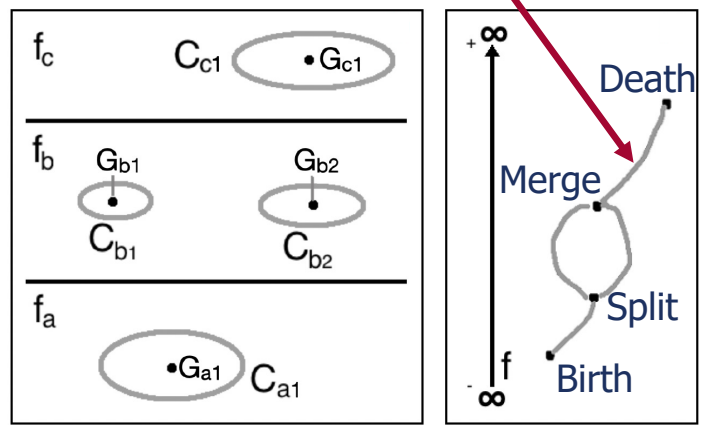
Isovalue  $f_b$  generates isocontour with two connected components  $C_{b1}$  and  $C_{b2}$

Isovalue  $f_a$  generates isocontour with single connected component  $C_a$



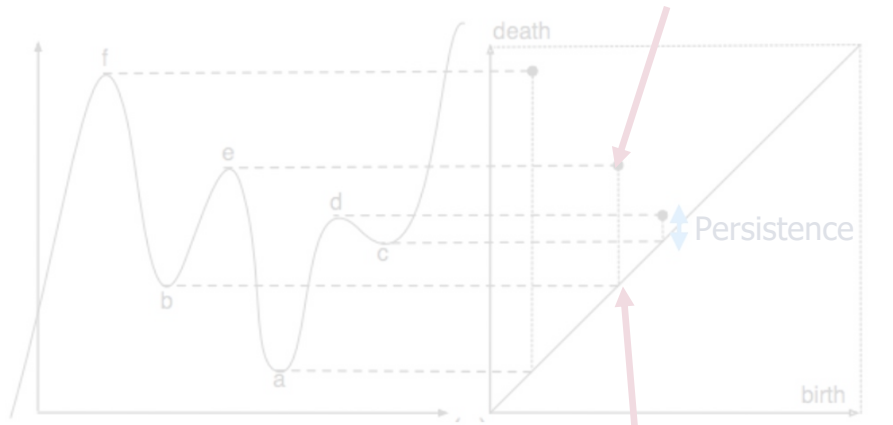
(a) Isocontours  
[Lorenson and Cline, 1987]

A point on arc indicates a connected component

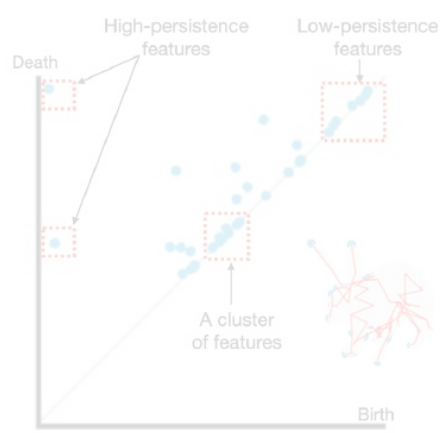


(b) Reeb graphs  
[Edelsbrunner and Harer, 2010]

Non-diagonal points represent death of a connected component



Diagonal corresponds to the birth time connected component

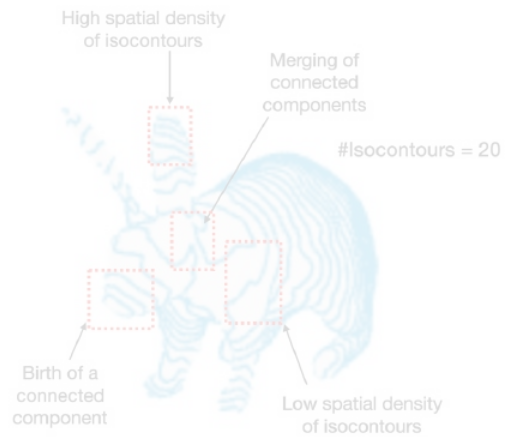
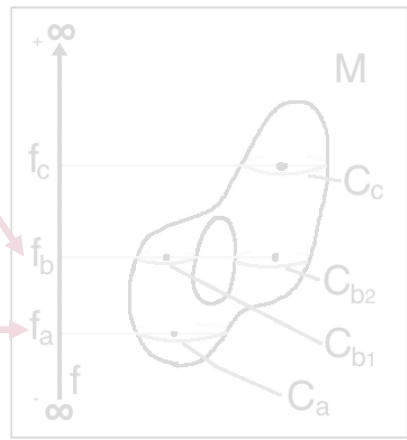


(c) Persistence diagram  
[Cohen-Steiner et al., 2005]

# Evaluated Topological Visualizations

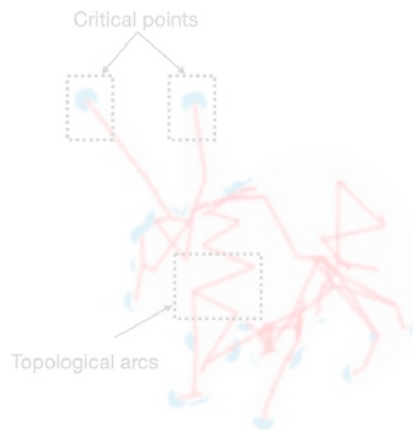
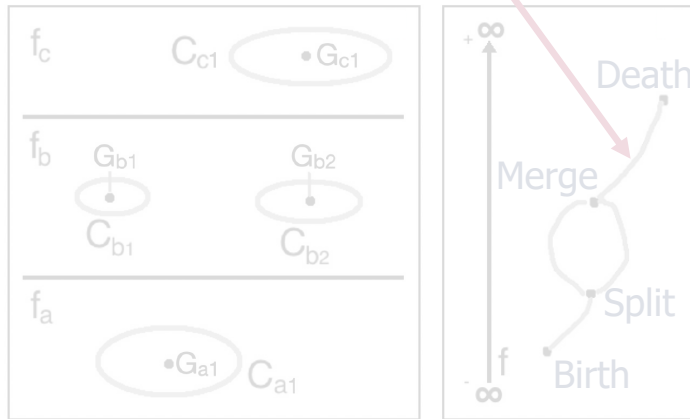
Isovalue  $f_b$  generates isocontour with two connected components  $C_{b1}$  and  $C_{b2}$

Isovalue  $f_a$  generates isocontour with single connected component  $C_a$



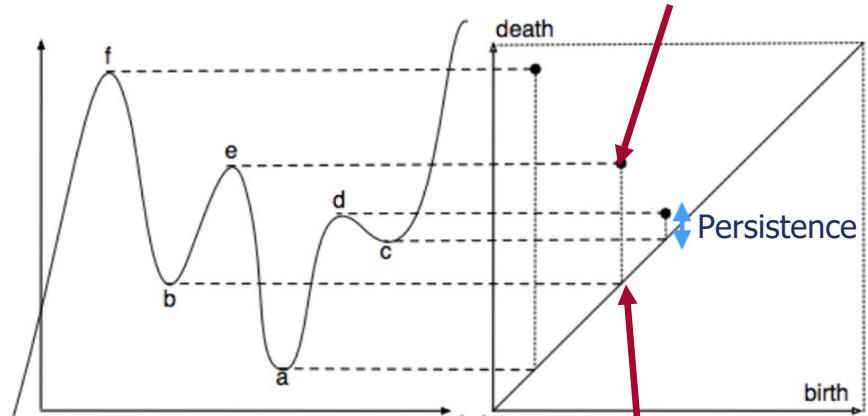
(a) Isocontours  
[Lorenson and Cline, 1987]

A point on arc indicates a connected component

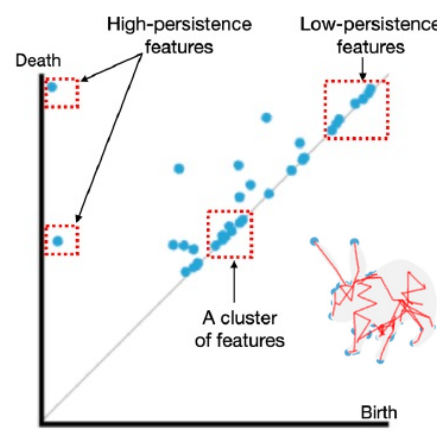


(b) Reeb graphs  
[Edelsbrunner and Harer, 2010]

Non-diagonal points represent death of a connected component

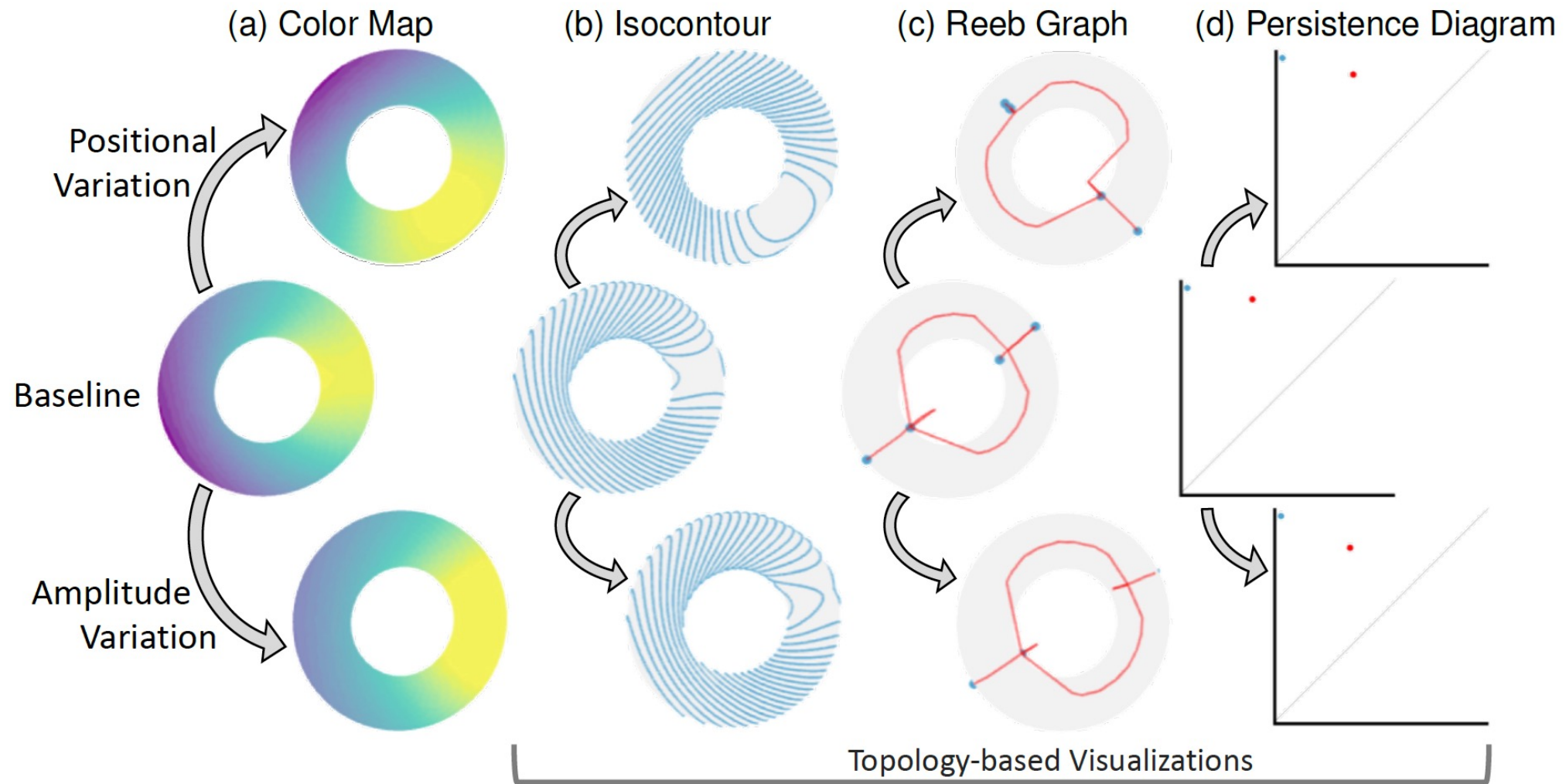


Diagonal corresponds to the birth time connected component



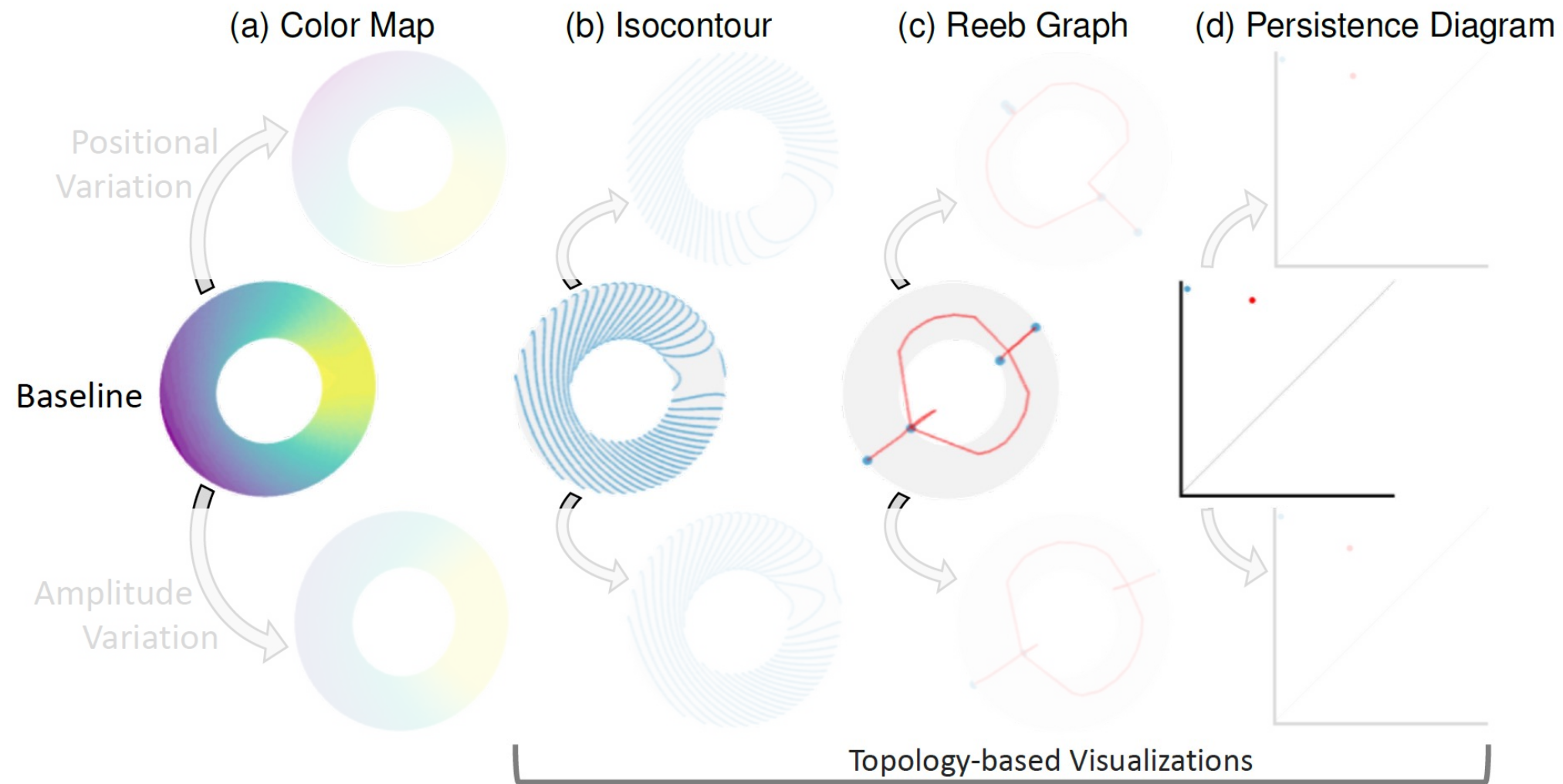
(c) Persistence diagram  
[Cohen-Steiner et al., 2005]

# Hypothesis

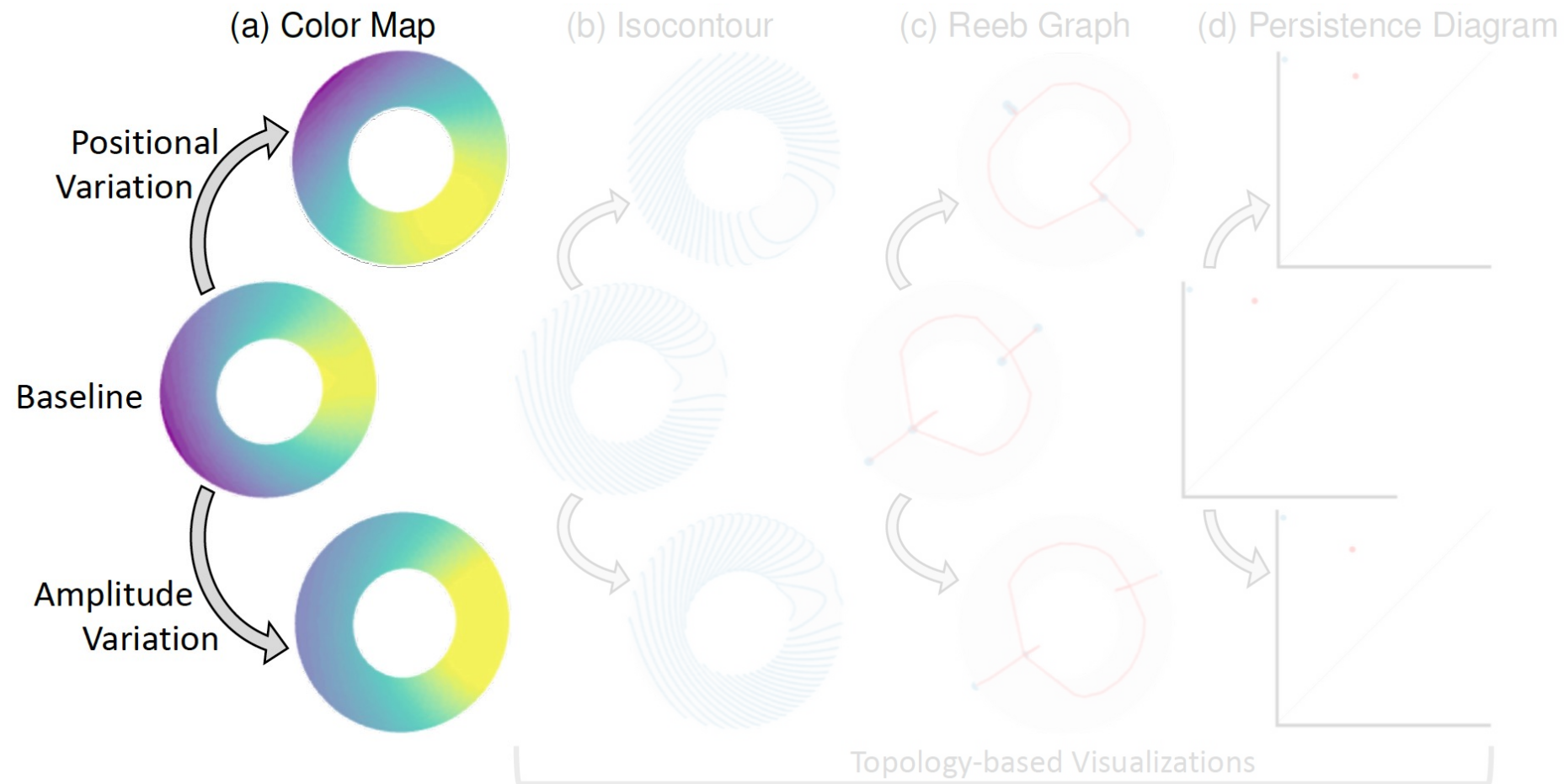




# Hypothesis

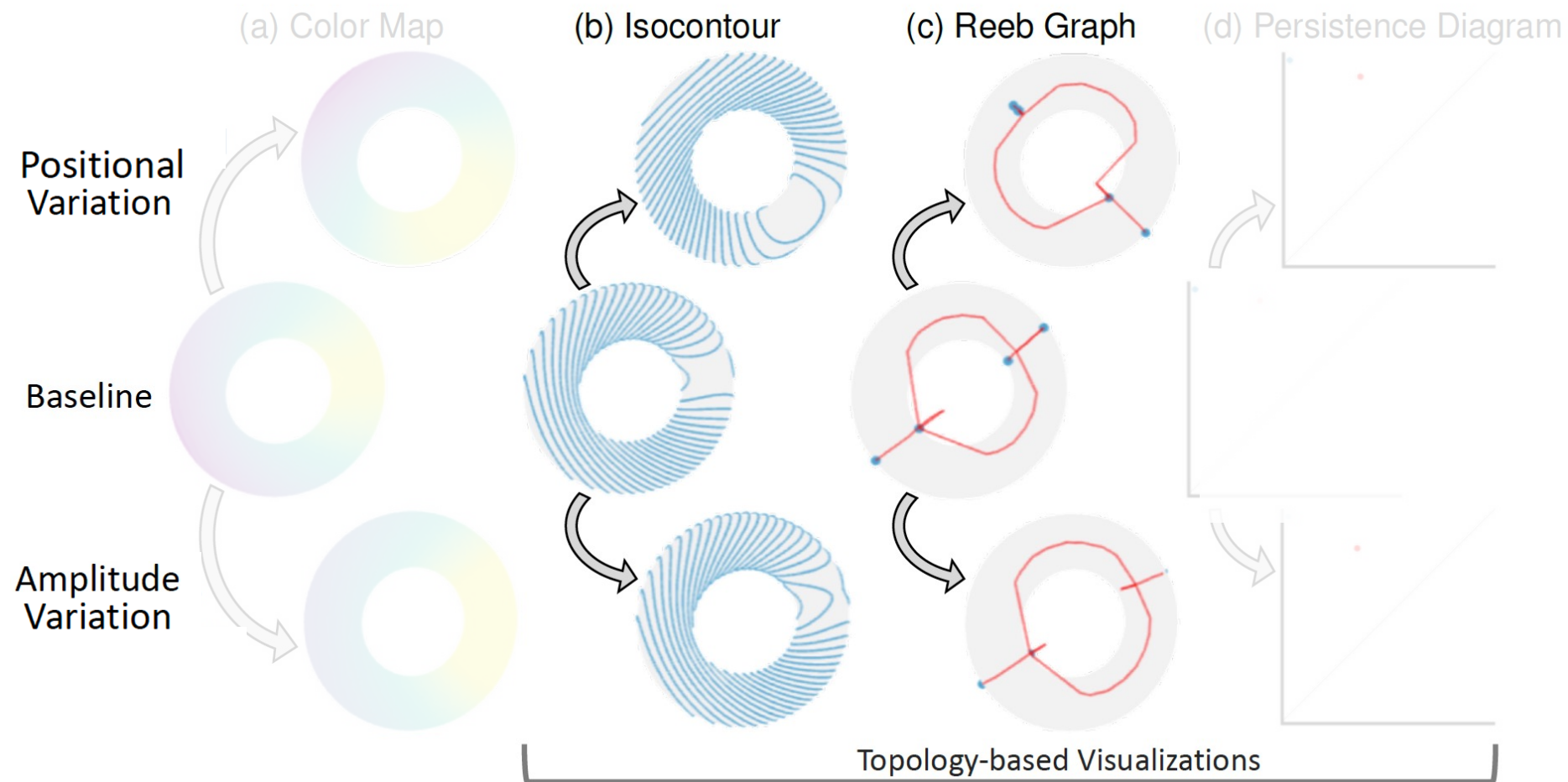


# Hypothesis



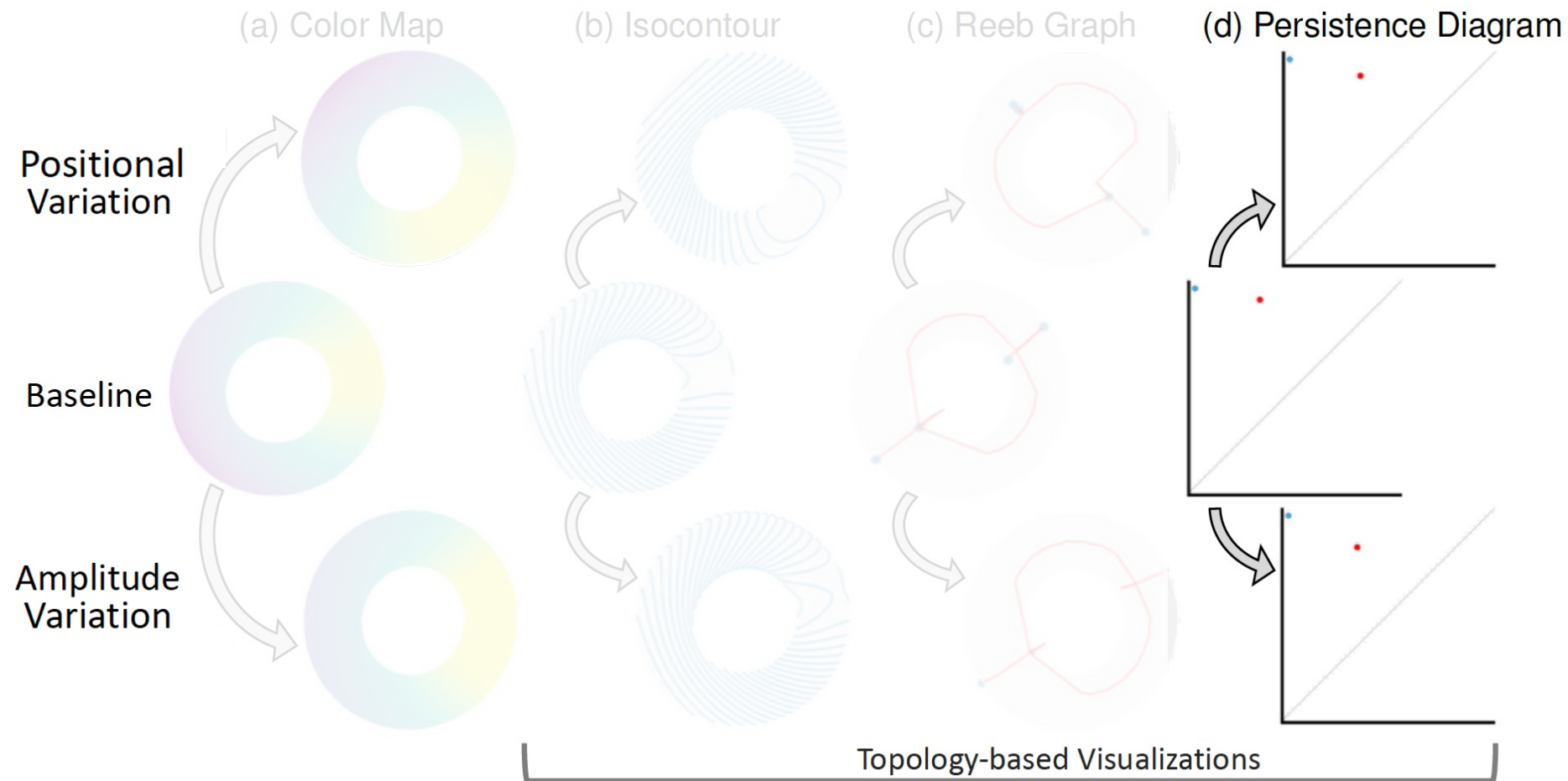
Visualization Method	Position sensitive	Amplitude sensitive
Color map	✓	✓

# Hypothesis



Visualization Method	Position sensitive	Amplitude sensitive
Color map	✓	✓
Isocontours	✓	✗
Reeb graph	✓	✗

# Hypothesis



Visualization Method	Position sensitive	Amplitude sensitive
Color map	✓	✓
Isocontours	✓	✗
Reeb graph	✓	✗
Persistence diagram	✗	✓

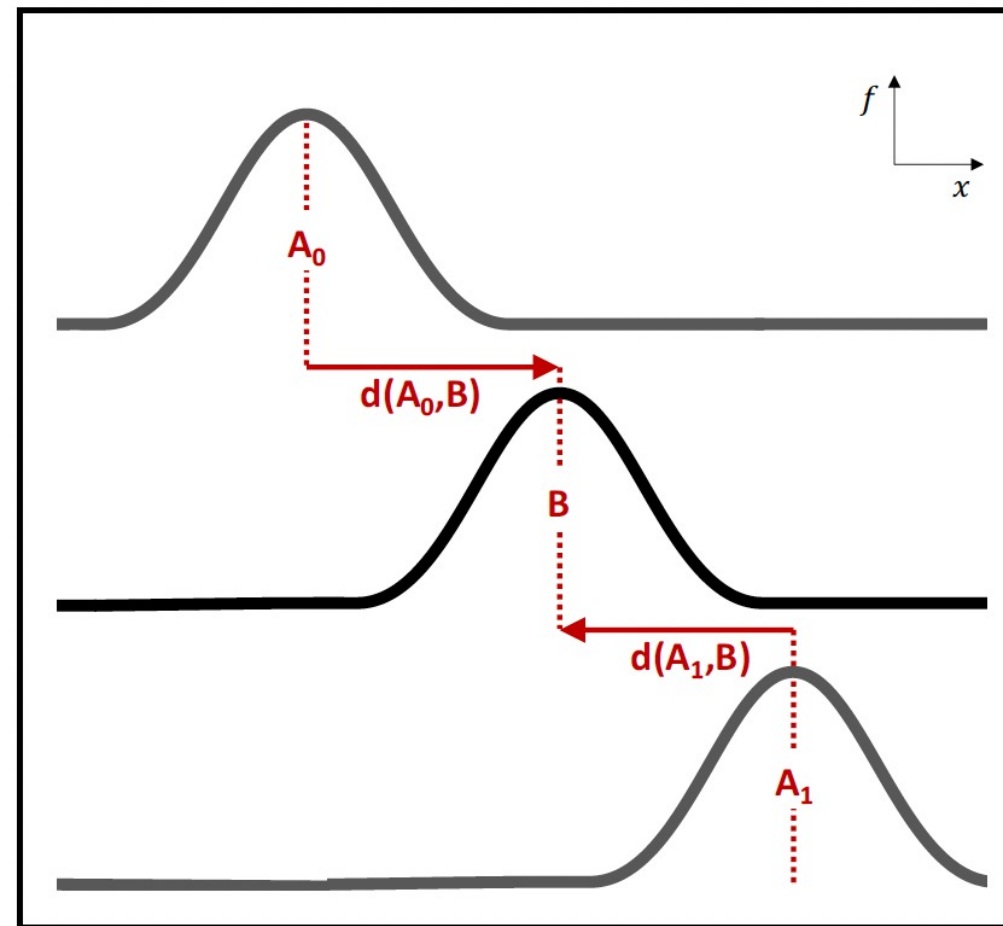


# Method: Sensitivity Analysis for Visualizations

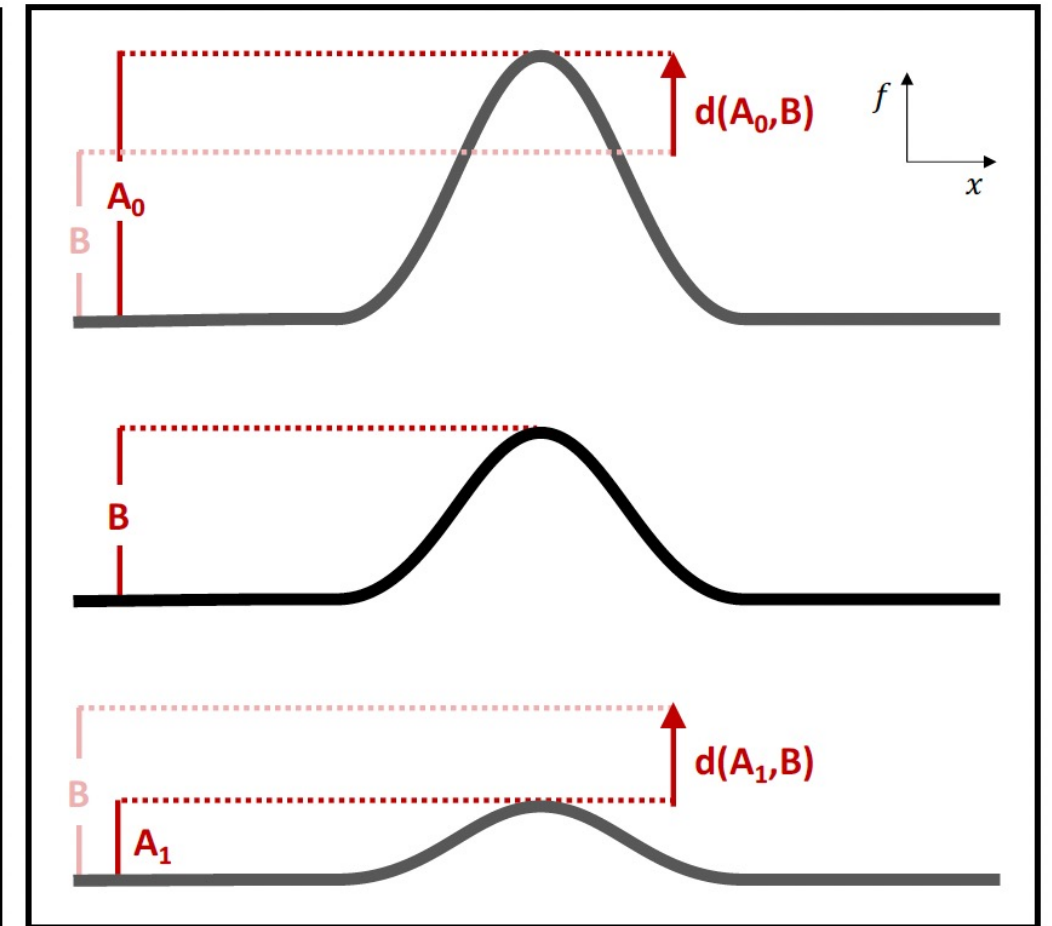


# 1D Example

Difficult to tell if variation A0 or A1 is closer to the baseline B



Positional Variation



Amplitude Variation

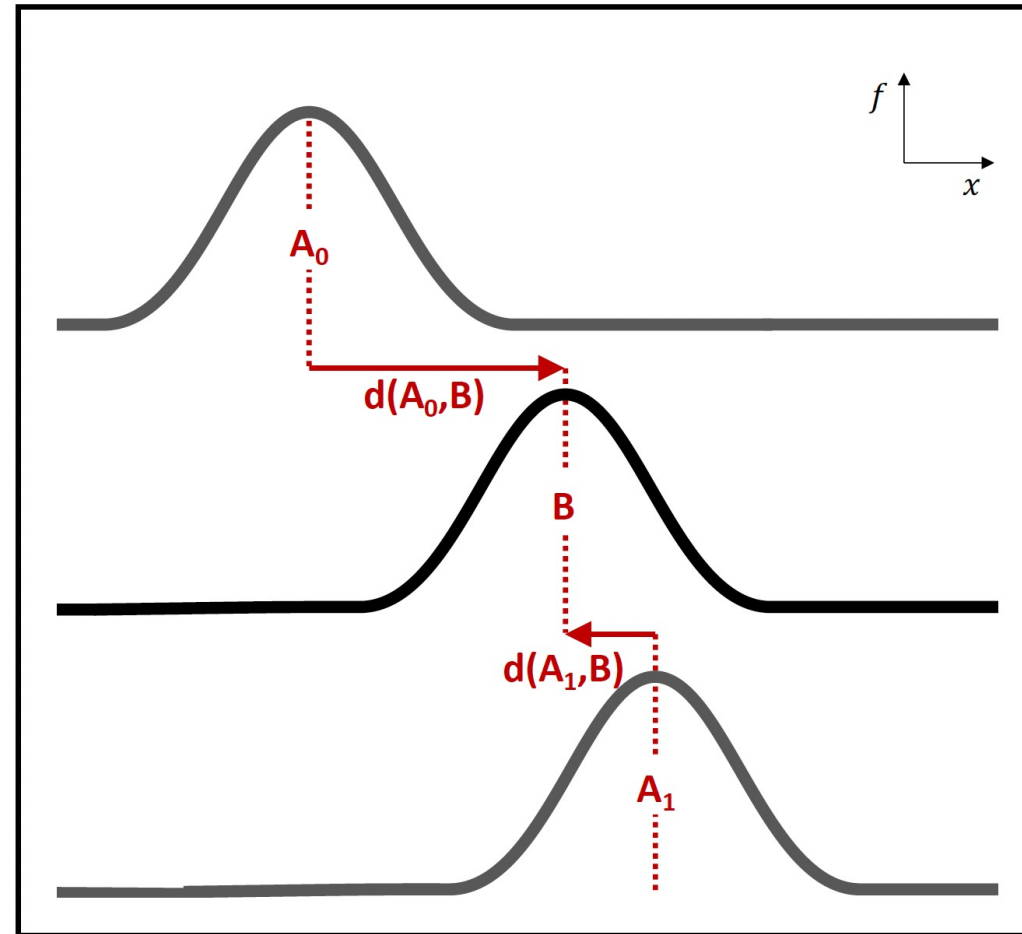
$$d(A_0, B) \approx d(A_1, B)$$

OR

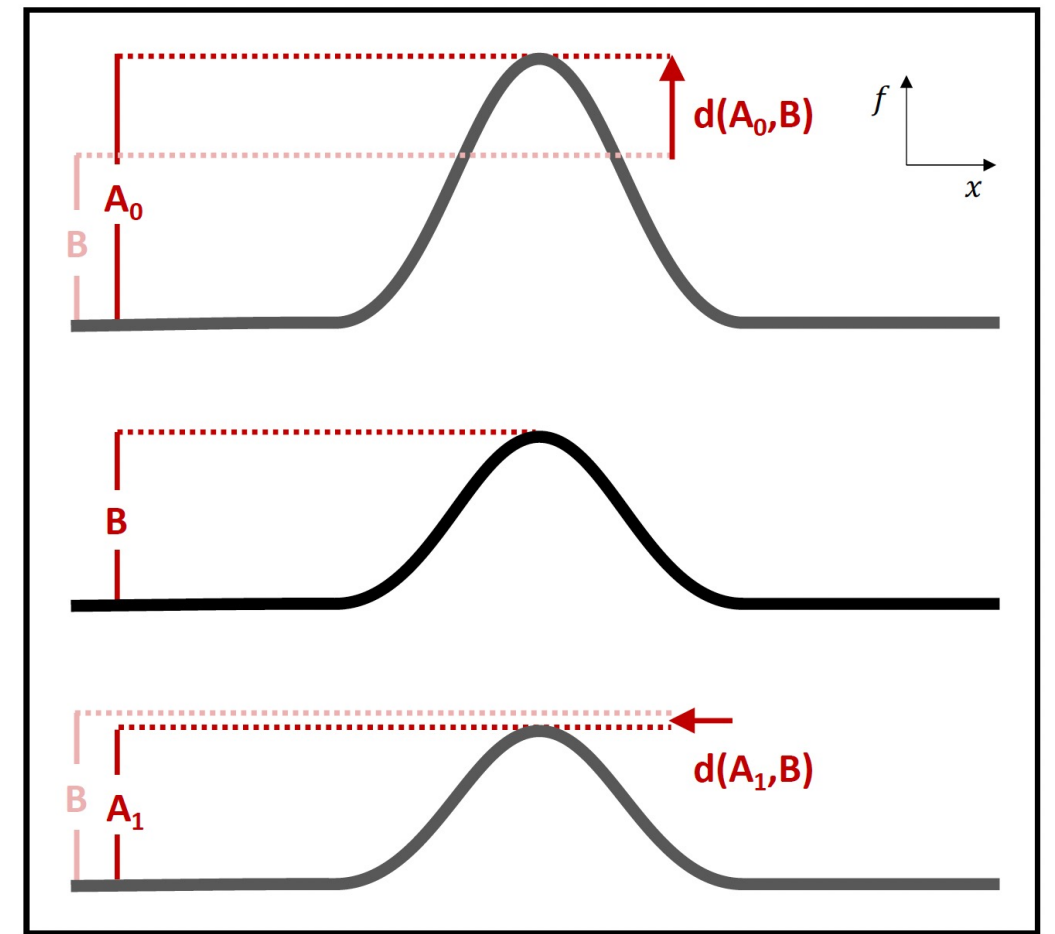
$$A' = |d(A_0, B) - d(A_1, B)| \approx 0$$

# 1D Example

Easier to tell if variation  $A_0$  or  $A_1$  is closer to the baseline  $B$



Positional Variation



Amplitude Variation

$$d(A_0, B) > d(A_1, B)$$

OR

$$A' = |d(A_0, B) - d(A_1, B)| > 0$$

# User Evaluation for 3D Topological Visualizations

46 seconds remaining

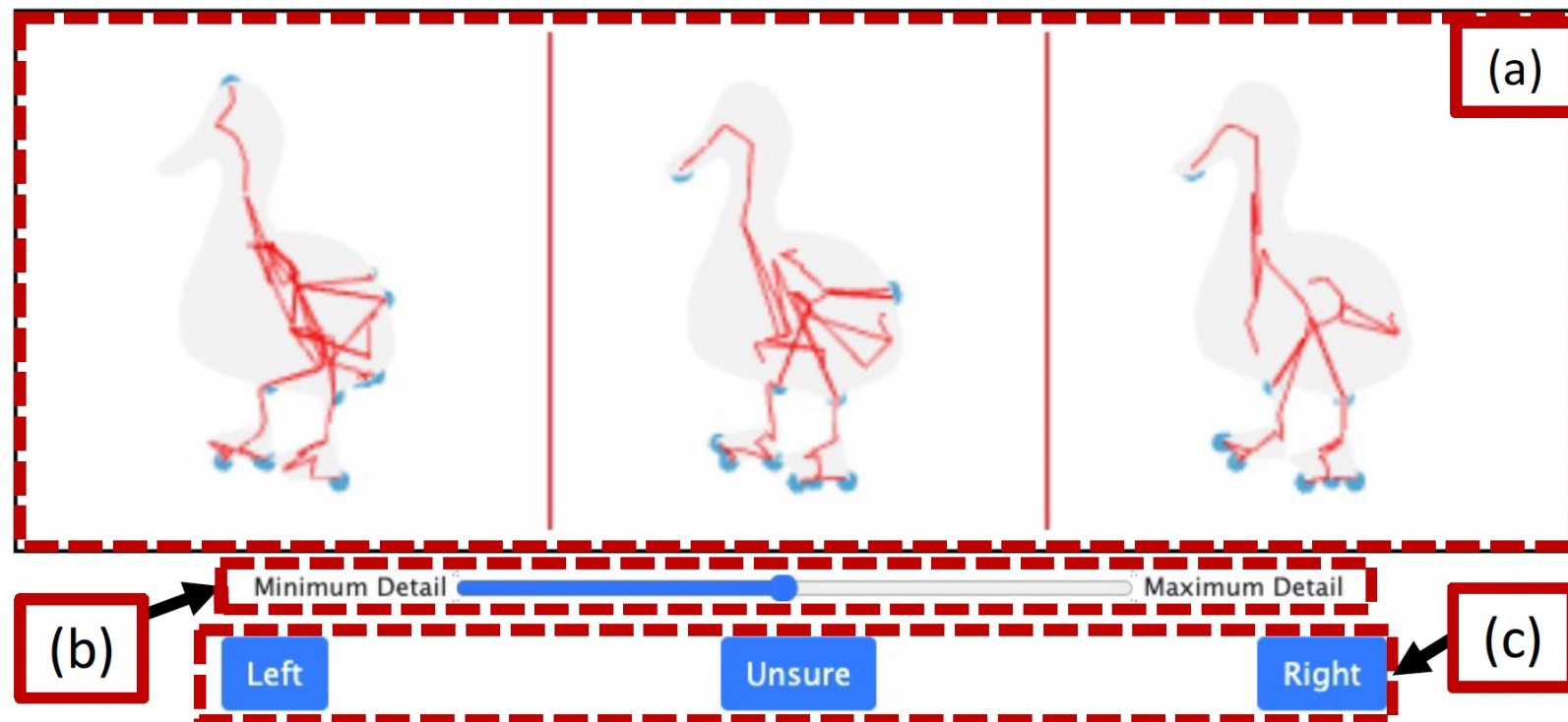
4 of 24

Which is more similar to the baseline – left or right?

Left-Option ( $A_0$ )

Baseline (B)

Right-Option ( $A_1$ )



(a) Users are presented baseline B in the centre and variations  $A_0$  and  $A_1$  on left and right, respectively.

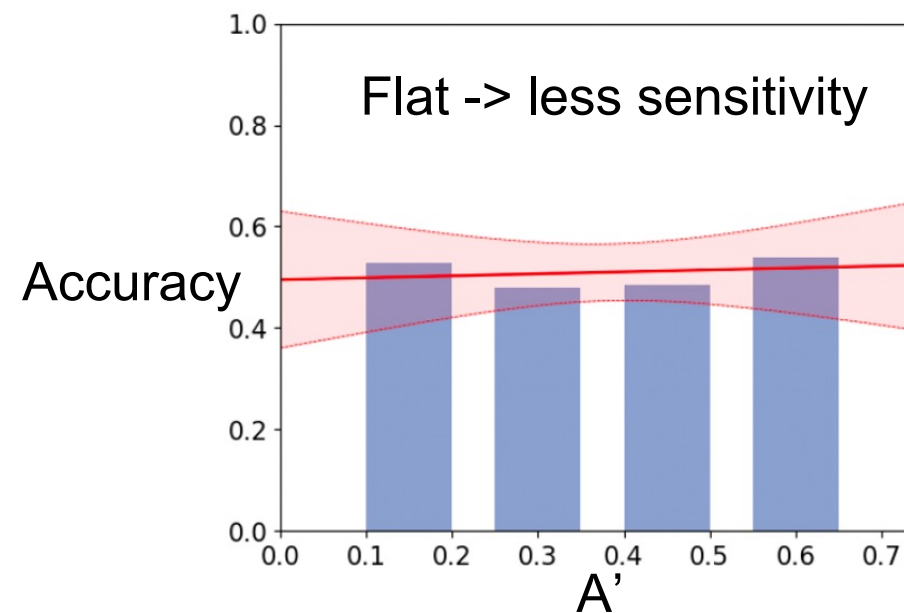
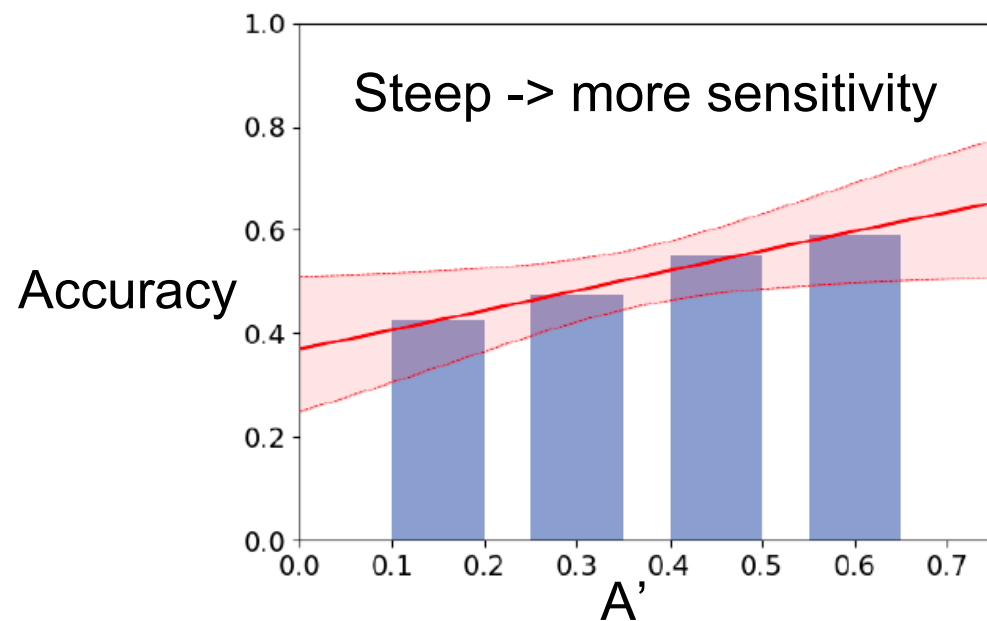
(b) Users can change the level of detail and rotate view and zoom in or out

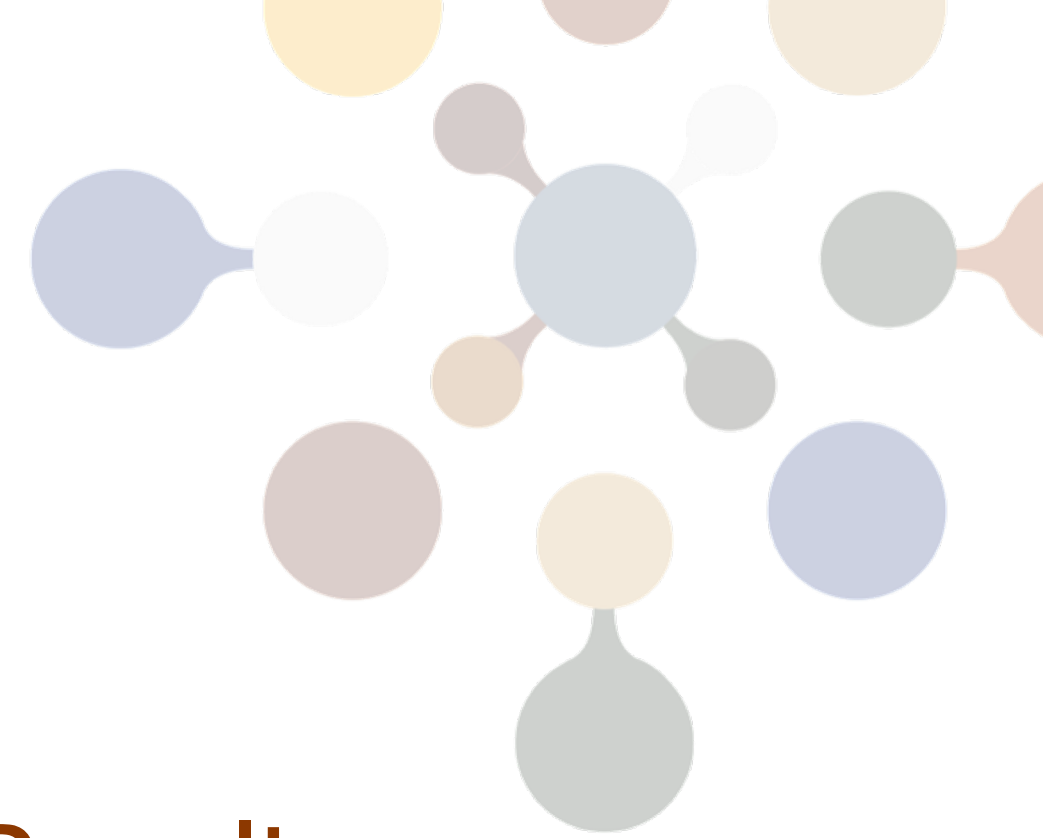
(c) Users need to visually select if visualization for variation  $A_0$  or  $A_1$  is closer to the visualization for baseline B

Remember that you can move the camera to see a different angle and zoom in or out if looking at a 3D model. You can also change the level of detail if the slider is available.

# Our Approach for Measuring Sensitivity

- Single experimental trial has an associated measure  $A' = |d(A_0, B) - d(A_1, B)|$  (Hidden from users, but known to the designers of the experiment)
- Small  $A'$  : We expect users to make random guess (close to 50% accuracy)  
Large  $A'$  : We expect users to be more accurate
- Sensitivity: Plot selection accuracy Vs.  $A'$  and estimate the rate of change in accuracy





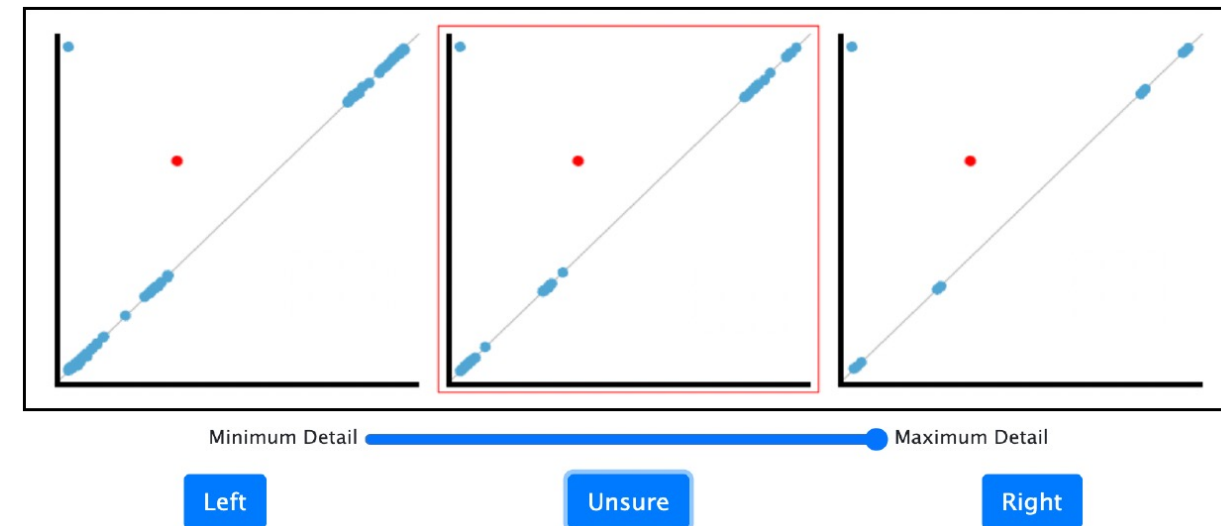
# Experimental Setup and Results



# Experimental Setup

- 102 non-expert participants, 24 experimental trials per participant, sensitivity analysis based on  $102 \times 24 = 2448$  trials
- Each user was presented with tutorial and practice session to get familiar with visualization types and the features to look for
- Between-subject experiment with the following parameters across 24 experimental trials
  - 1 trial per 3D model
  - 6 trials per visualizations type: {color map, isocontour, Reeb graph, persistence diagram}
  - 12 trials per variation type: {position, scale}
  - 6 trials per  $A'$ : {0.15, 0.30, 0.45, 0.60}
  - 8 trials per SNR value: {80, 90, 100}
  - 3 trials per NOF in the range: [2, 9]
- Conducted study on Amazon Mechanical Turk (users with HIT approval rate > 95%)

Practice question for persistence diagram



Here's some tips to help: Here the diagonal line is your friend. First check the distribution of points along that diagonal and see if you can spot immediate similarities. Then check for dots further away from the diagonal. From this you should be able to gauge how similar a chart is with the baseline.

# Results: Accuracy

$$\text{Accuracy} = N_{\text{corr}}/N_{\text{trials}}$$

Positional variation

Method	Accuracy				Overall
	$A' = .15$	$A' = .30$	$A' = .45$	$A' = .60$	
Color maps	62.3%	61.4%	56.6%	67.4%	<b>64.0%</b> ( $p < .001$ )
Isocontours	54.7%	59.3%	56.7%	56.0%	<b>58.8%</b> ( $p = .002$ )
Reeb graph	42.7%	47.4%	55.1%	58.9%	<b>52.5%</b> ( $p = .208$ )
Persistence diagrams	56.5%	66.2%	55.2%	50.6%	<b>57.8%</b> ( $p = .002$ )

Amplitude variation

Method	Accuracy				Overall
	$A' = .15$	$A' = .30$	$A' = .45$	$A' = .60$	
Color maps	48.8%	52.9%	60.3%	67.1%	<b>59.3%</b> ( $p < .001$ )
Isocontours	48.7%	49.4%	54.9%	62.5%	<b>55.8%</b> ( $p = .022$ )
Reeb graph	52.8%	48.1%	48.5%	53.9%	<b>52.2%</b> ( $p = .243$ )
Persistence diagrams	47.4%	57.5%	65.7%	81.3%	<b>63.0%</b> ( $p < .001$ )

- $A' = |d(A0, B) - d(A1, B)|$
- **Our hypothesis:**  
Small  $A'$ : lower expected accuracy  
Large  $A'$ : higher expected accuracy
- Our hypothesis statistically significant for all visualization types except for Reeb graphs

# Results: Accuracy

$$\text{Accuracy} = N_{\text{corr}}/N_{\text{trials}}$$

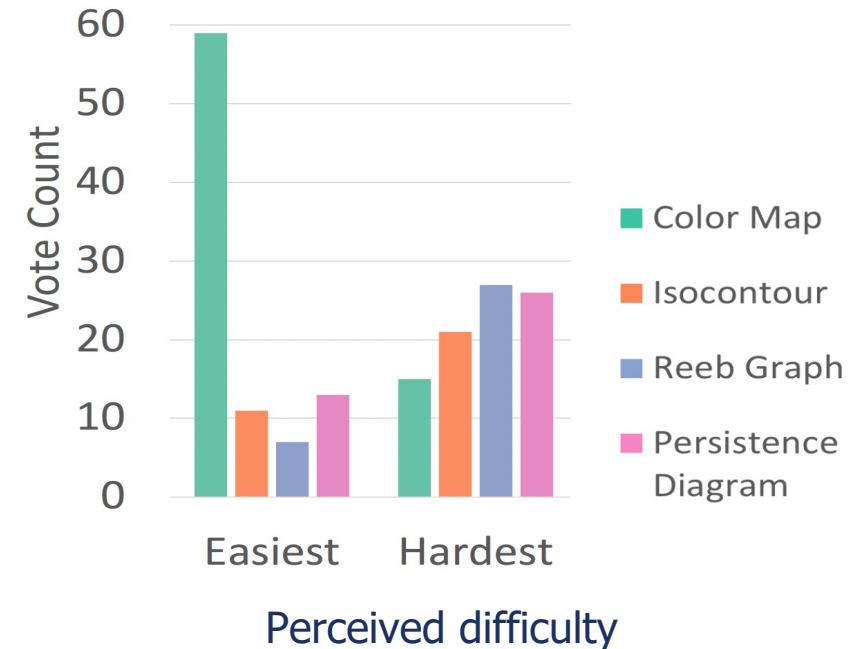
Positional variation

Method	Accuracy				Overall
	$A' = .15$	$A' = .30$	$A' = .45$	$A' = .60$	
Color maps	62.3%	61.4%	56.6%	67.4%	<b>64.0%</b> ( $p < .001$ )
Isocontours	54.7%	59.3%	56.7%	56.0%	<b>58.8%</b> ( $p = .002$ )
Reeb graph	42.7%	47.4%	55.1%	58.9%	<b>52.5%</b> ( $p = .208$ )
Persistence diagrams	56.5%	66.2%	55.2%	50.6%	<b>57.8%</b> ( $p = .002$ )

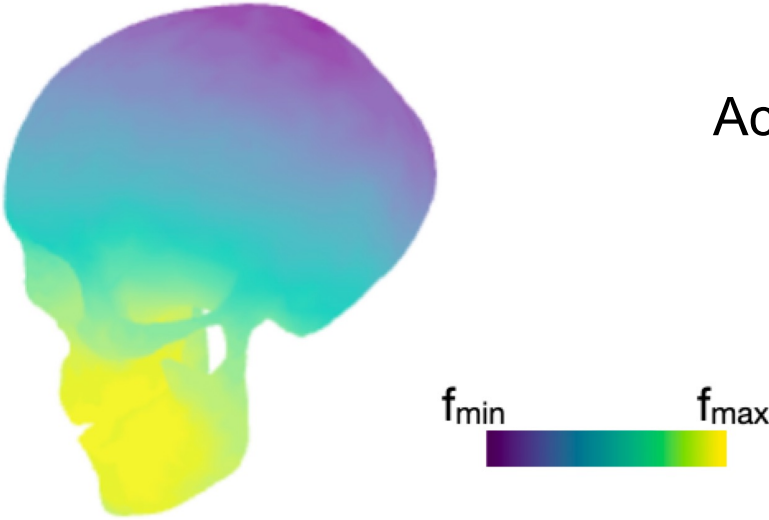
Amplitude variation

Method	Accuracy				Overall
	$A' = .15$	$A' = .30$	$A' = .45$	$A' = .60$	
Color maps	48.8%	52.9%	60.3%	67.1%	<b>59.3%</b> ( $p < .001$ )
Isocontours	48.7%	49.4%	54.9%	62.5%	<b>55.8%</b> ( $p = .022$ )
Reeb graph	52.8%	48.1%	48.5%	53.9%	<b>52.2%</b> ( $p = .243$ )
Persistence diagrams	47.4%	57.5%	65.7%	81.3%	<b>63.0%</b> ( $p < .001$ )

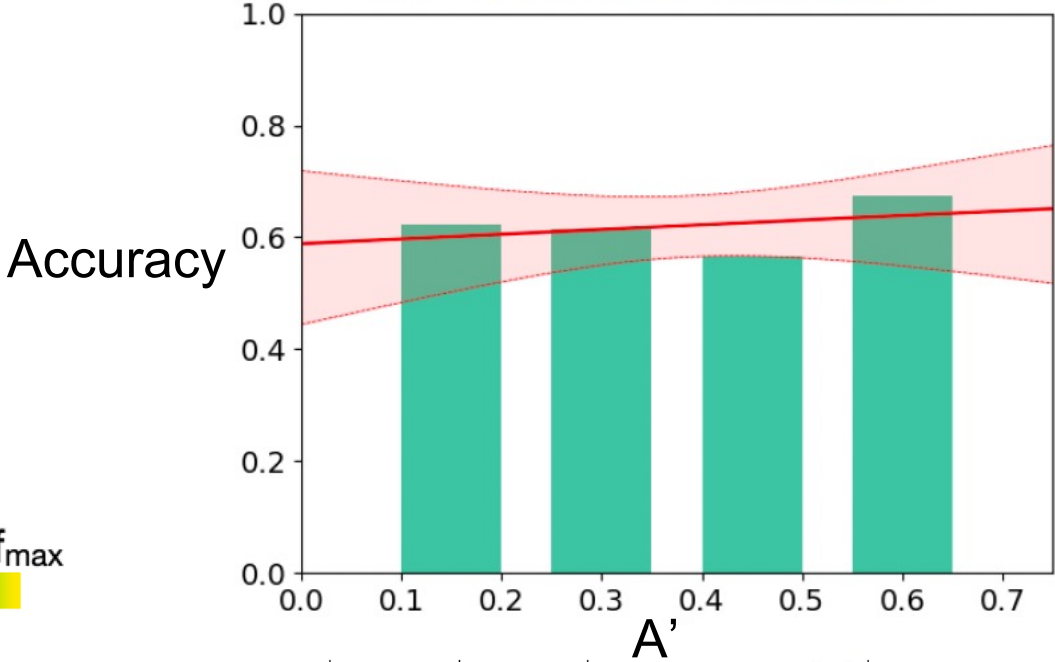
Reeb graphs displayed overall lower accuracy due to their discrete, high-frequency nature



# Results: Color Map Sensitivity



*Positional variation*

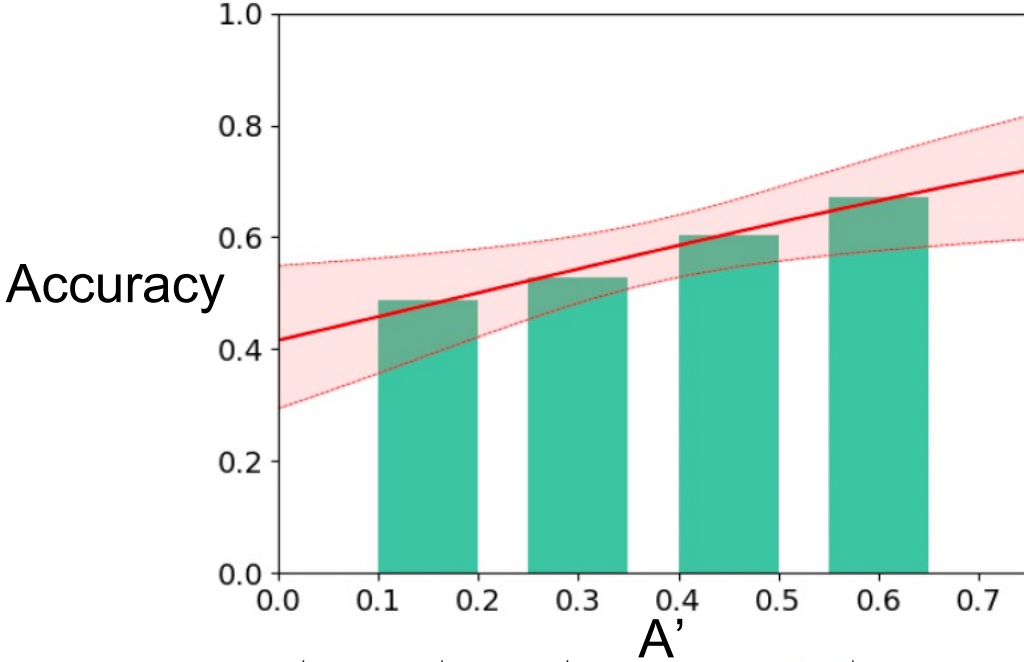


Param.	Coef.	SE	$z$	$P >  z $	95% CI
$A'$	0.355	0.703	0.505	0.613	[-1.022, 1.732]
(intcp)	0.357	0.297	1.204	0.228	[-0.224, 0.939]

Color maps ( $p = .613$ )

Hypothesis: *sensitive*  
**hypothesis rejected**

*Amplitude variation*



Param.	Coef.	SE	$z$	$P >  z $	95% CI
$A'$	1.708	0.672	2.541	0.011	[0.391, 3.026]
(intcp)	-0.340	0.274	-1.241	0.215	[-0.876, 0.197]

Color maps ( $p = .010$ )

Hypothesis: *sensitive*  
**hypothesis validated**

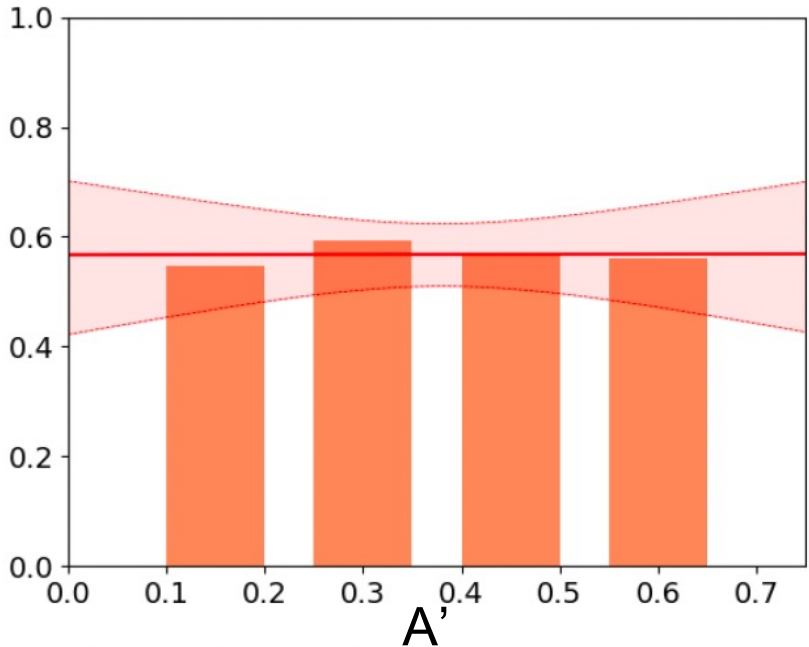


# Results: Isocontour Sensitivity



Accuracy

*Positional variation*

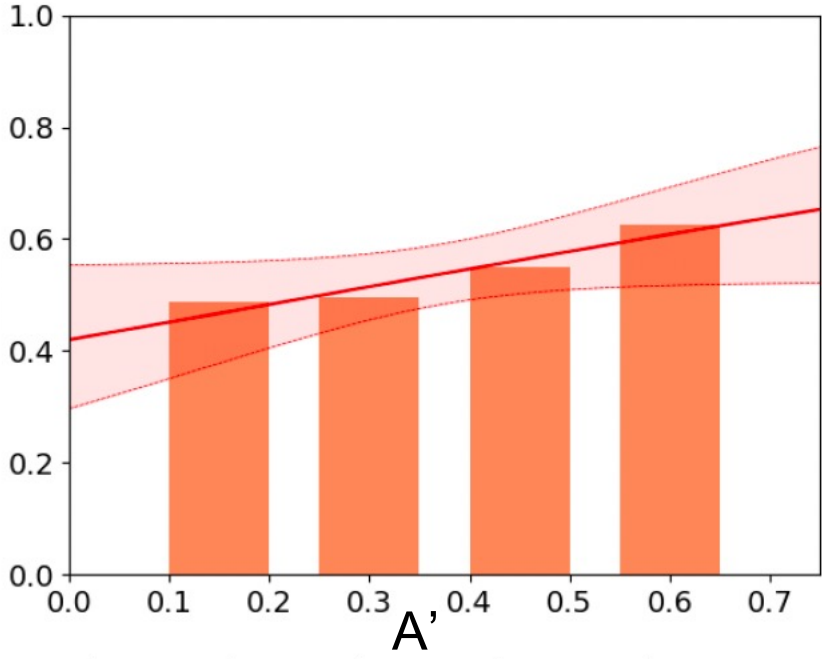


Param.	Coef.	SE	$z$	$P >  z $	95% CI
$A'$	0.008	0.720	0.011	0.991	[-1.403, 1.419]
(intcp)	0.270	0.298	0.906	0.365	[-0.314, 0.855]

Isocontours ( $p = .991$ )

Hypothesis: *sensitive*  
**hypothesis rejected**

*Amplitude variation*



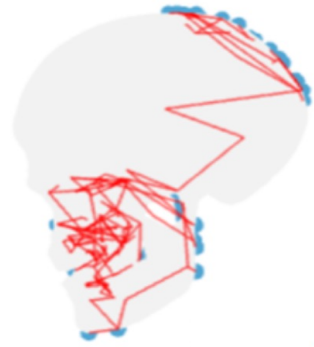
Param.	Coef.	SE	$z$	$P >  z $	95% CI
$A'$	1.272	0.676	1.881	0.060	[-0.054, 2.598]
(intcp)	-0.323	0.275	-1.173	0.241	[-0.862, 0.217]

Isocontours ( $p = .059$ )

Hypothesis: *not sensitive*  
**ambiguous result**

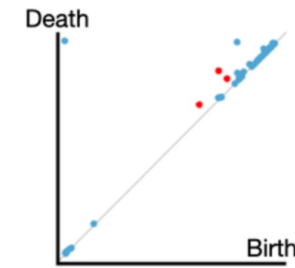
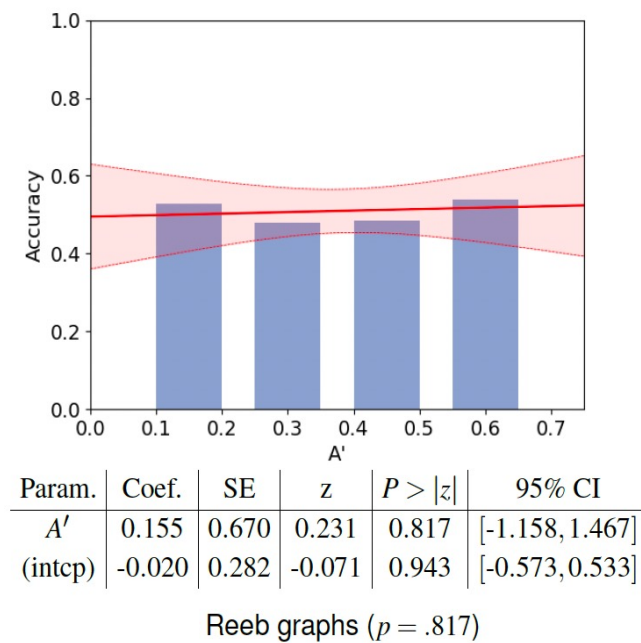
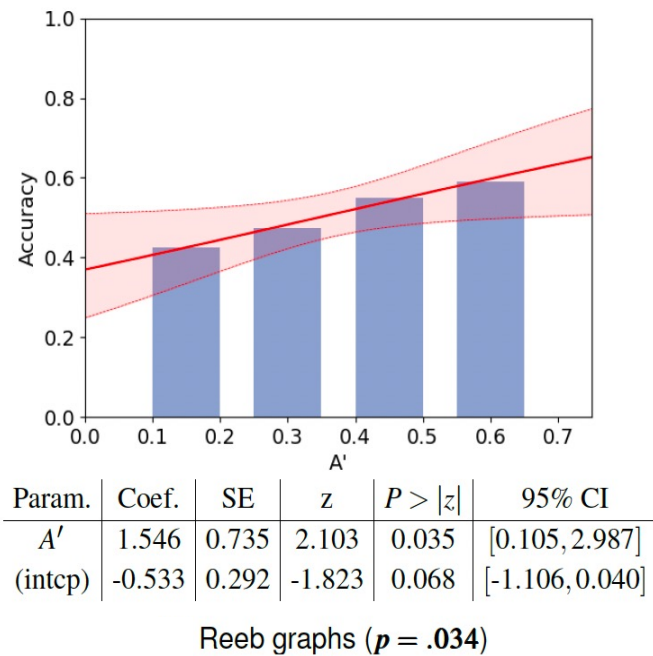


# Results: Reeb Graph and Persistence Diagram Sensitivity



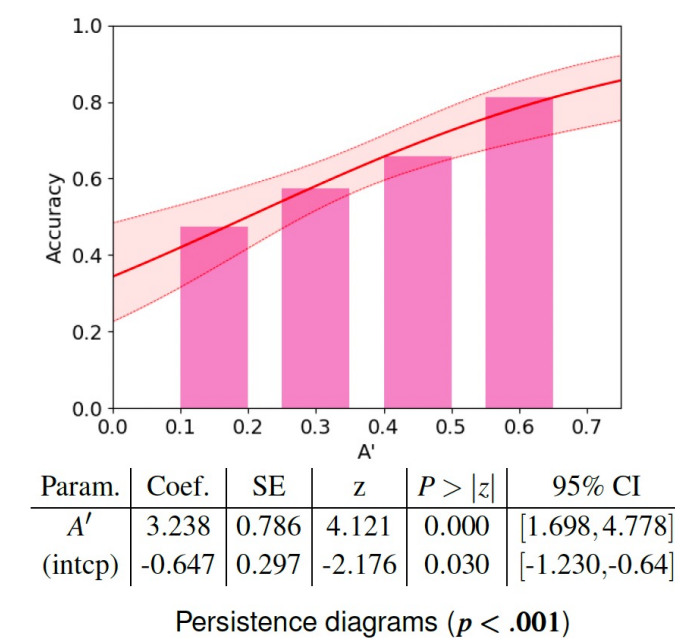
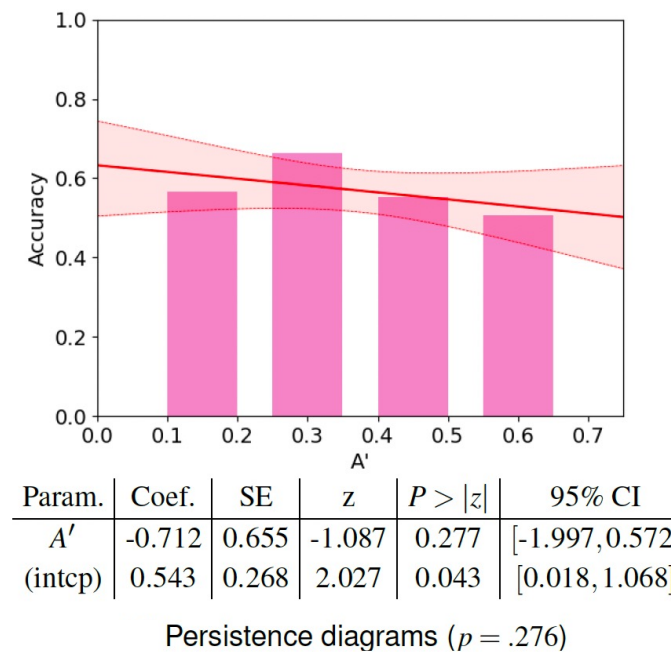
*Positional variation*

*Amplitude variation*



*Positional variation*

*Amplitude variation*



Hypothesis was validated in the all cases!

# Observations and Implications

## Hypothesis

Visualization Method	Position Sensitive	Amplitude Sensitive
Color map	Yes	Yes
Isocontours	Yes	No
Reeb graph	Yes	No
Persistence diagram	No	Yes

## Observation

Visualization Method	Position Sensitive	Amplitude Sensitive
Color map	Yes	No
Isocontours	No	Maybe
Reeb graph	Yes	No
Persistence diagram	No	Yes

- No single visualization to rule them all!
- Need for multiview visualization or enhancement in existing visualization design for better portrayal of features and enhanced sensitivity

# Limitations and Future Work

- **Task:**

Limitation: Task of comparison of scalar fields.

Future work: Study different tasks performed with scalar fields.

- **Participant Pool:**

Limitation: Participant pool comprises mainly non-experts and can have effect on accuracy statistics. We note that experts may be influenced by familiarity bias (Dunning-Kruger effect [Kurger and Dunning, 1999])

Future work: Cover more diverse pool of participants.

- **Data and Features Evaluated:**

Limitation: Data is modeled as a mixture of isotropic Gaussian functions on 2D manifolds, scale and position variation for evaluation.

Future work: Need study for non-isotropic Gaussian functions, 3D volumetric datasets, variations other than position and scale.

- **Visualizations Evaluated:**

Limitation: Our study is limited to color maps (viridis), isocontours, Reeb graphs, and persistence diagrams.

Future work: Other visualization variations, e.g., planer Reeb graphs, Morse complexes, Multiview visualizations yet remain to be investigated.

# Thank you for your attention!

This research is supported by a grant from the National Science Foundation (III-2316496) and by the U.S. Department of Energy (DOE) RAPIDS-2 SciDAC project under contract number DE-AC05-00OR22725.

For any questions, please contact me at:

Email: [athawaletm@ornl.gov](mailto:athawaletm@ornl.gov)