





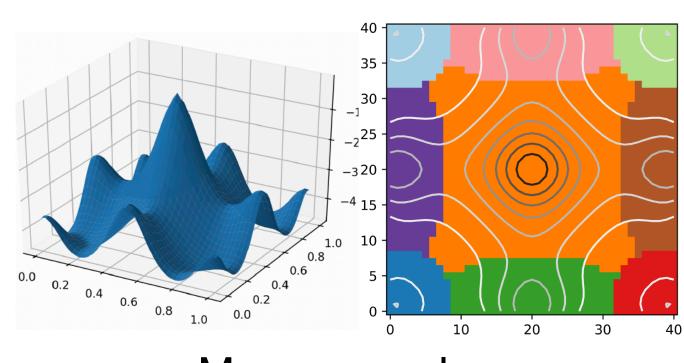
Statistical Analysis for Uncertainty Quantification and Visualization of Scientific Data

Tushar Athawale,
Scientific Computing & Imaging (SCI) Institute, University of Utah

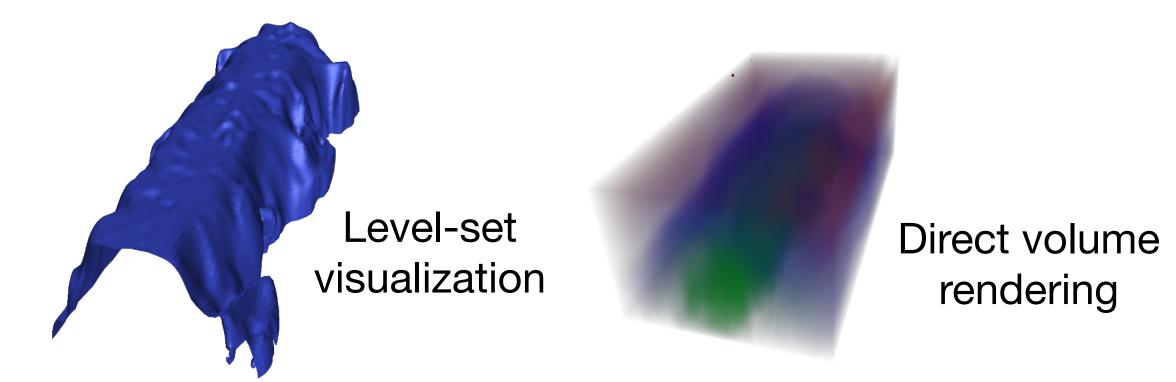
Advisor: Dr. Chris R. Johnson

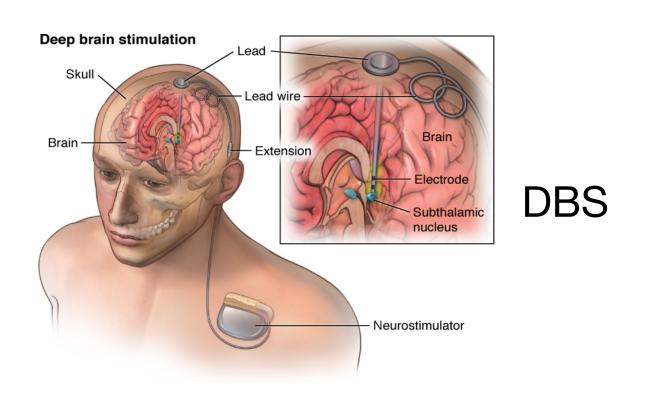
Outline

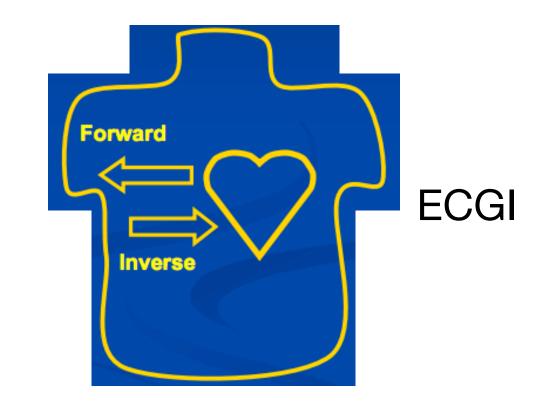
- Need for uncertainty visualization
- Uncertainty visualization for level sets
 - Marching squares/cubes algorithm in uncertain data, e.g., ensemble simulations
- Other applications of uncertainty visualization
 - Morse complex visualizations for ensembles
 - Direct volume rendering using ray casting
 - Deep brain stimulation (DBS) imaging
 - Electrodcardiographic Imaging (ECGI)
- Conclusion and future work



Morse complex visualization





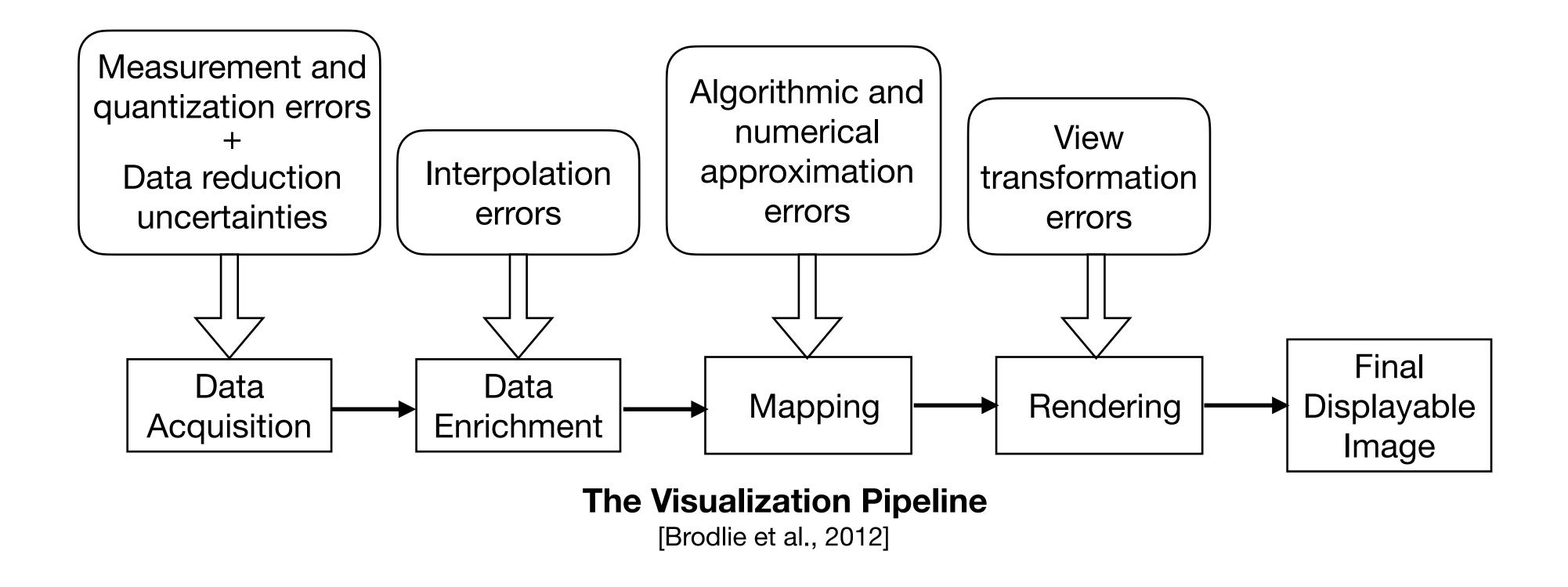




Why Visualize Uncertainty? [Johnson and Sanderson, 2004]

Uncertainty Visualization of Level Sets

Minimize risks associated with scientific decisions

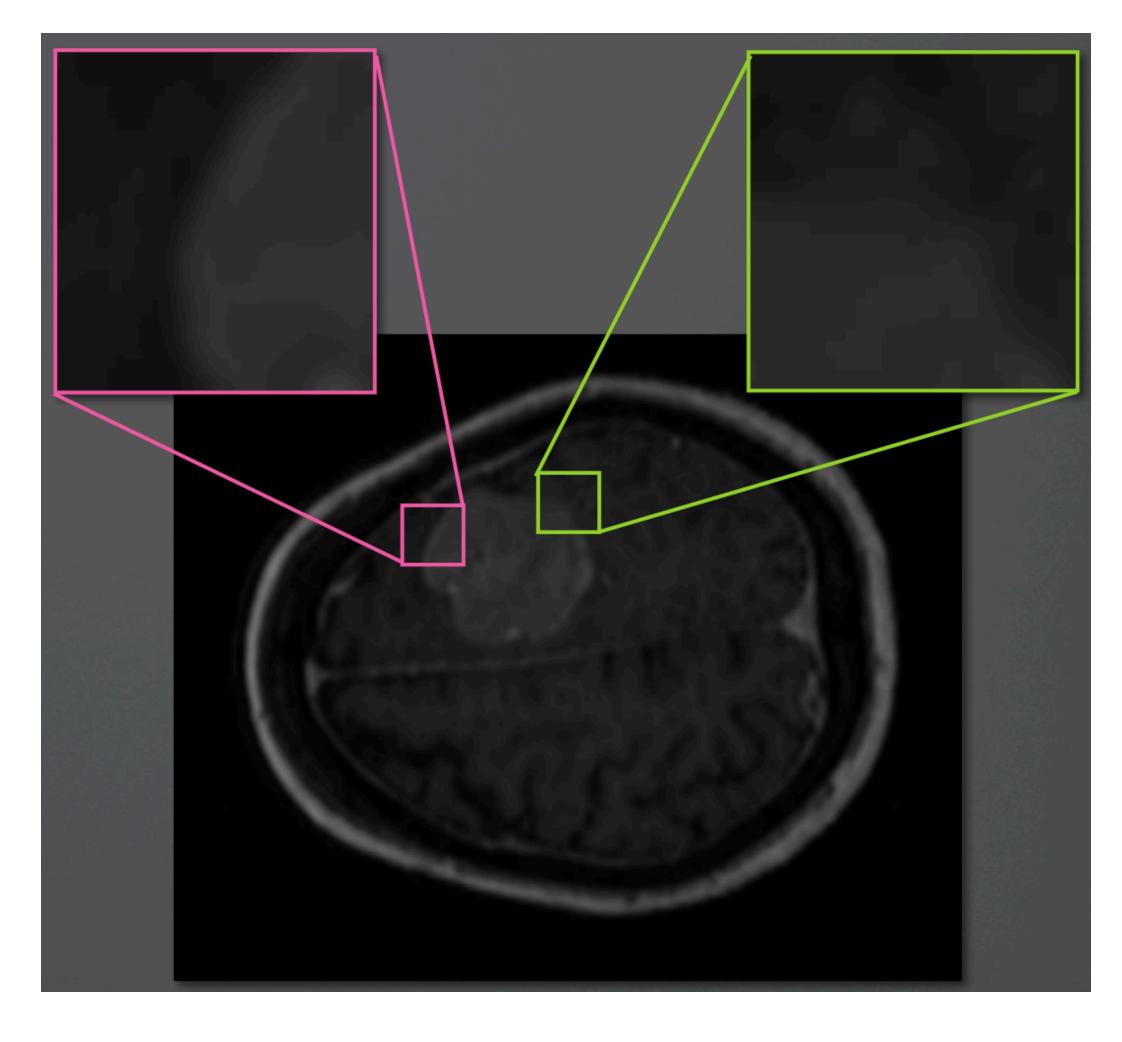




Why Visualize Uncertainty?

Uncertainty Visualization of Level Sets

Can you identify a tumor boundary?

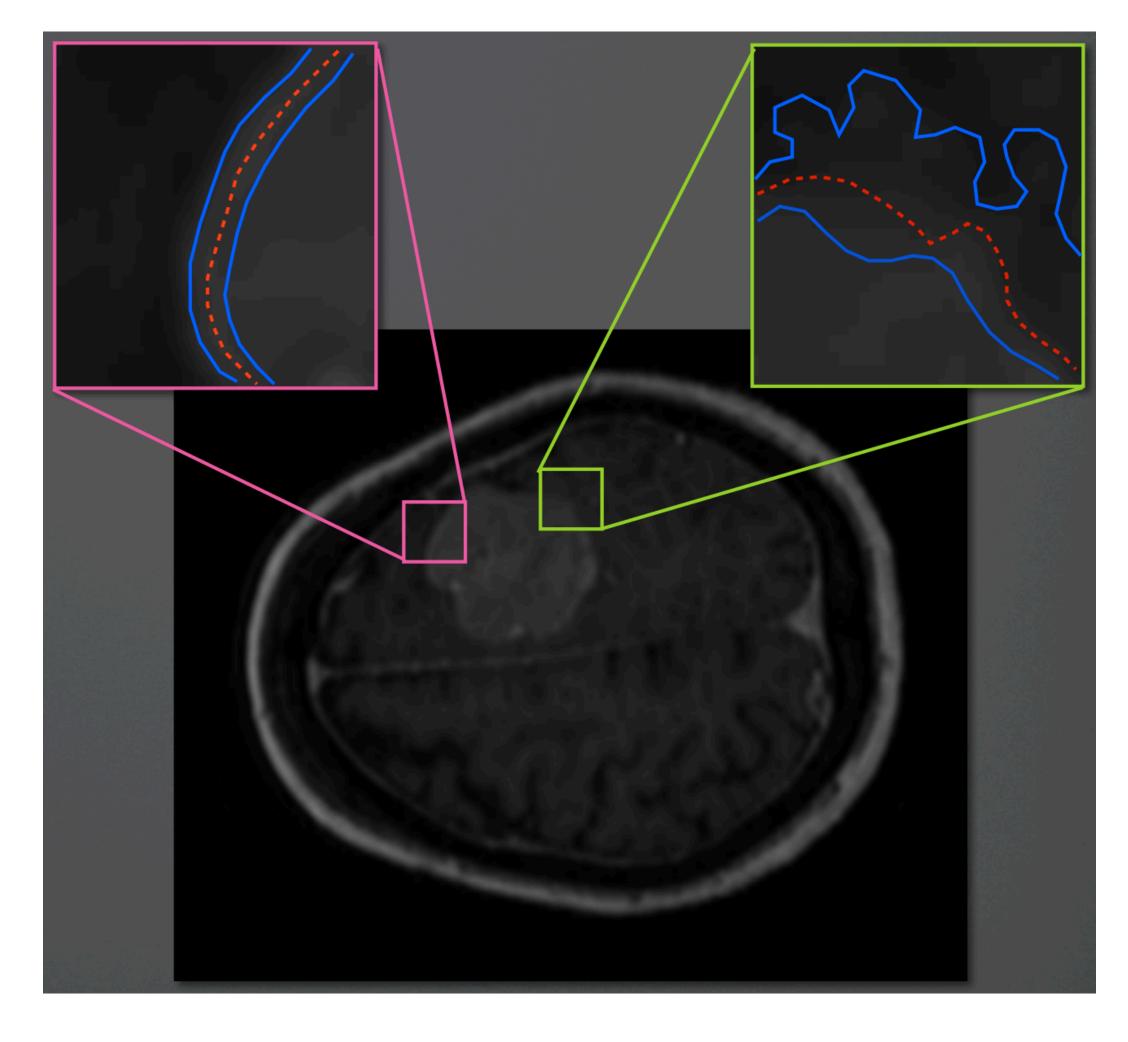




Why Visualize Uncertainty?

Uncertainty Visualization of Level Sets

Can you identify a tumor boundary?



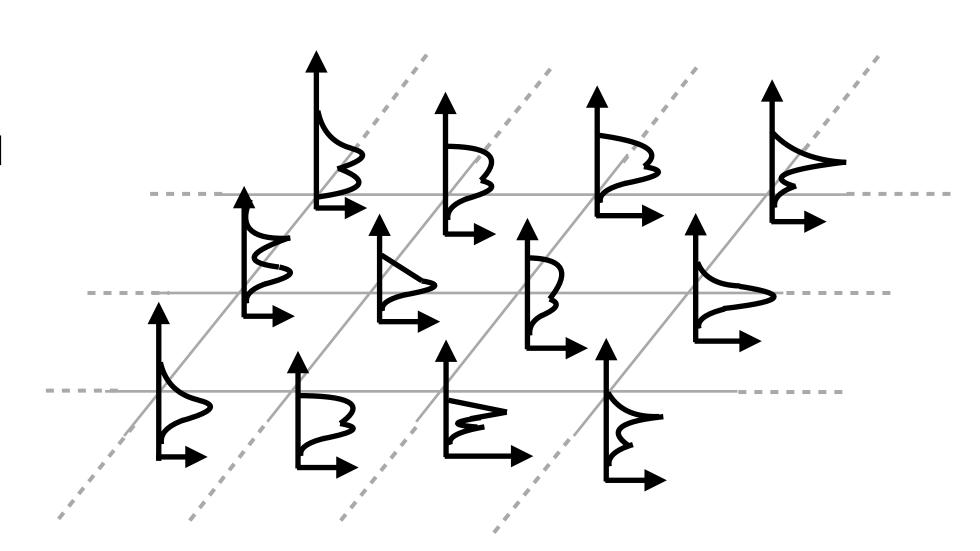


Data Reduction and Distributions

Uncertainty Visualization of Level Sets

Distributions: Hixel representation/ in-situ statistical summaries for large-scale data [Thompson et al., 2011, Lehmann and Jung, 2014, Hazarika et al., 2018]

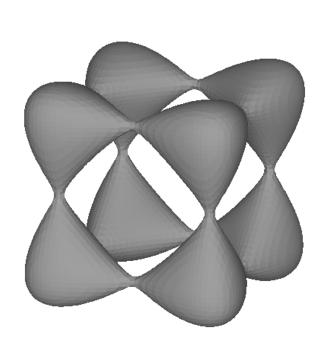
Ensemble Data: Multiple simulations for PDE solutions (Store min/max, Approximate distributions from samples)



Hixel representation: Storing a histogram/probability distribution at each vertex of a scalar grid

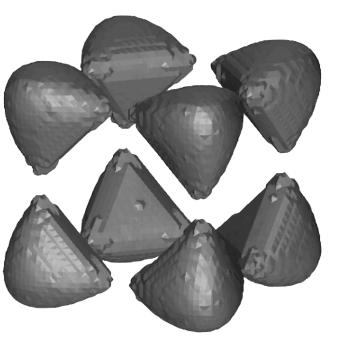


Data Reduction and Distributions



Ground truth

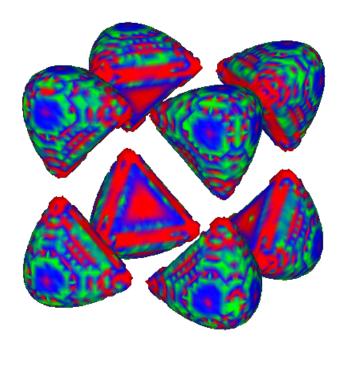
Memory consumption = 100*X



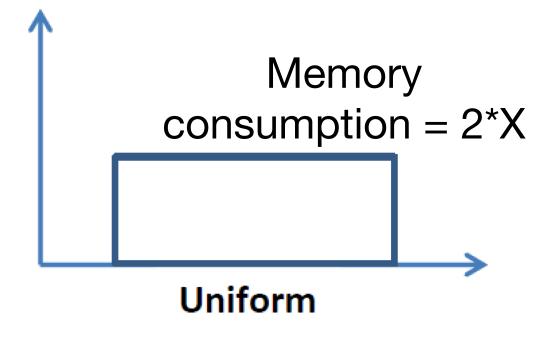
Mean

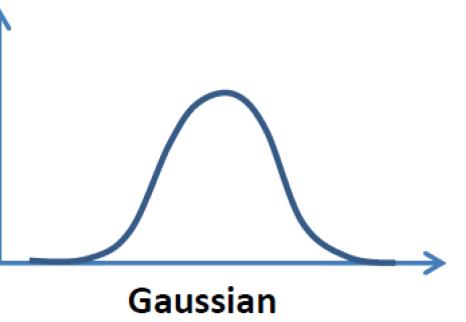
Memory consumption = X

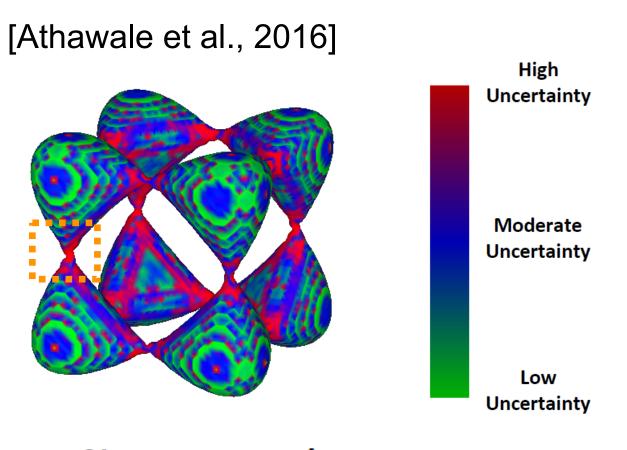
Brick size = 100



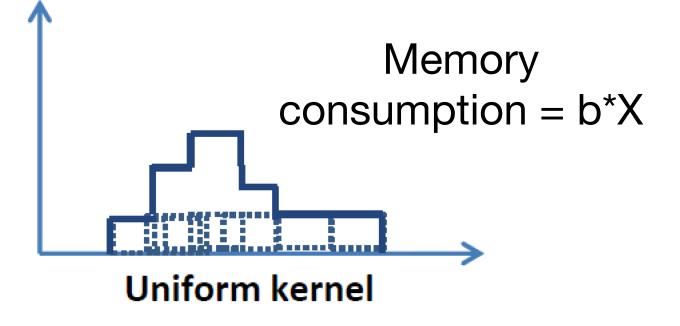
Parametric

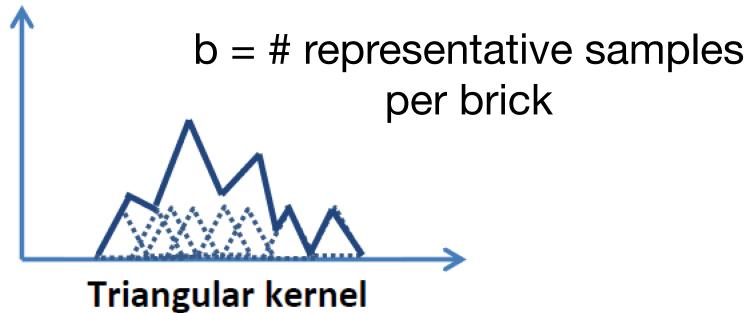










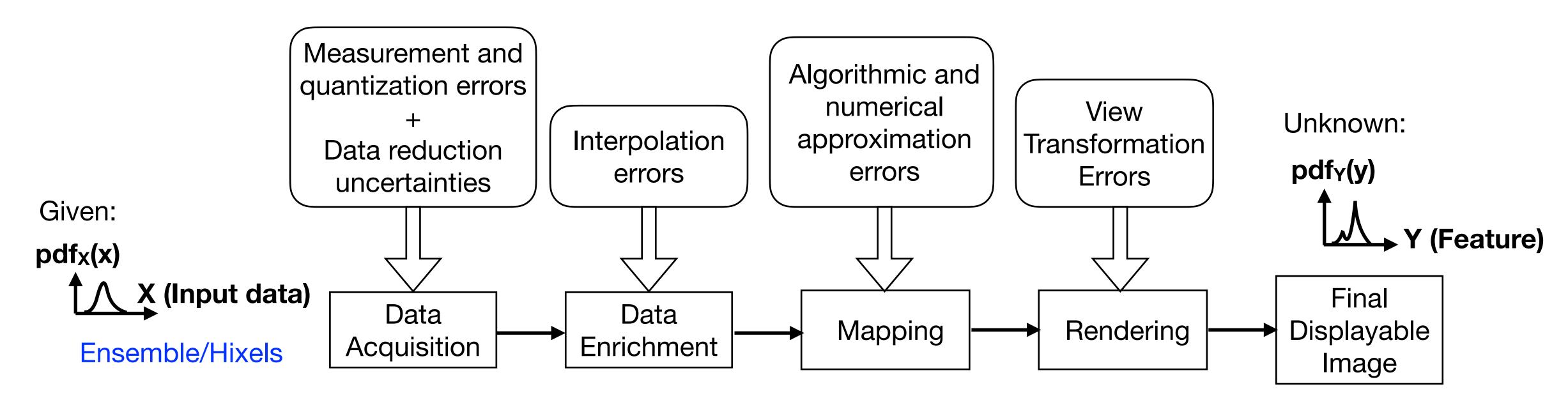




Uncertainty Quantification (Abstract Statistical Approach)

Monte Carlo (easy but expensive) vs. Analytical (difficult but fast)

Uncertainty Visualization of Level Sets

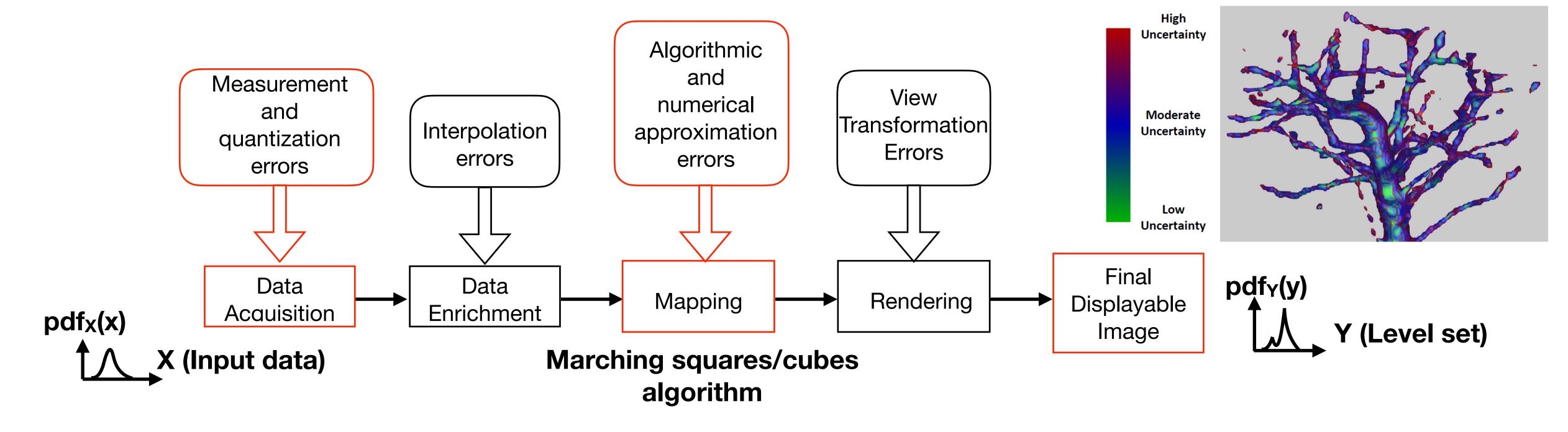


The Visualization Pipeline



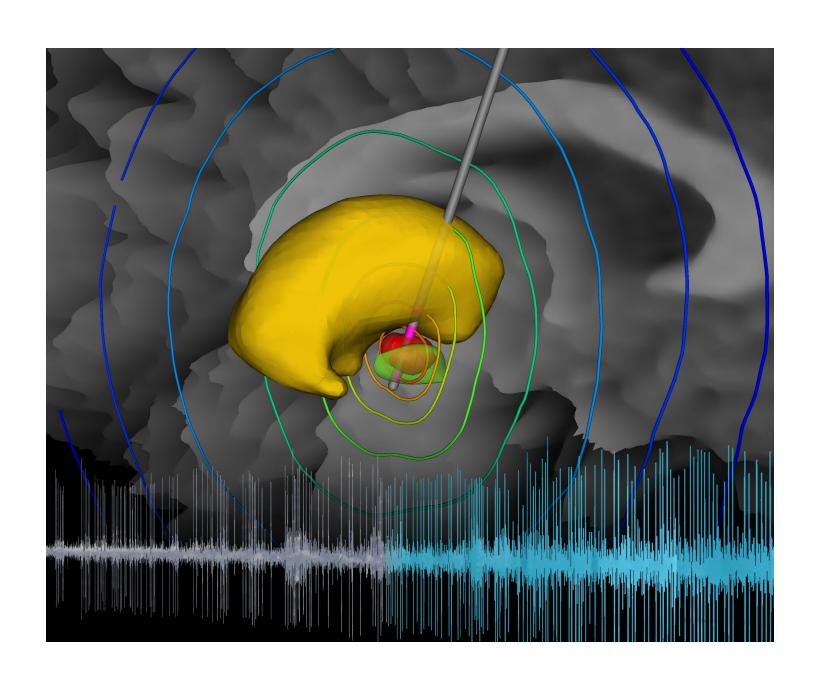
Level-Set Extraction in Uncertain Data

- Level sets and data uncertainty
- Marching squares/cubes algorithm in certain vs. uncertain data (our contribution!)
- Results

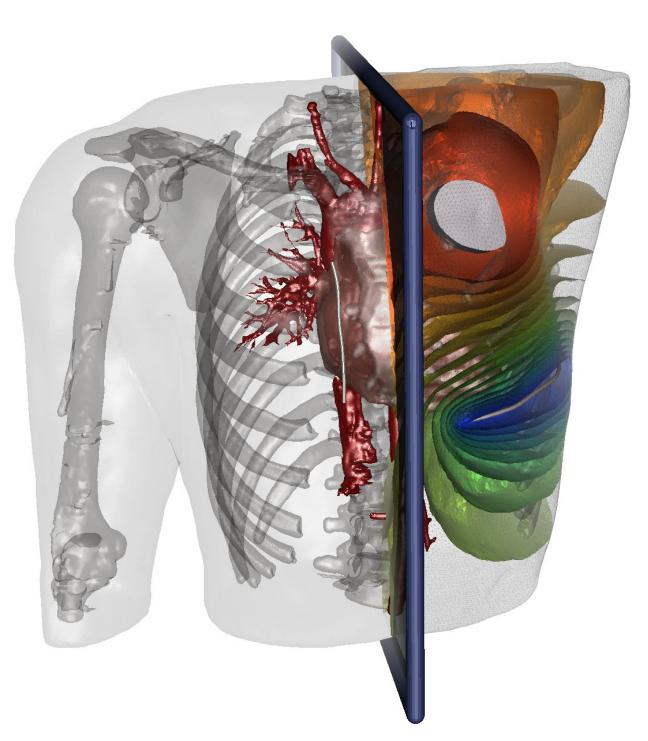




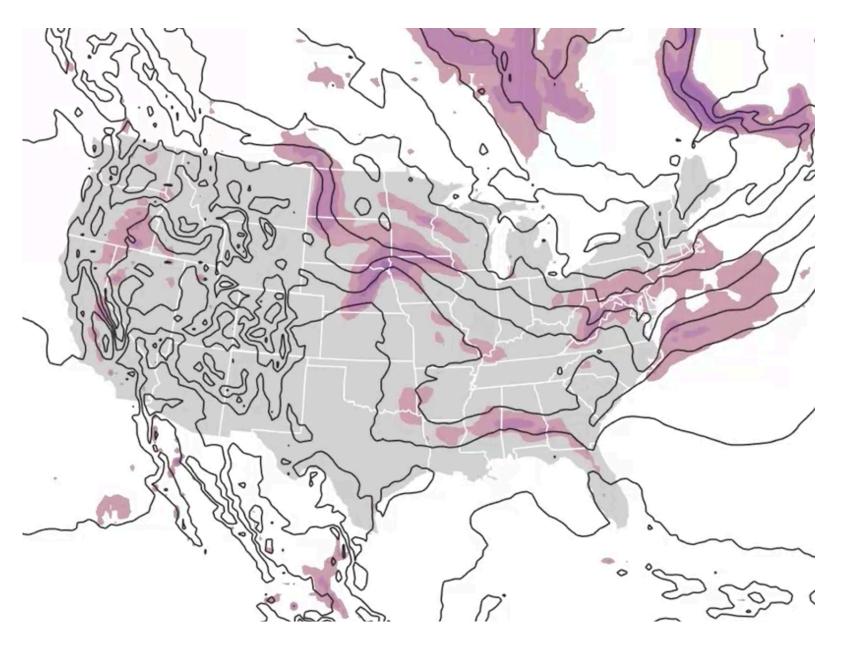
Level-Set Visualization



Deep Brain Stimulation (DBS)



Bioelectric-field Simulation



Temperature Field

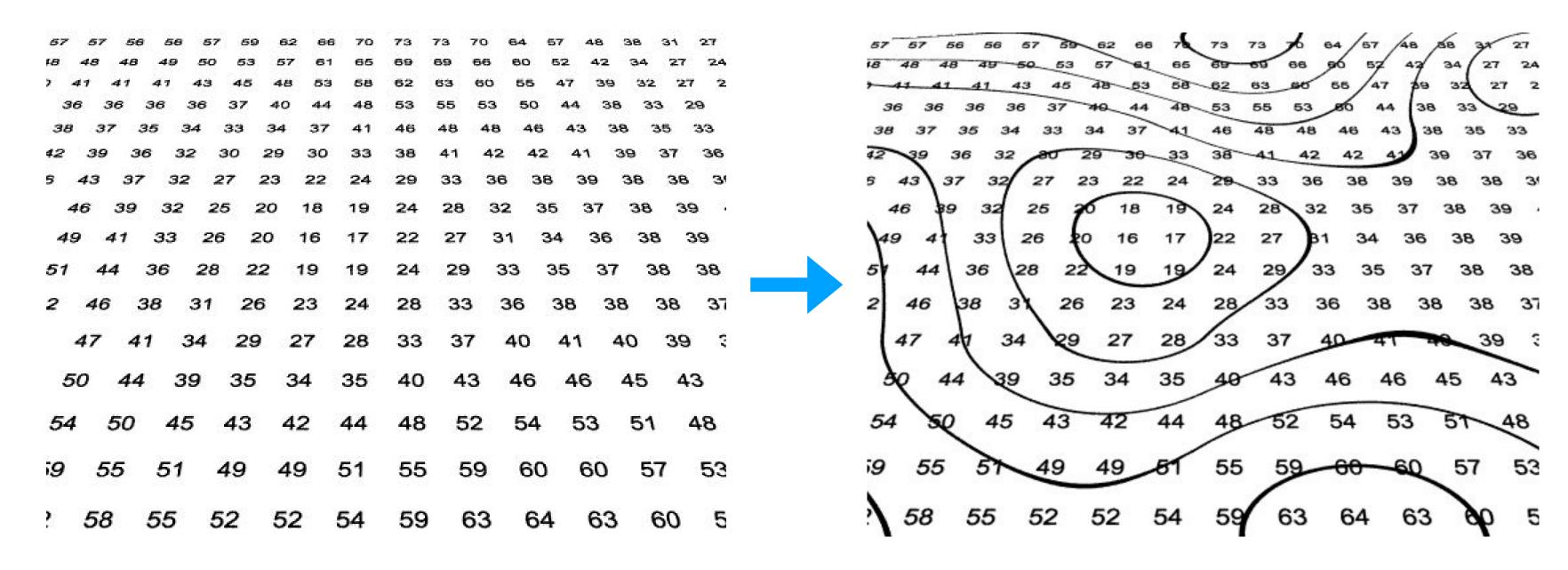


Level-Set Extraction

Uncertainty Visualization of Level Sets

The inverse problem: The level-set S corresponding to the isovalue k is given by:

$$S = \{x \in \mathbb{R}^n | f(x) = k\}$$
 , where $f: \mathbb{R}^n \to \mathbb{R}$



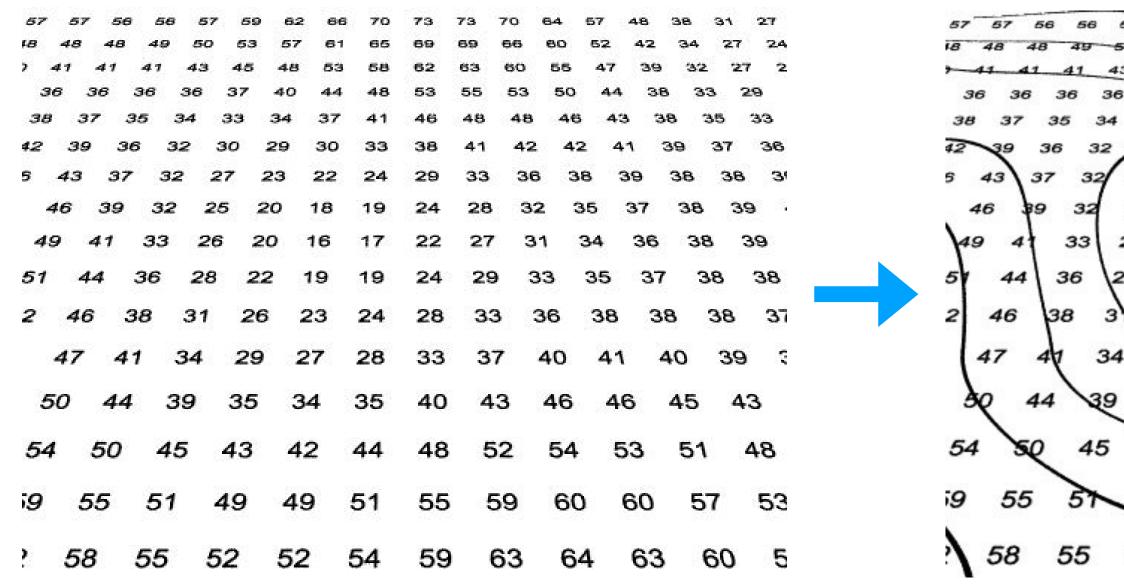






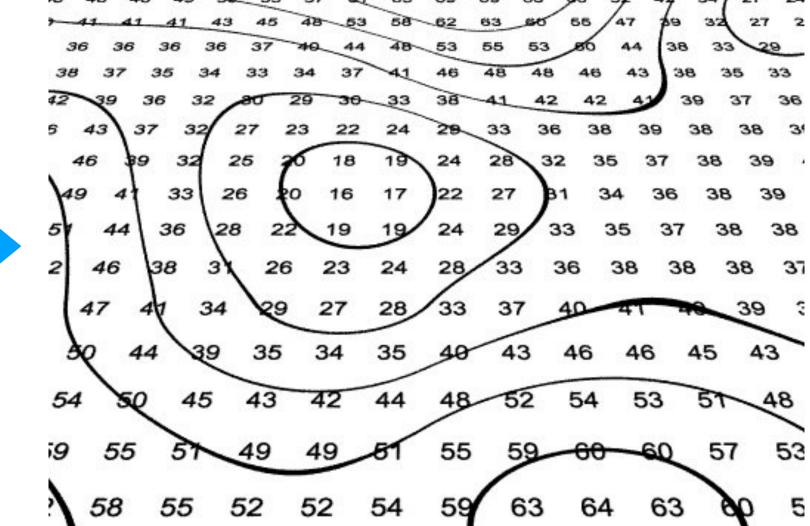
Level-Set Extraction in Uncertain Data

Research Question: Analysis of topological and geometric variations in level sets for uncertain scalar field



Uncertainty Visualization of Level Sets





Output: Level-Sets Visualization May not represent the true level sets!

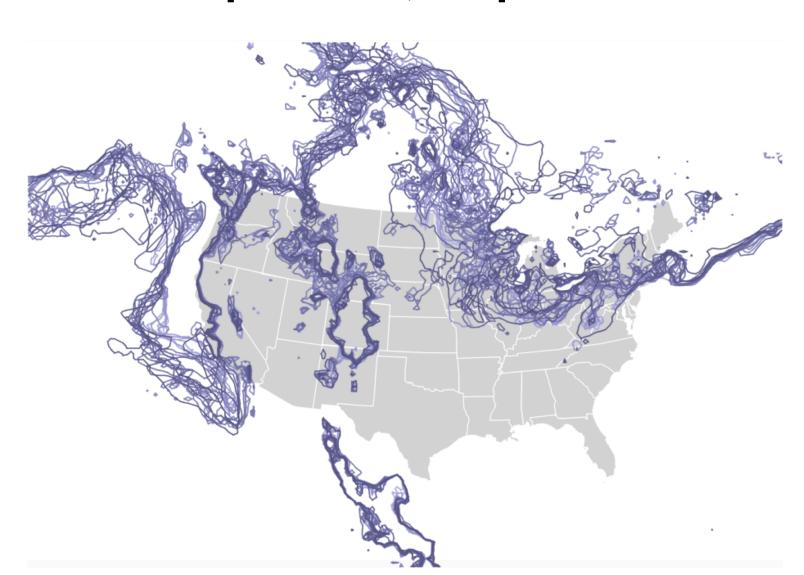


Visualization of Level-Sets in Uncertain Data

Spaghetti plots

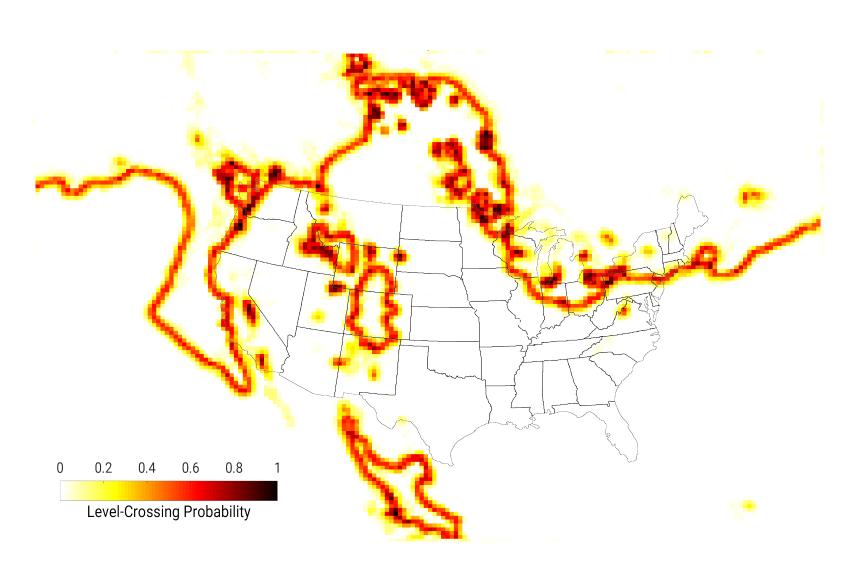
Uncertainty Visualization of Level Sets

[Potter et al., 2009]



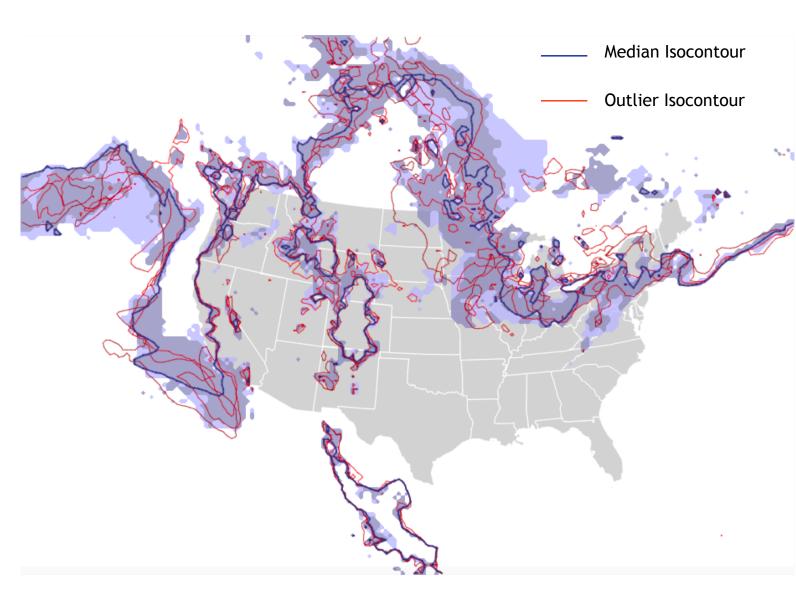
Visualization software: The WeaVER [Quinan and Meyer, 2016]

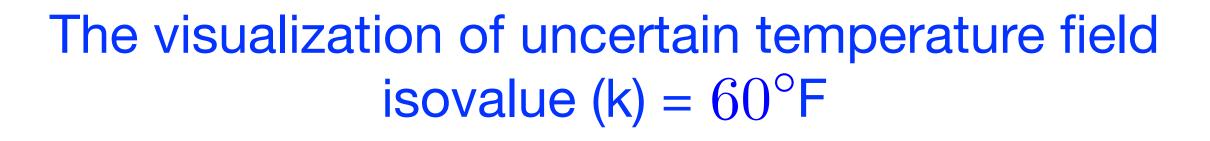
Probabilistic marching cubes [Pöthkow et al., 2011]



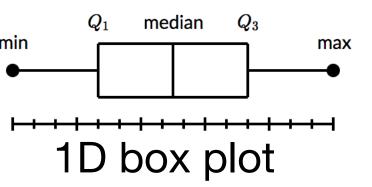
Contour/Surface box plots

[Whitaker et al., 2013; Genton et al., 2014]









Marching Squares/Cubes Algorithm for Level-Set Extraction

[Lorenson and Cline, 1987]

Google Scholar



Bill Lorensen

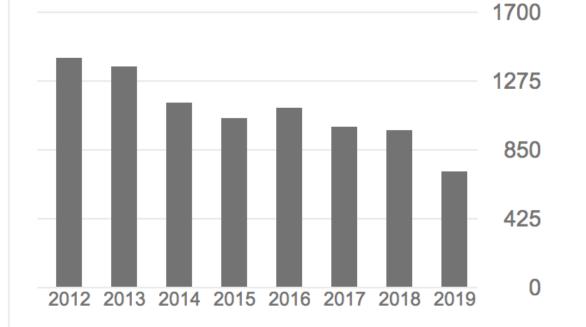
Uncertainty Visualization of Level Sets

GE Global Research (retired) Verified email at nycap.rr.com - Homepage



TITLE	CITED BY	YEAR
Marching cubes: A high resolution 3D surface construction algorithm WE Lorensen, HE Cline ACM siggraph computer graphics 21 (4), 163-169	15483	1987
Object-oriented modeling and design J Rumbaugh, M Blaha, W Premerlani, F Eddy, WE Lorensen Prentice-hall 199 (1)	11730	1991
The visualization toolkit: an object-oriented approach to 3D graphics WJ Schroeder, B Lorensen, K Martin Kitware	3994	2004

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Citations	36273	5984
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i10-index	24	14



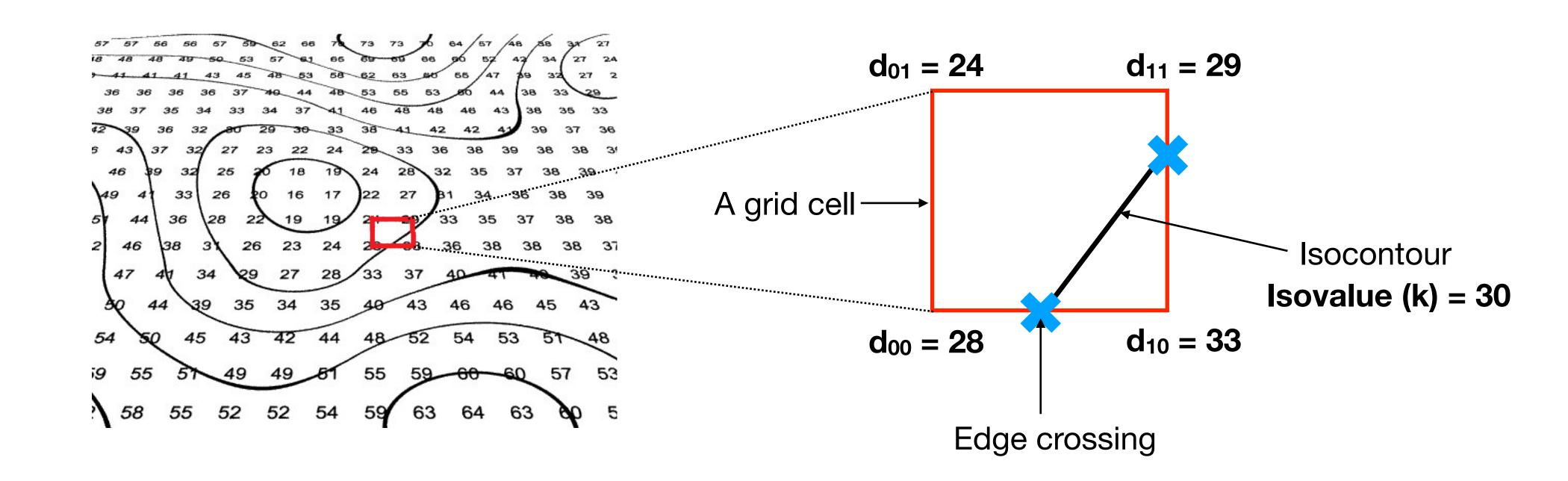


Marching Squares Algorithm (MSA)

- Bilinear interpolation: prediction of unknown data values within a grid cell
- For each cell:
 - Extract isocontour topology (Which cell edges are crossed?)

Uncertainty Visualization of Level Sets

Compute geometry (Where on the cell edge?)



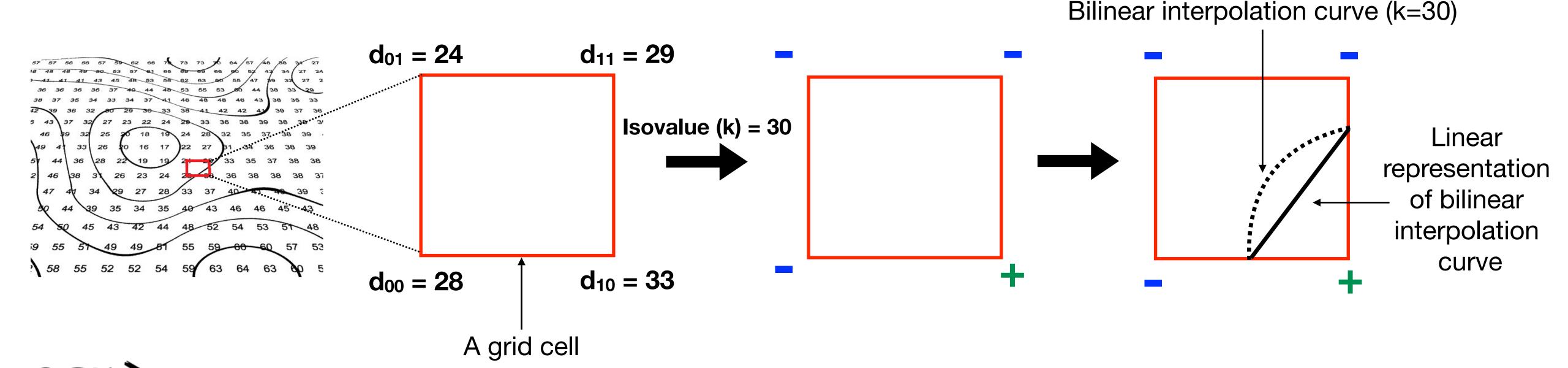


MSA: The Topology Step (which edges?)

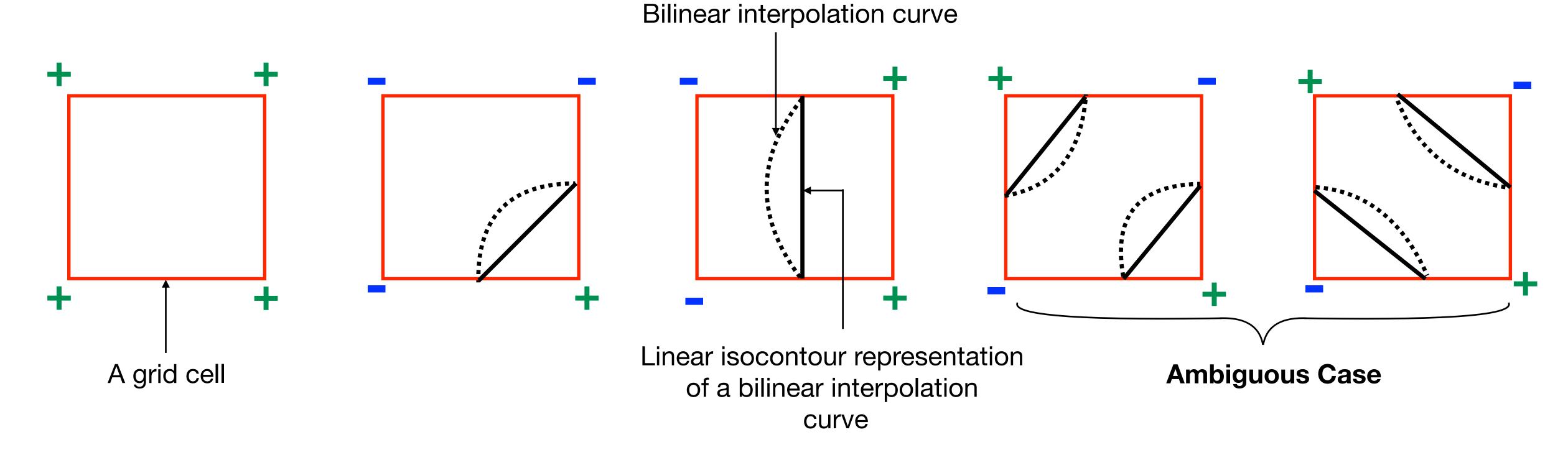
Data $(d_{xy}) > Isovalue(k)$: Positive vertex (+) Data (d_{xy}) < Isovalue (k) : Negative vertex (-)

Bilinear interpolation function:

```
f: [0,1]x[0,1] \to R
f(x,y) = ax + by + cxy + d (the equation of hyperbola!), where
a = d_{10} - d_{00}, b = d_{01} - d_{00}
c = d_{00} + d_{11} - d_{01} - d_{10}, d = d_{00}
```

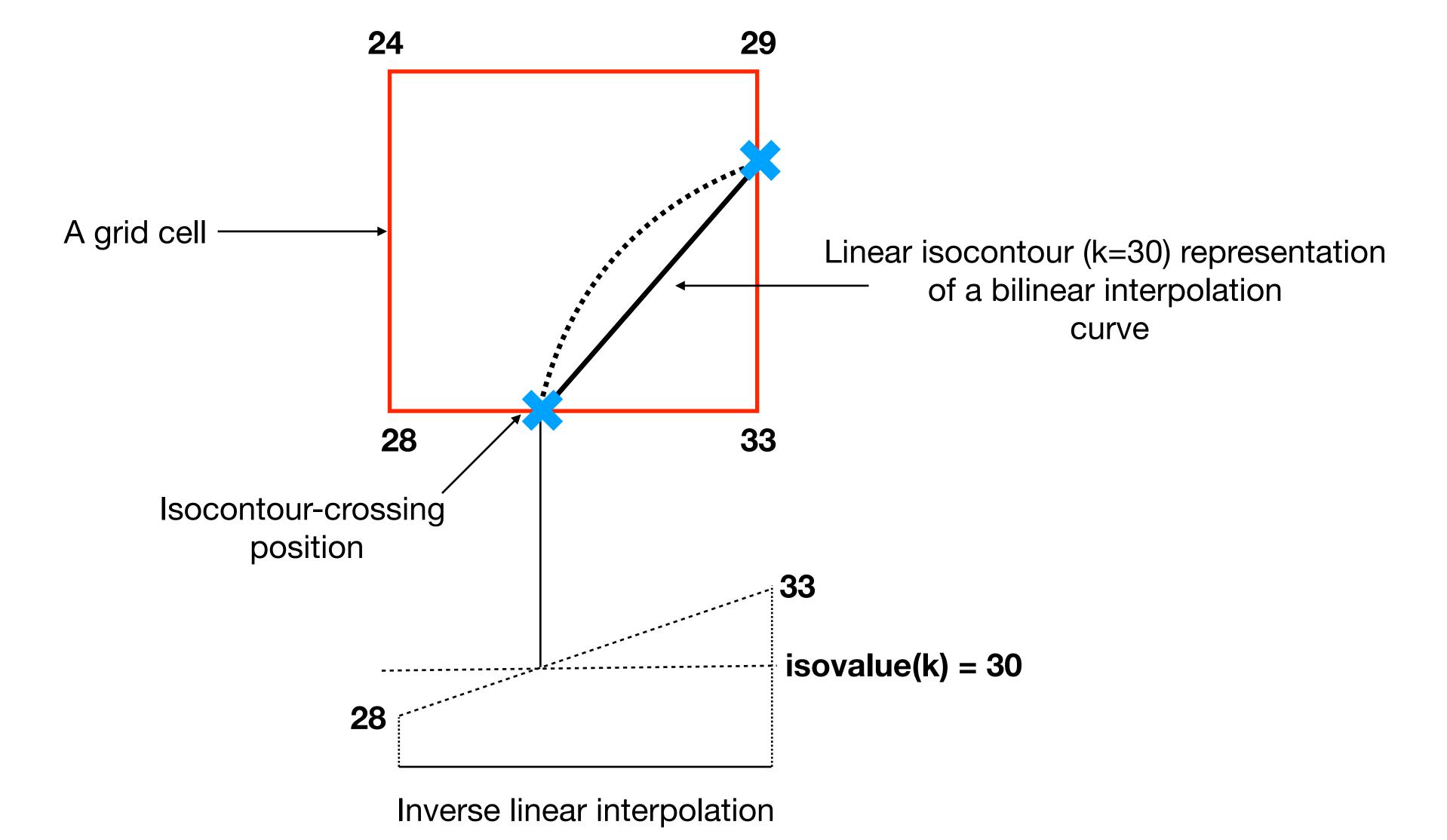


MSA: Topological Cases (which edges?)



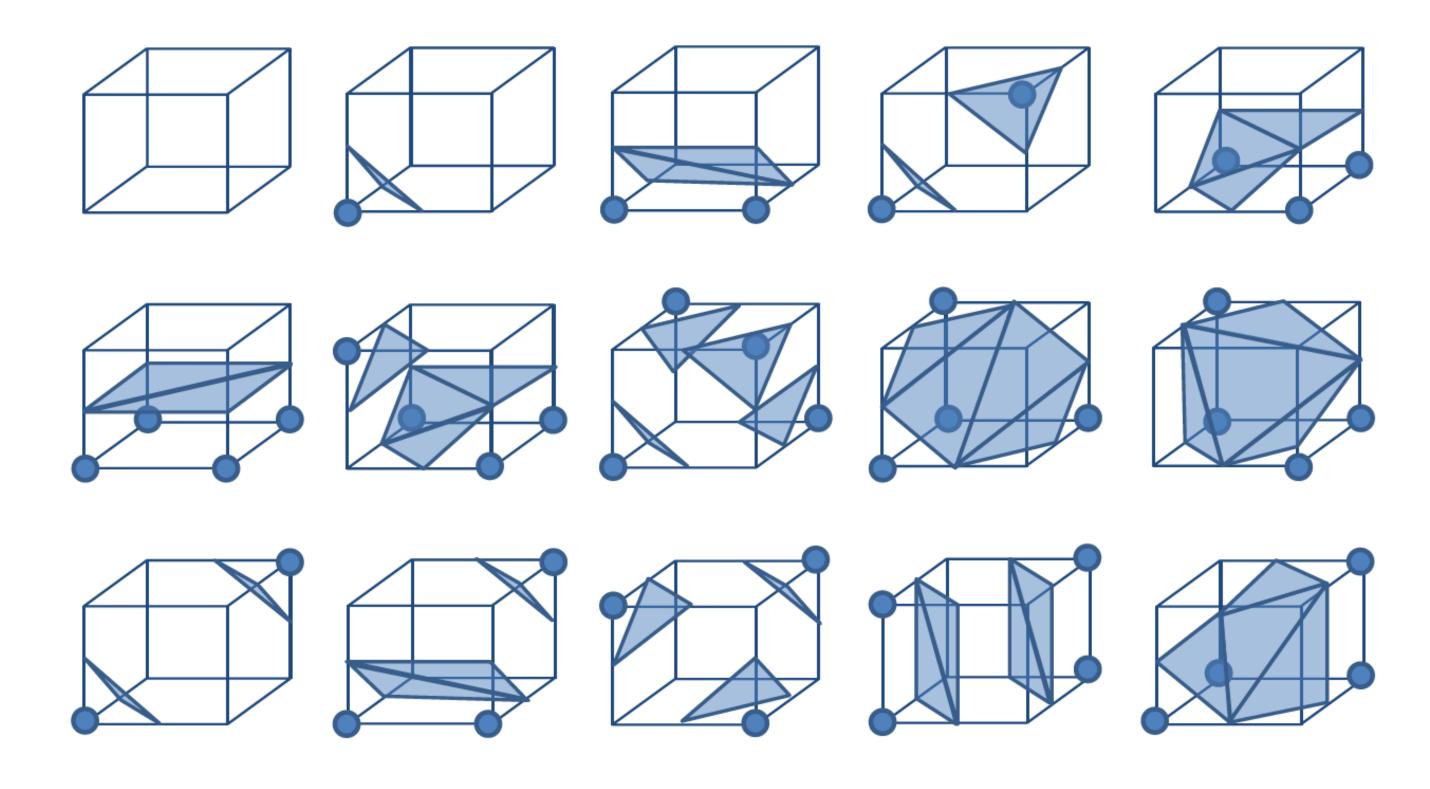


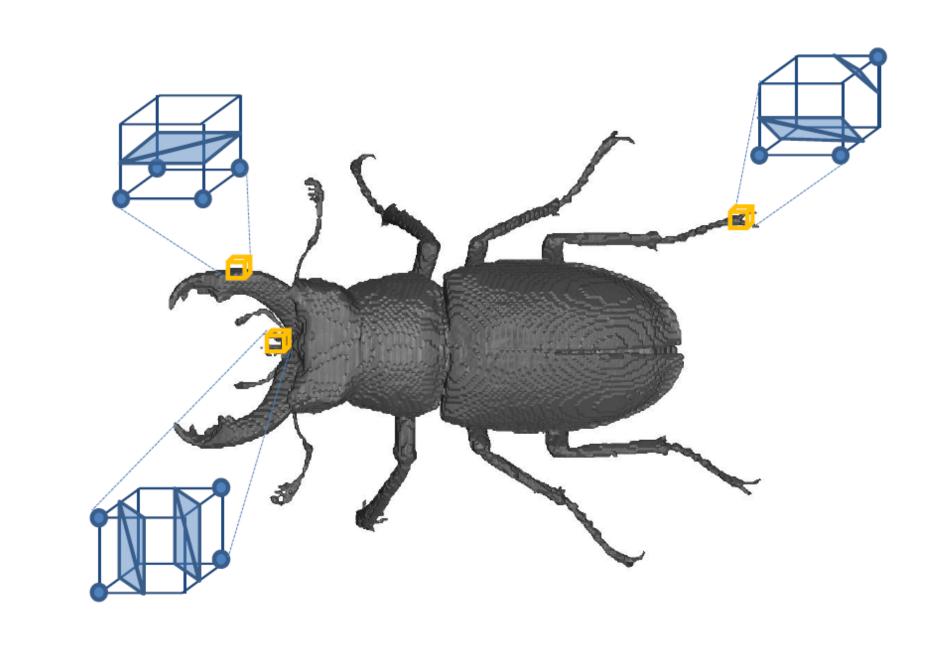
MSA: The Geometry Step (where on the edge?)





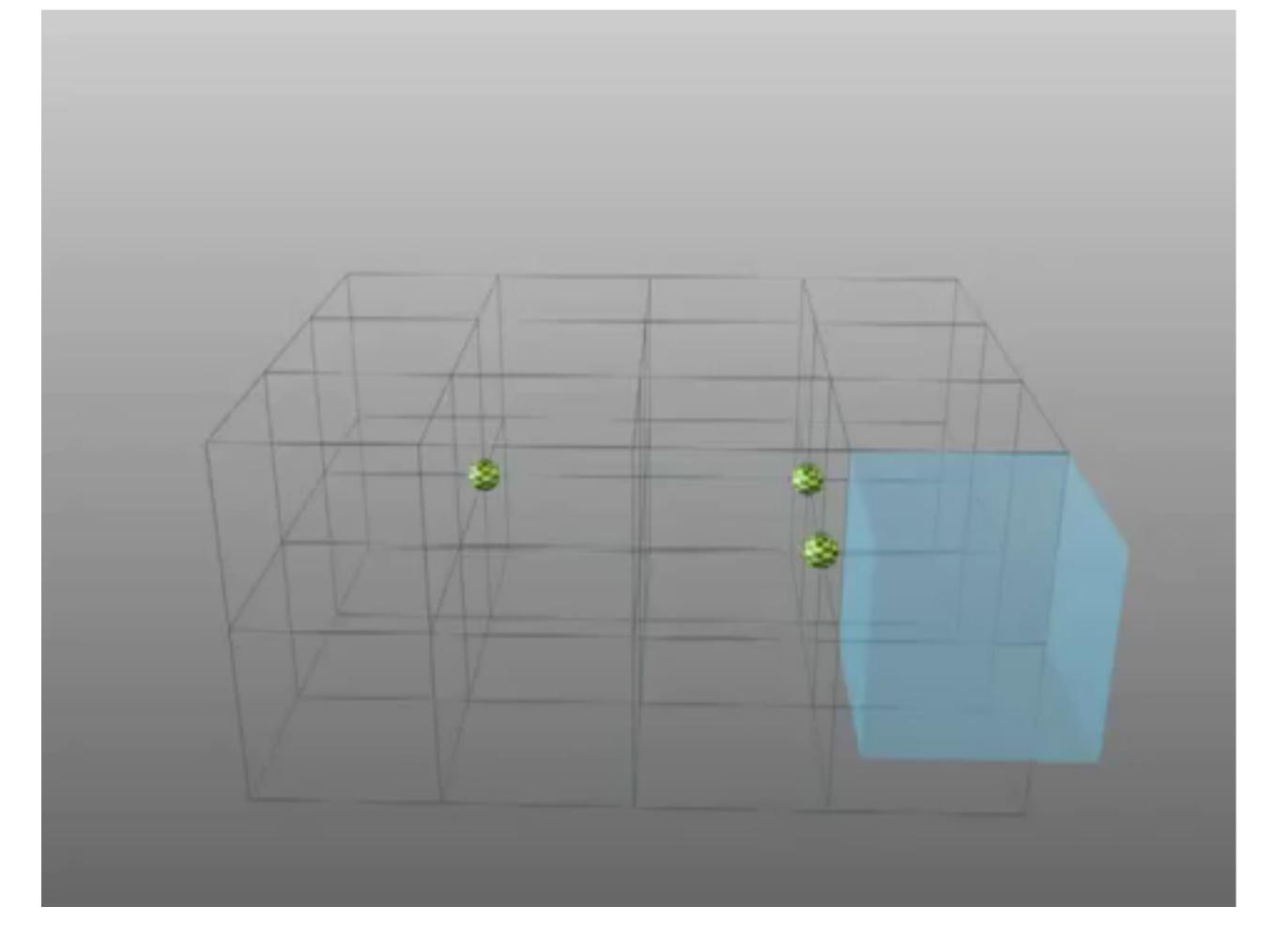
Marching Cubes Algorithm (MCA): Topological Cases







Marching Cubes Algorithm in Action!





Marching Squares/Cubes Algorithm for Level-Set Extraction in Uncertain Data

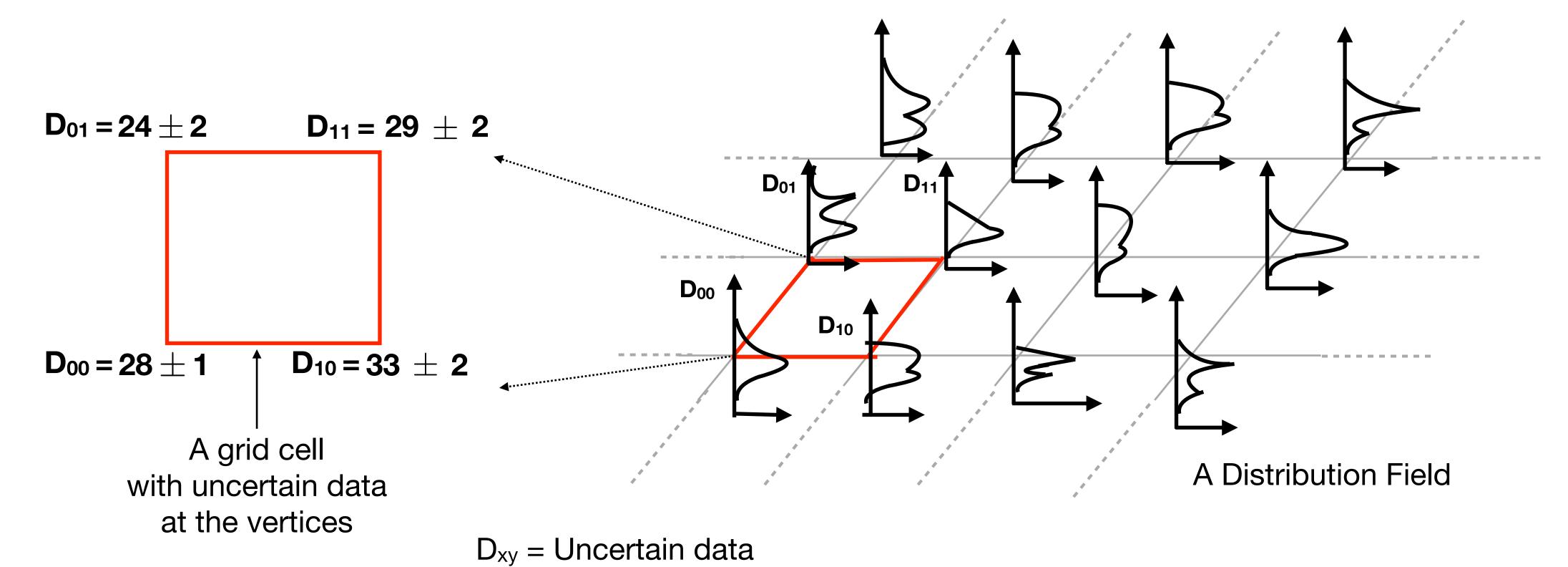


MSA for Uncertain Data (our contribution!)

Topological (which edges) uncertainty resolution

Uncertainty Visualization of Level Sets

Geometric (where on the edges) uncertainty resolution

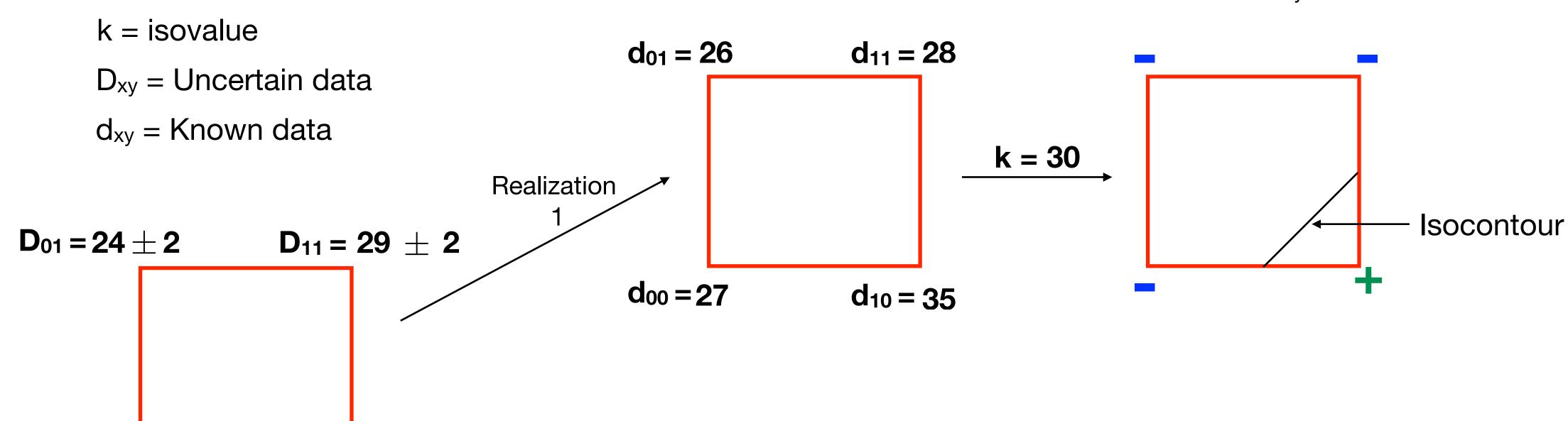




MSA: Topological Uncertainty

Uncertainty Visualization of Level Sets

if data d_{xy} > kif data d_{xy} < k



A grid cell with uncertain input data

 $D_{00} = 28 \pm 1$

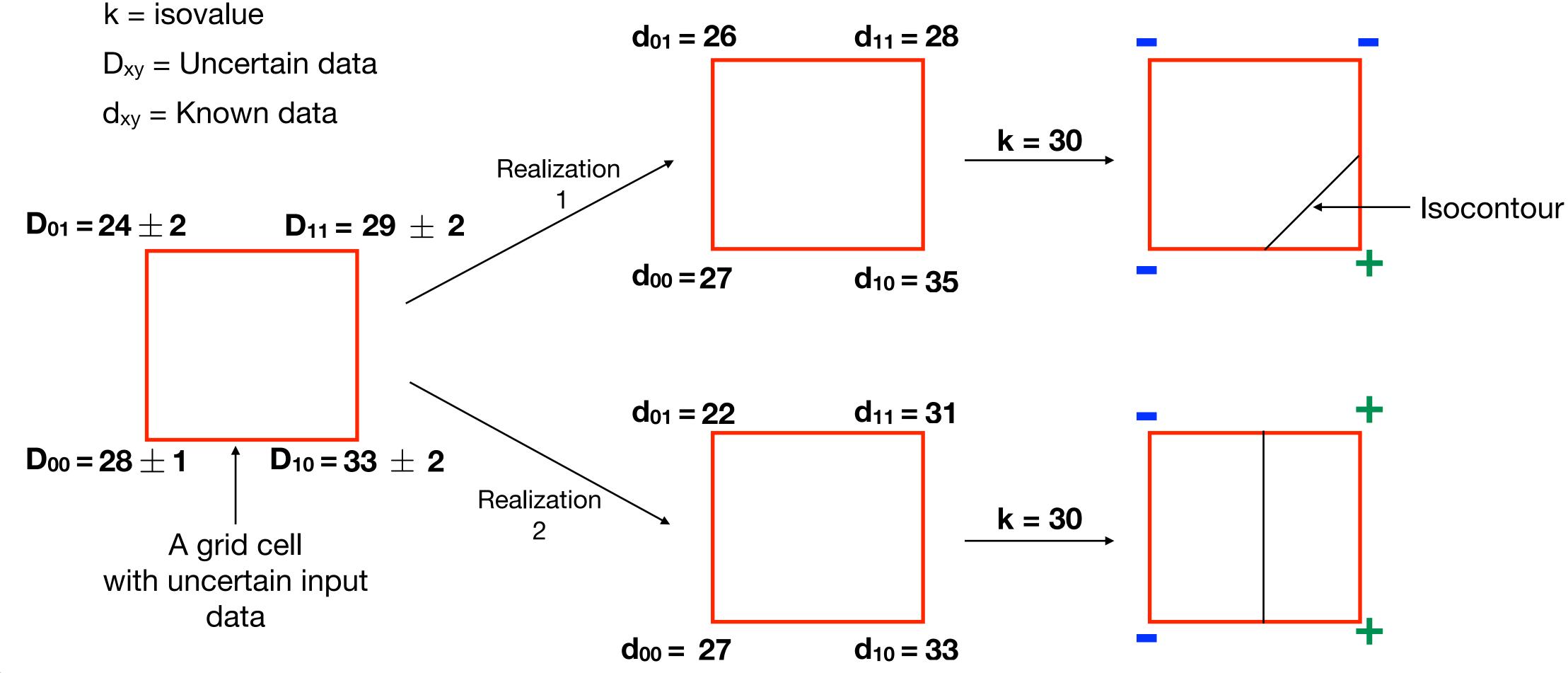
 $D_{10} = 33 \pm 2$



MSA: Topological Uncertainty

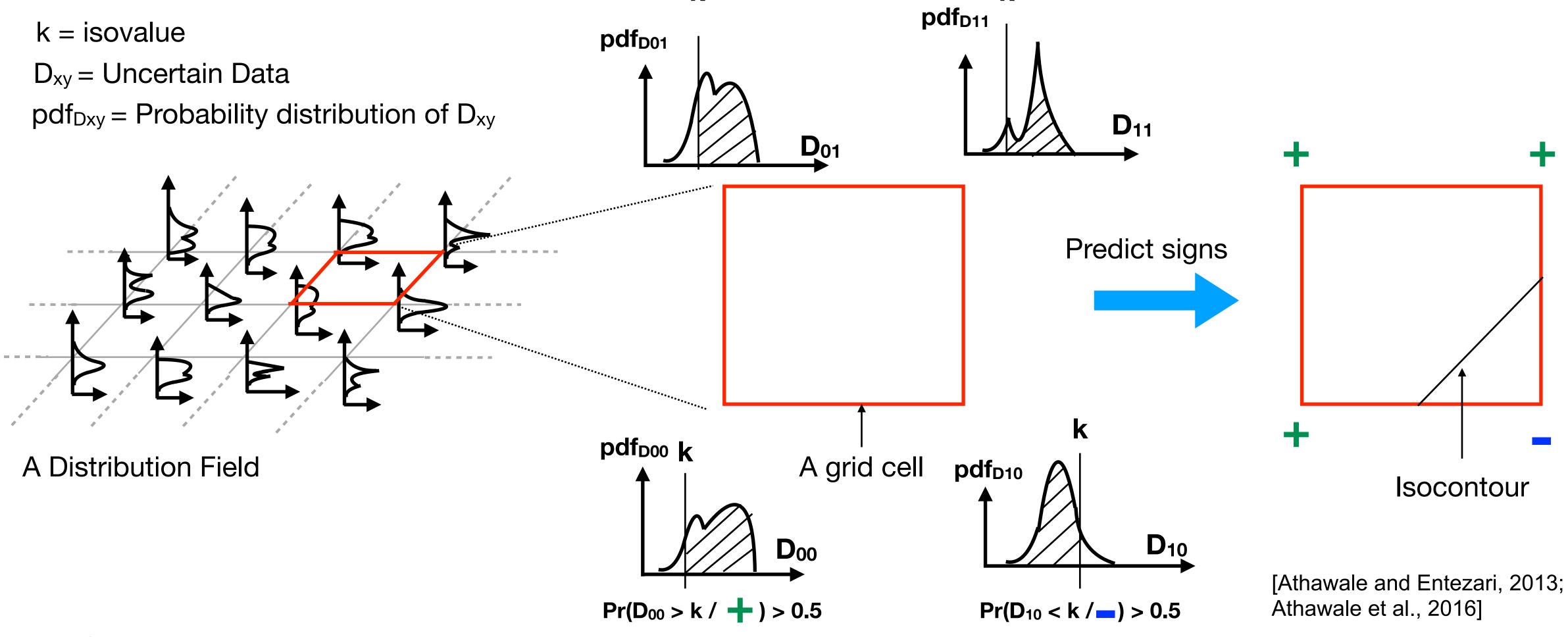
Uncertainty Visualization of Level Sets

+: if data $d_{xy} > k$ -: if data $d_{xy} < k$



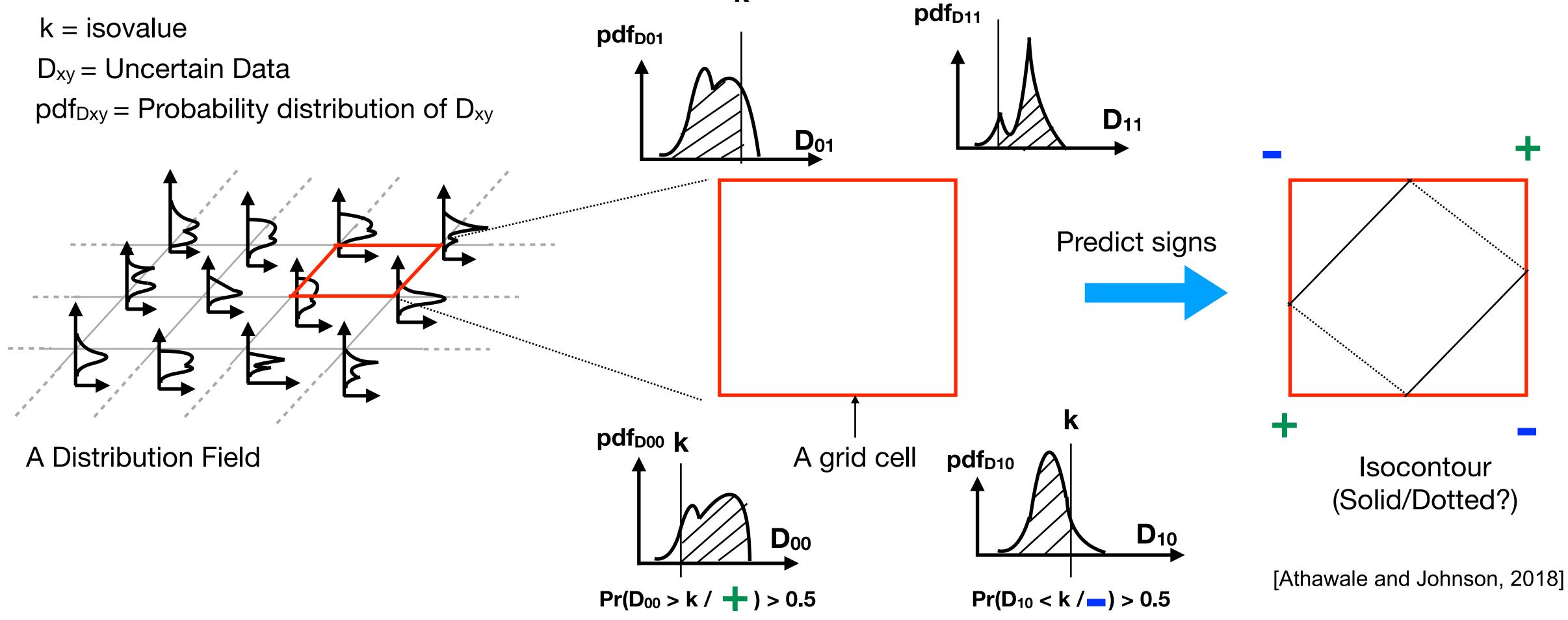


MSA: Topological Uncertainty Resolution



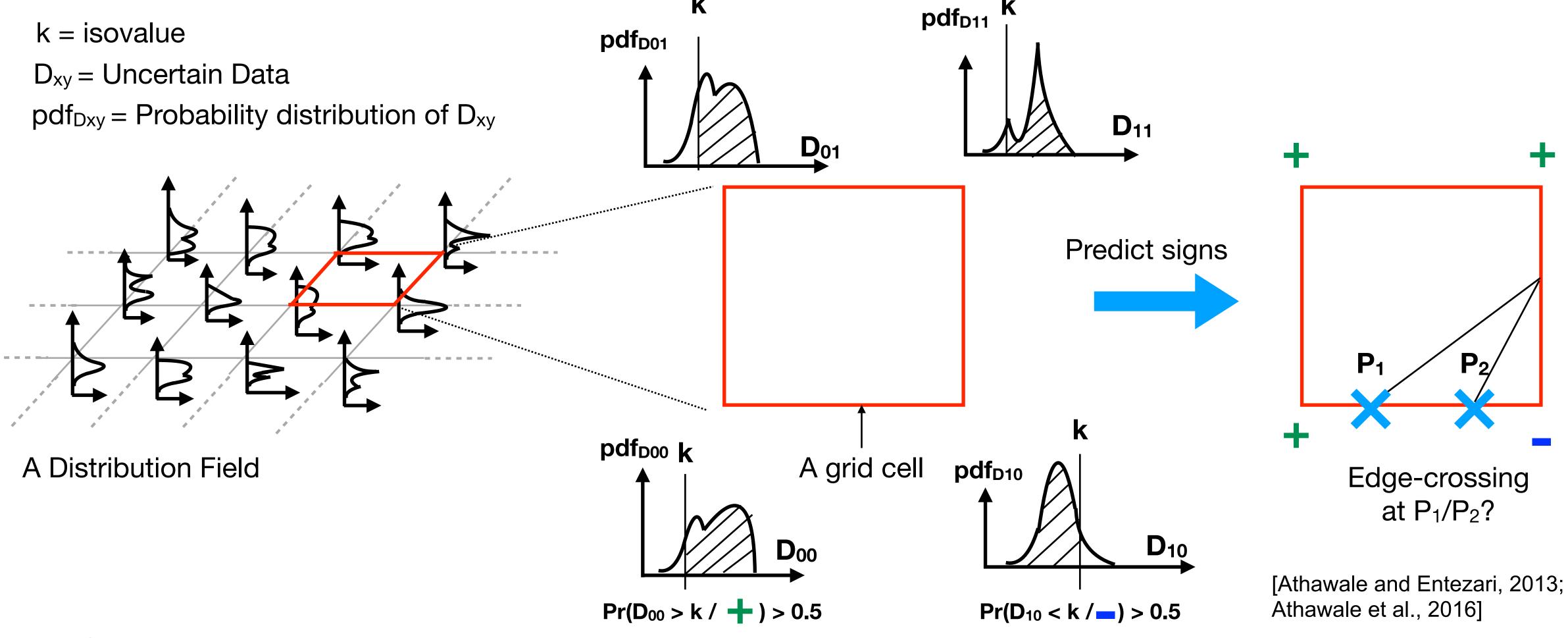


MSA Ambiguous Case: Topological Uncertainty Resolution





MSA: Geometric Uncertainty



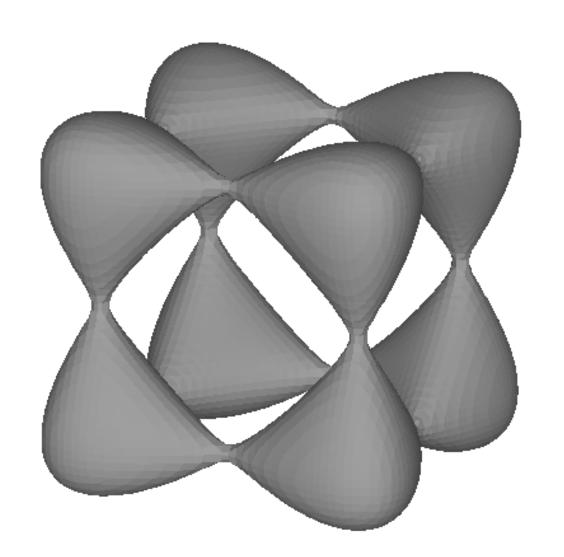


Results: Visualization of Uncertain Level Sets

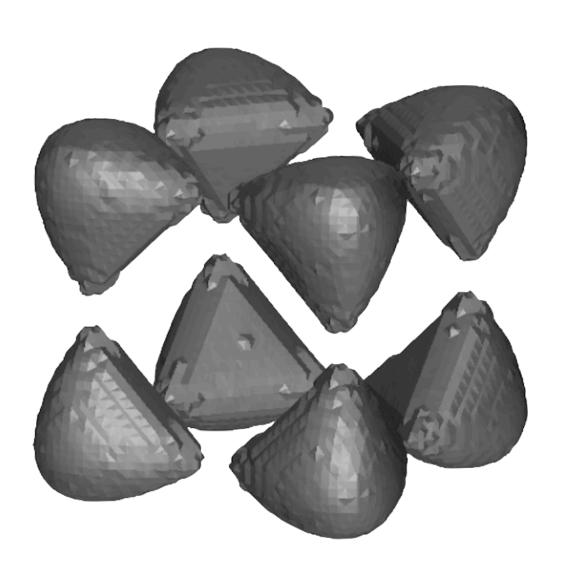


Isosurface Extraction in Uncertain Data

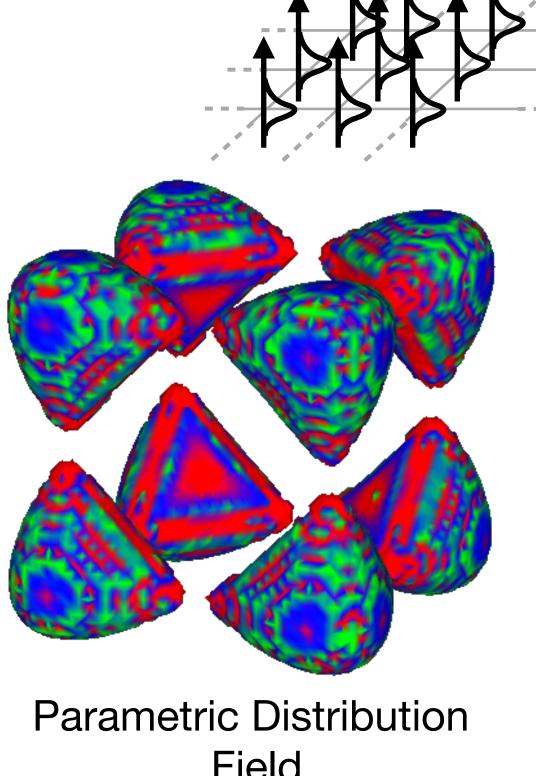
Tangle function (synthetic data)



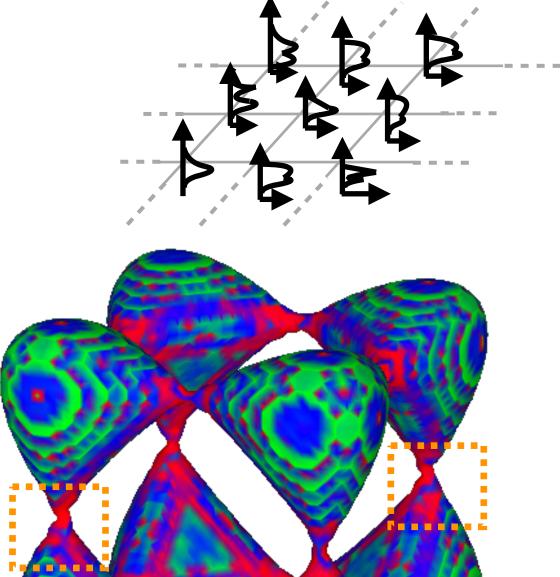
Ground truth



Mean Field



Field



Nonparametric Distribution Field

[Athawale and Entezari, 2013; Athawale et al., 2016]

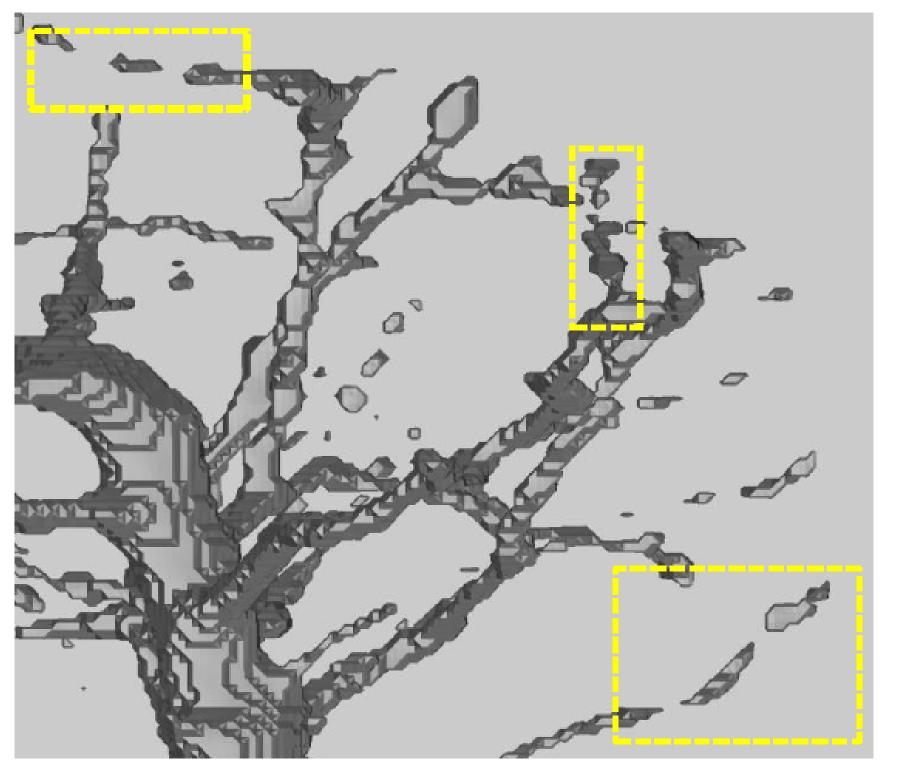
(Visualization software: The Geomview, Developer: The Geometry Center at the University of Minnesota)

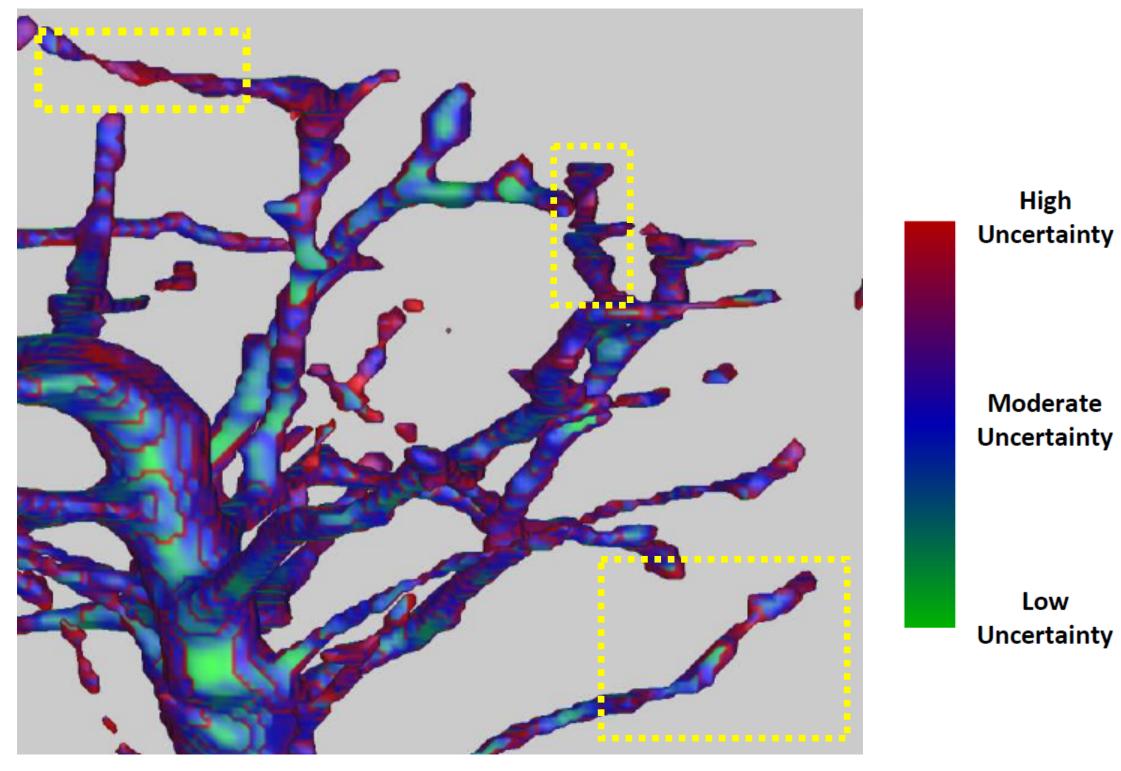




Isosurface Extraction in Uncertain Data

Bonsai tree (real data)







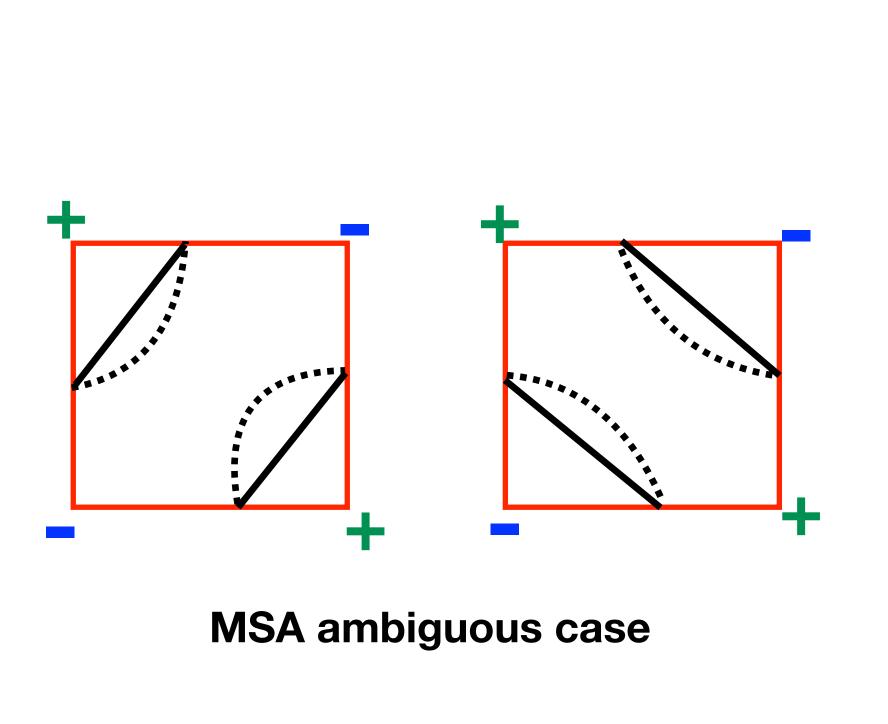
Nonparametric



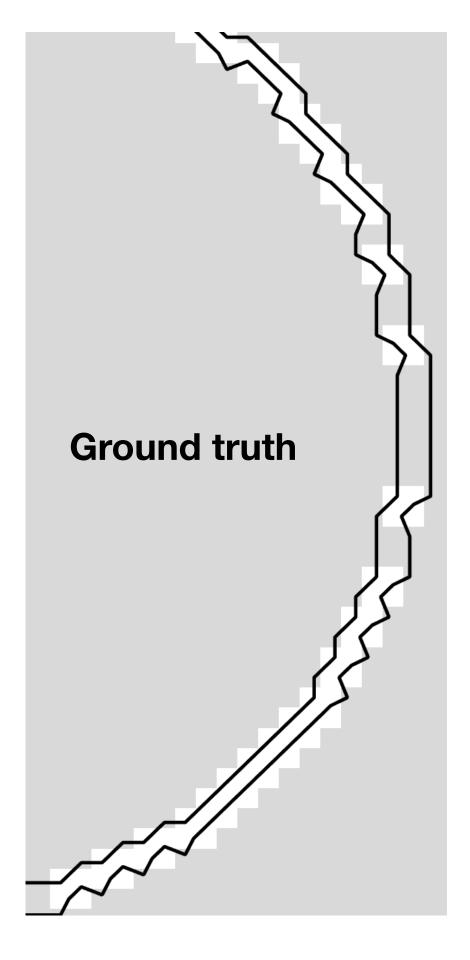
Introduction

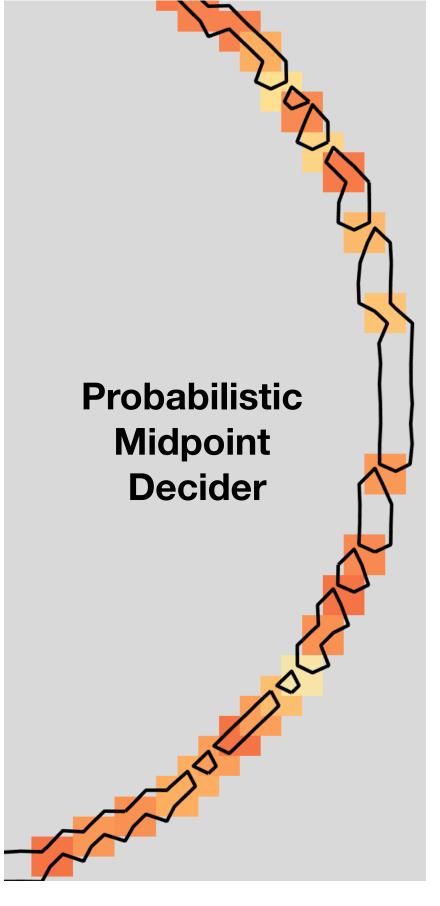
MSA Ambiguous Case Resolution in Uncertain Data

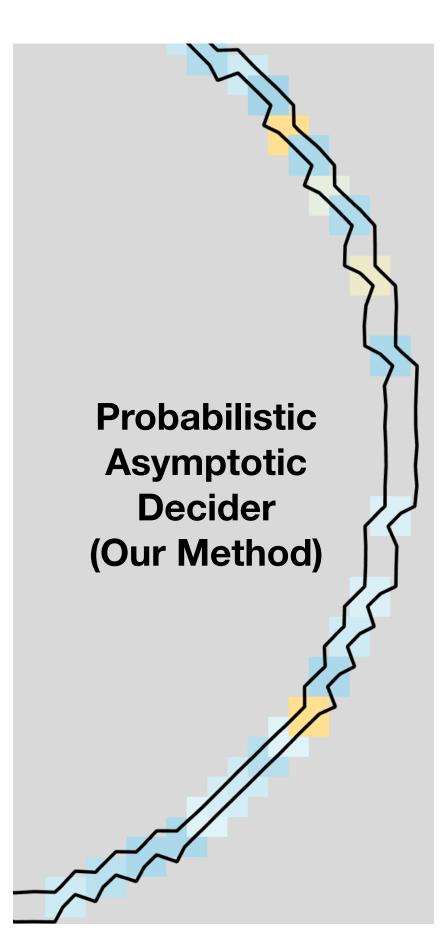
Concentric circles (synthetic data)

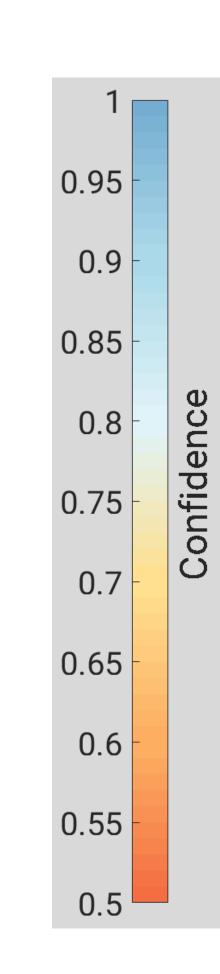


[Athawale and Johnson, 2018]





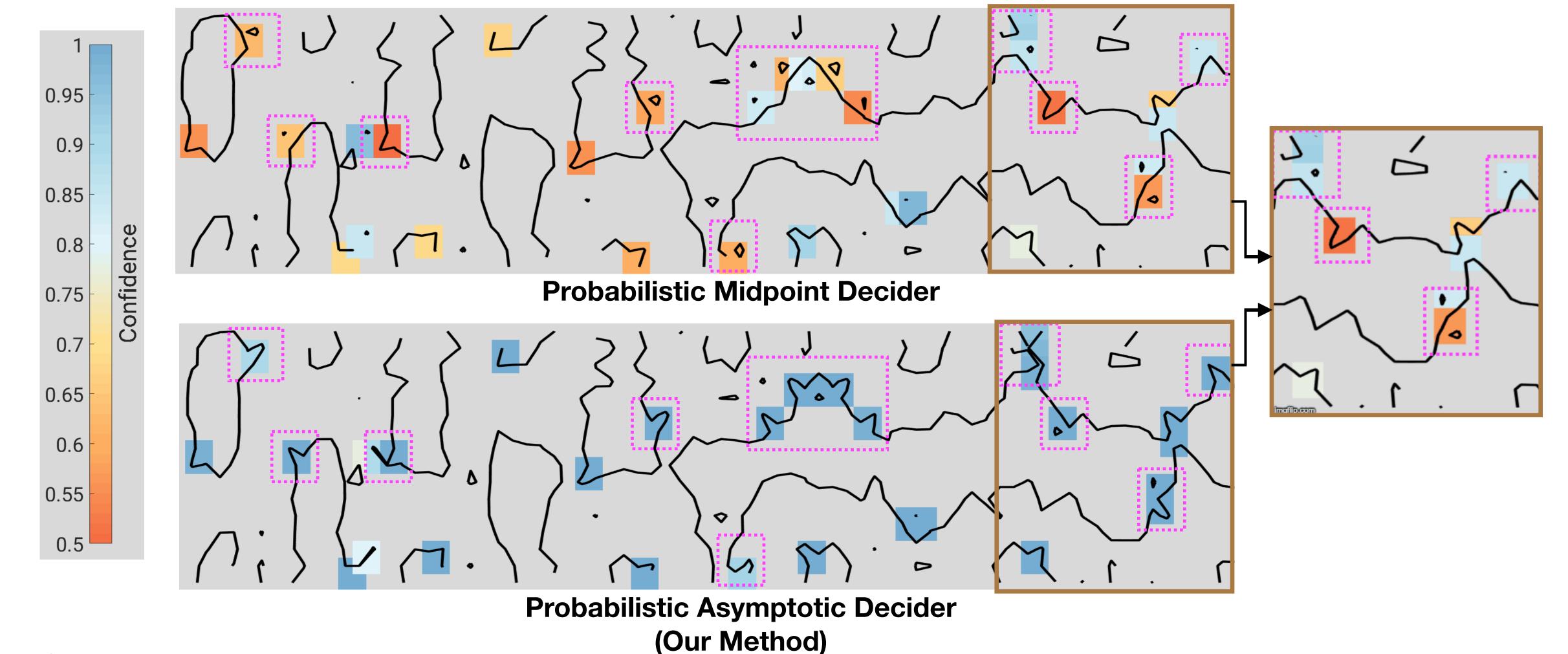






Isocontour Visualizations (Karman Vortex Street)

Uncertainty Visualization of Level Sets

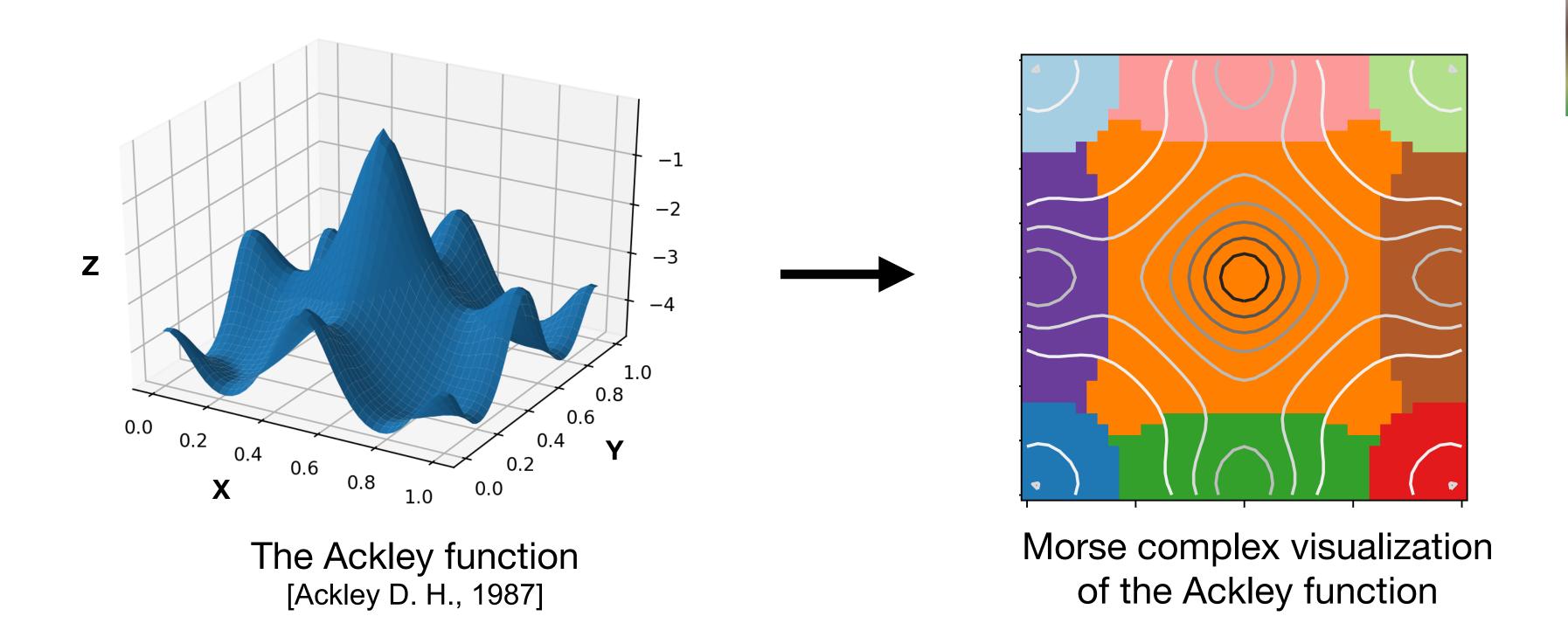




The flow simulation dataset is courtesy of the Gerris project [Popinet, 2003]

Morse Complex Visualizations

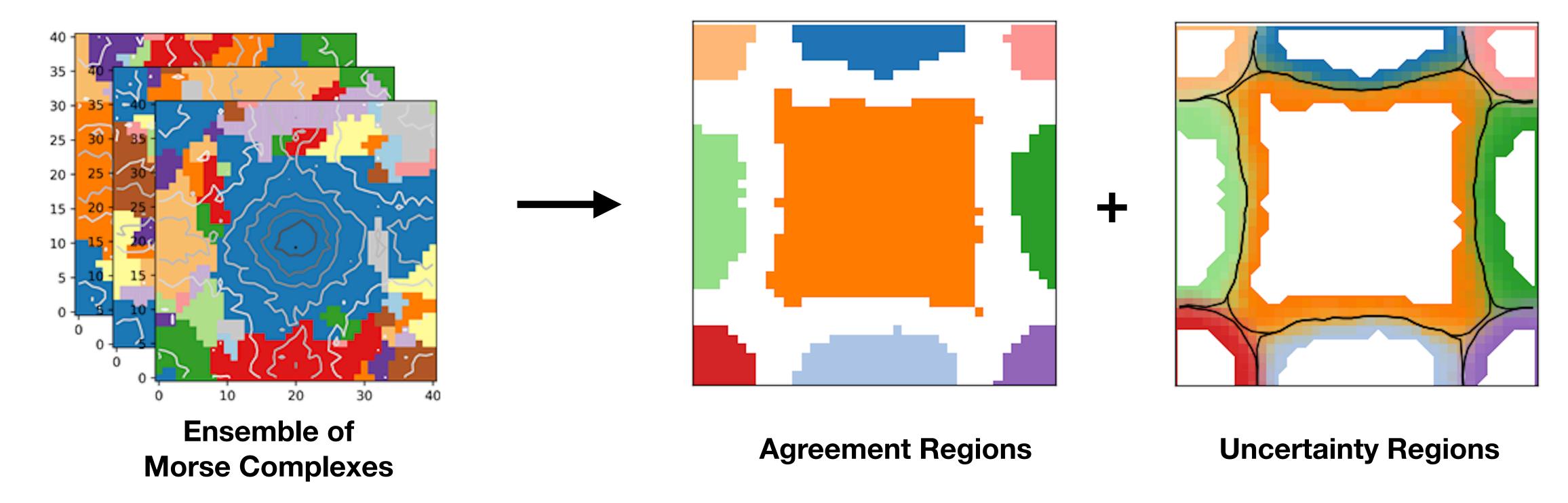
Topological descriptors, which provide an abstract representation of gradient flows of a scalar field





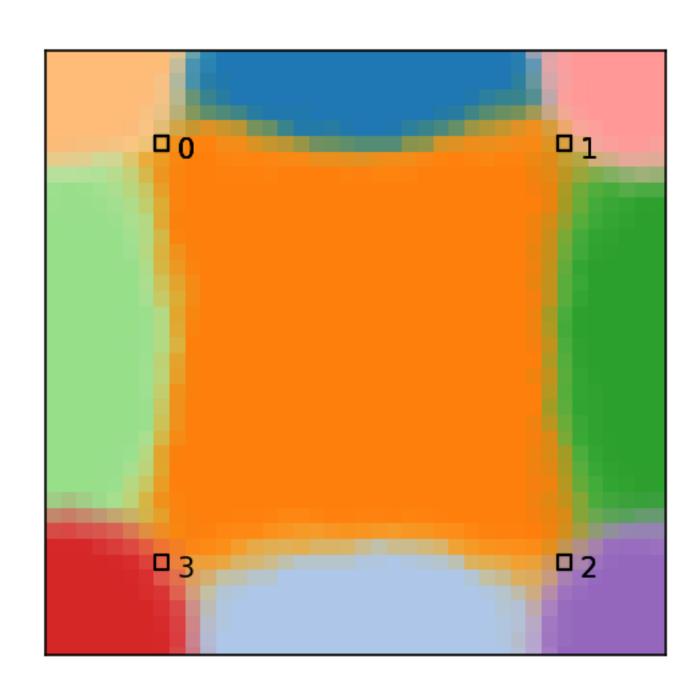
Uncertainty Visualization of Morse Complexes

Visualize agreement/certainty and disagreement/uncertainty among abstract Morse complexes for ensembles

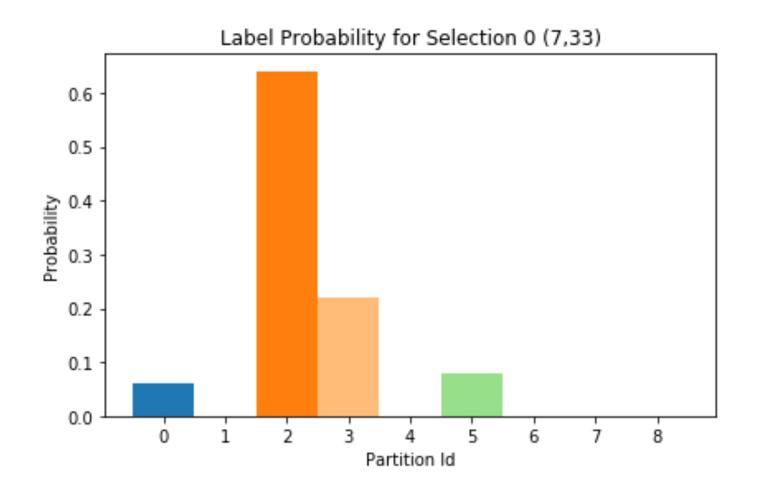


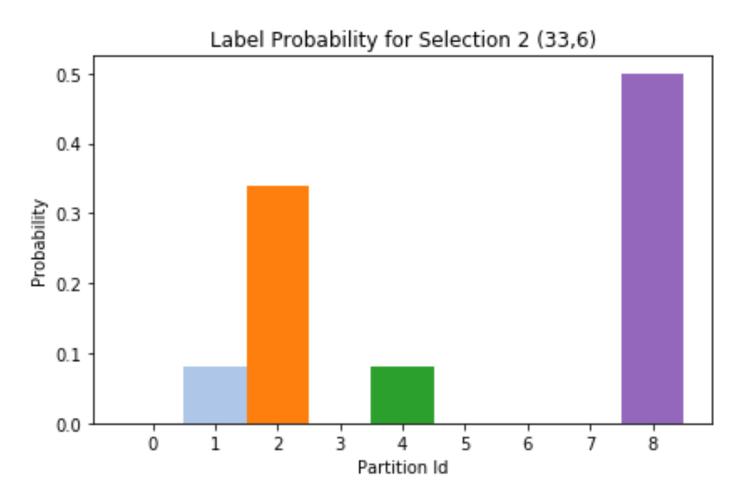


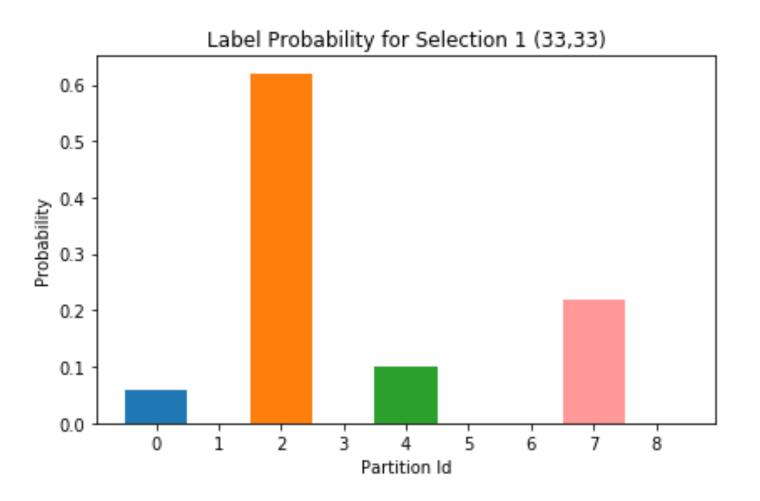
Interactive PDF Queries for Uncertain Regions

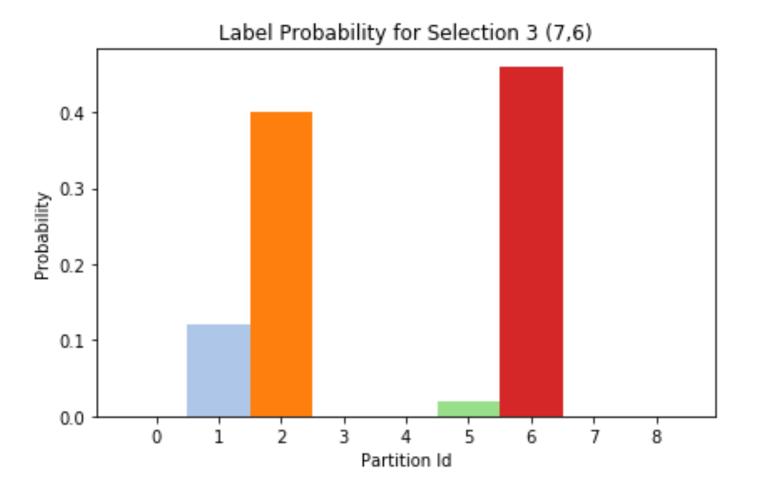


[K. Potter, R. M. Kirby, D. Xiu, and C. R. Johnson; Interactive Visualization of Probability and Cumulative Density Functions; 2011]



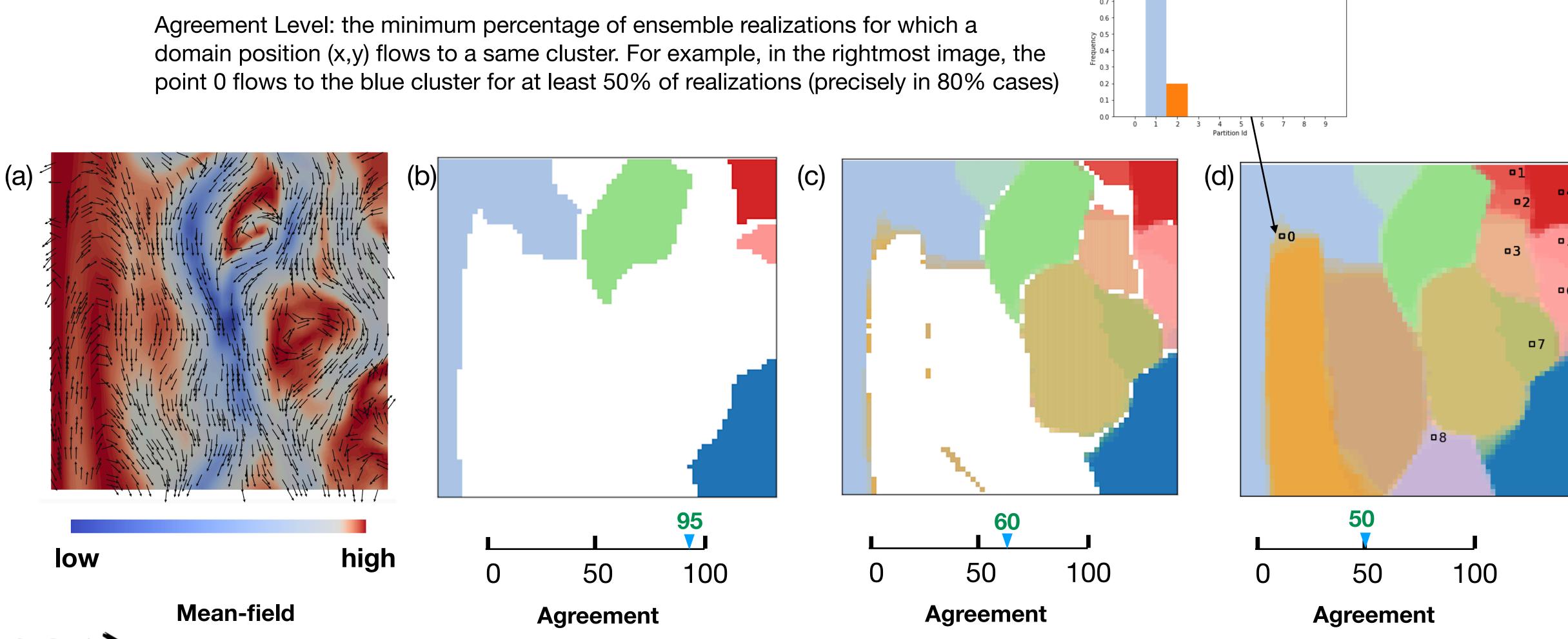








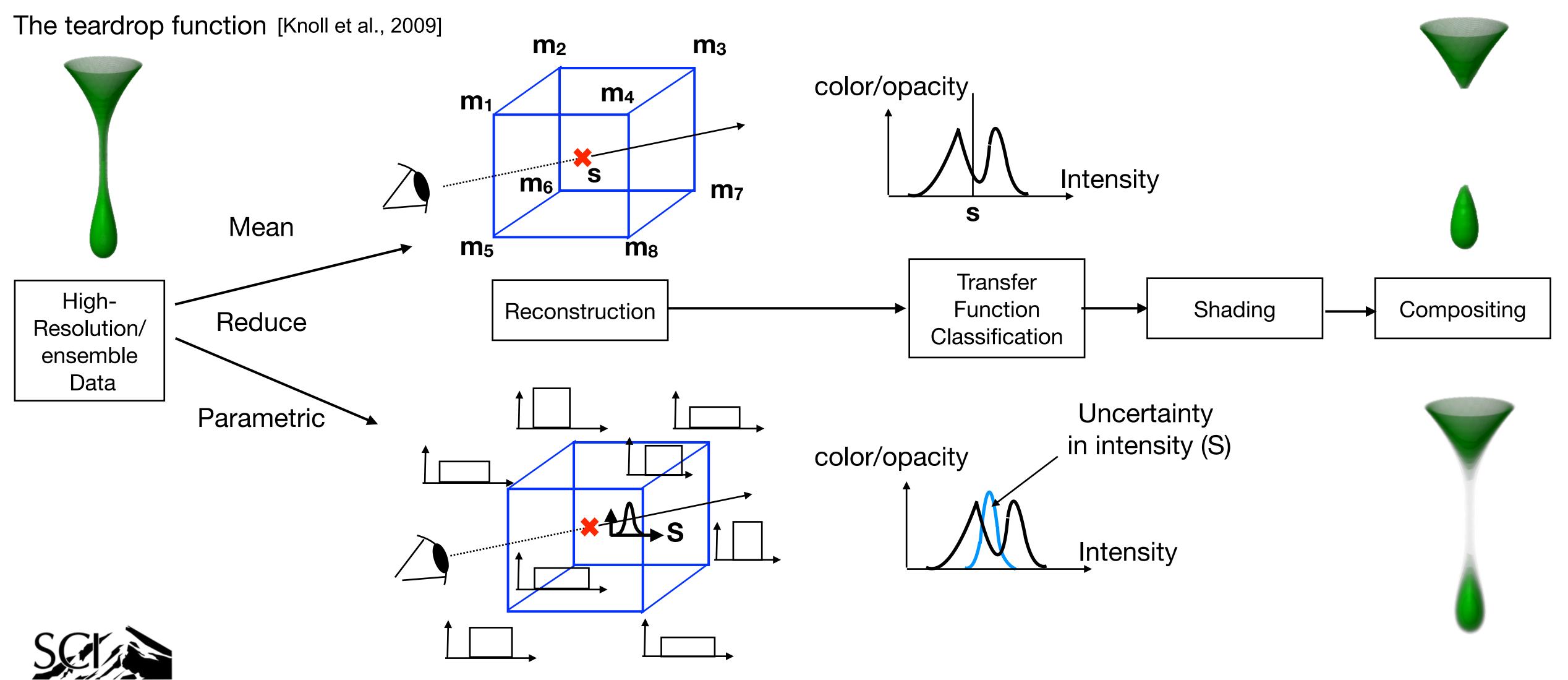
Uncertainty-Aware Morse Complex Visualizations



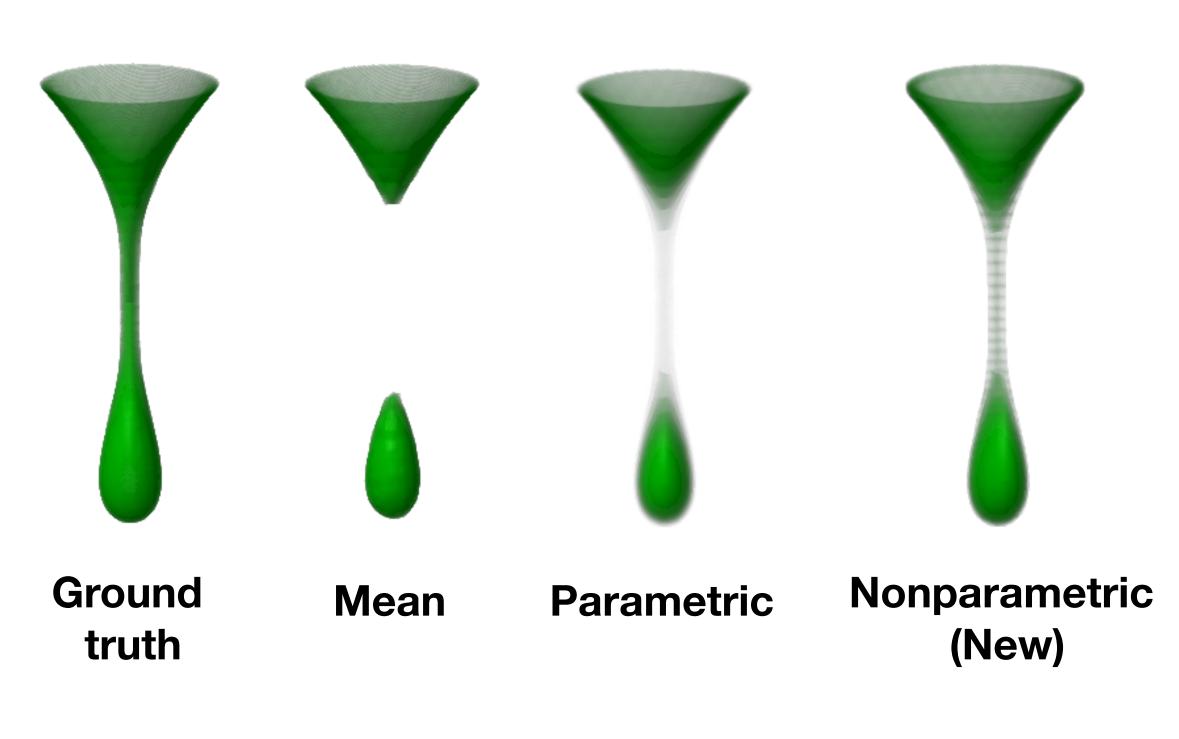


Direct Volume Rendering of Uncertain Data

[Liu et al., 2012; Sakhaee and Entezari, 2017]



DVR of Uncertain Data (Nonparametric)



Groundtruth **Parametric** Nonparametric (New)

The teardrop function

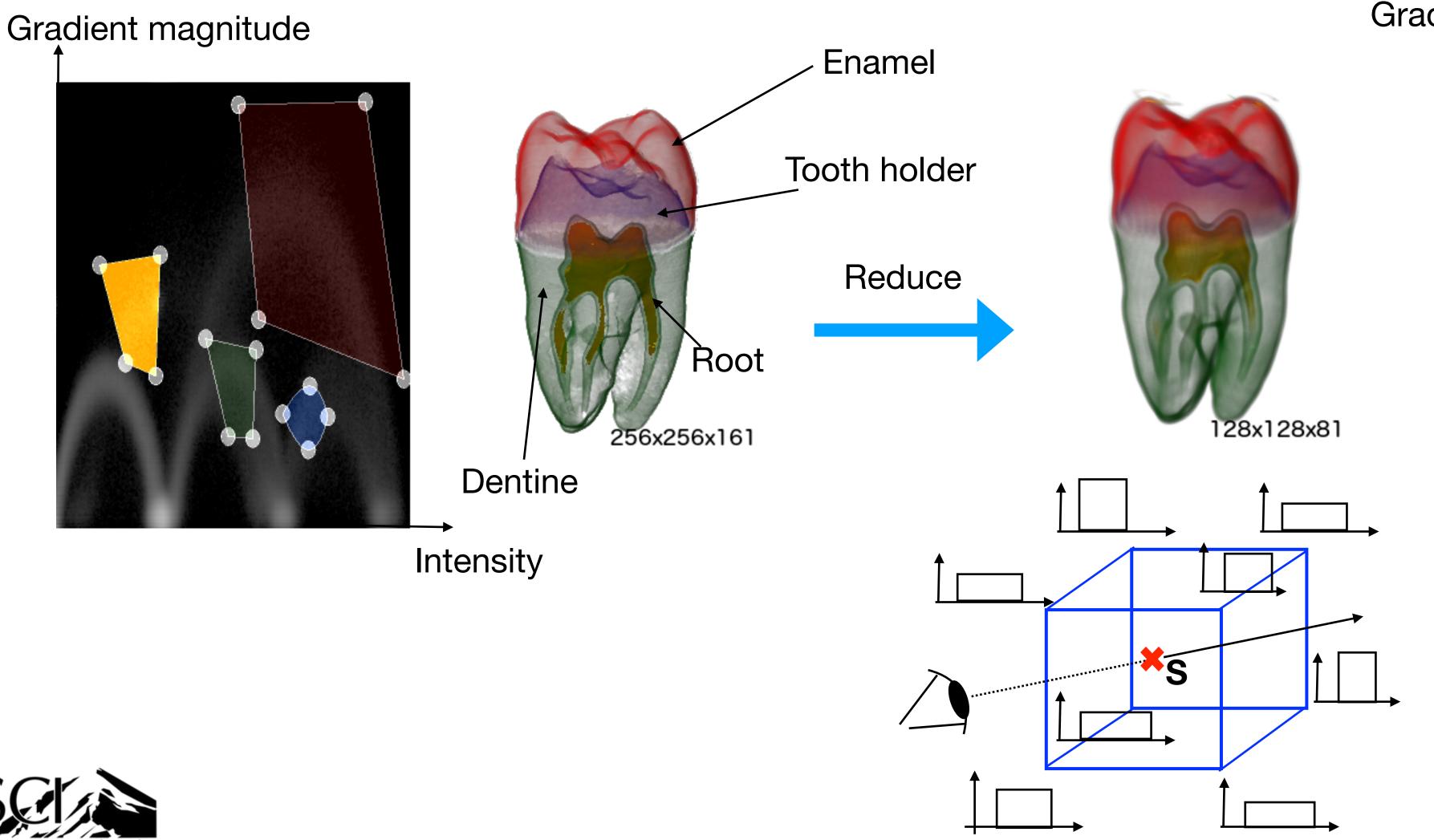
Osirix OBELIX dataset (http://medvis.org/datasets/)

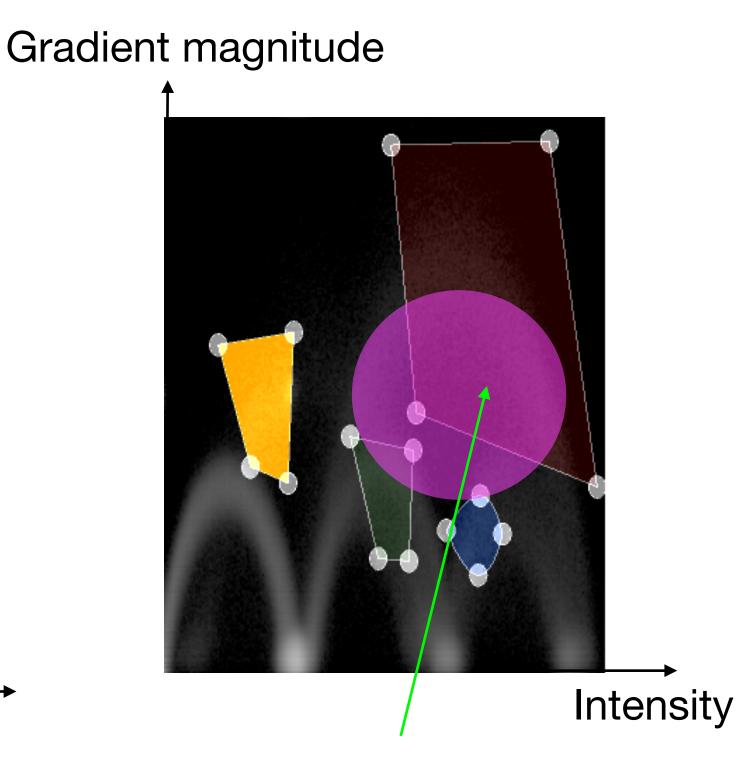


T. M. Athawale, B. Ma, E. Sakhaee, L. Zhou, C. R. Johnson, and A. Entezari; **Nonparametric Models for Direct Volume Rendering of Uncertain Data Using Multidimensional Transfer Functions** (in progress)

DVR of Uncertain Data (2D Transfer Functions)

[Kniss et al., 2002]





Probability density of S: The material for the sample is most likely to be Enamel



A Statistical Framework for Visualization of Positional Uncertainty in Deep Brain Stimulation Electrodes

Tushar Athawale¹, Ph.D. (<u>tushar.athawale@sci.utah.edu</u>); Kara Johnson²; Chris R. Butson², Ph.D.; and Chris R. Johnson¹, Ph.D.



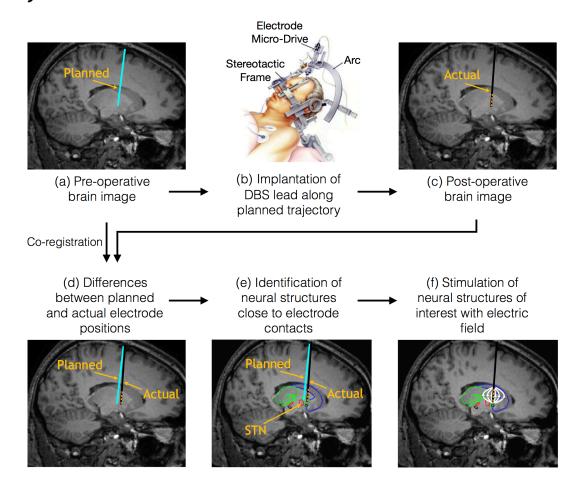




¹Scientific Computing & Imaging (SCI) Institute, University of Utah, Salt Lake City, USA; ²Department of Biomedical Engineering, University of Utah, Salt Lake City, USA

Deep Brain Stimulation (DBS)

 An FDA-approved neurosurgical procedure for treating patients with movement disorders, e.g., Parkinson's and dystonia.

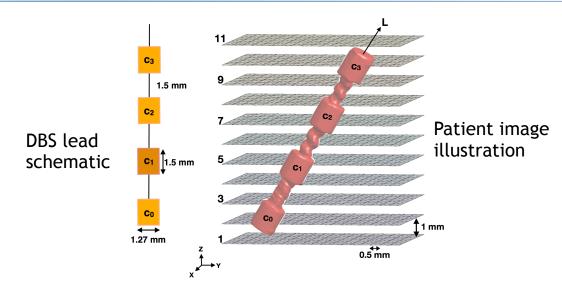


- The effectiveness of DBS depends upon physician's knowledge regarding precise DBS electrode positions in the patient brain.
- The role of post-operative DBS imaging:
 - Understand DBS electrode positions in the patient brain.
 - Mitigate the uncertainty in DBS electrode positions arising from mechanical inaccuracies of stereotactic frames [1] and brain shift [2].

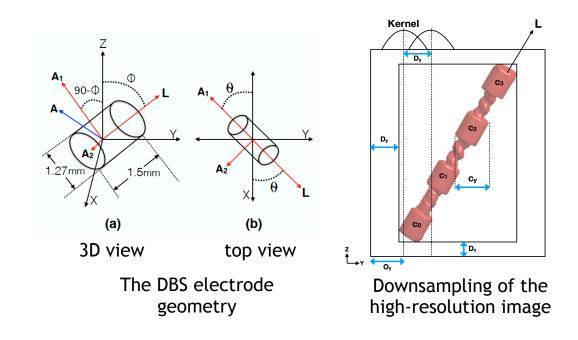
Problem with Post-Operative DBS imaging

• The finite resolution of post-operative imaging limits our knowledge of exact electrode positions in the patient brain.

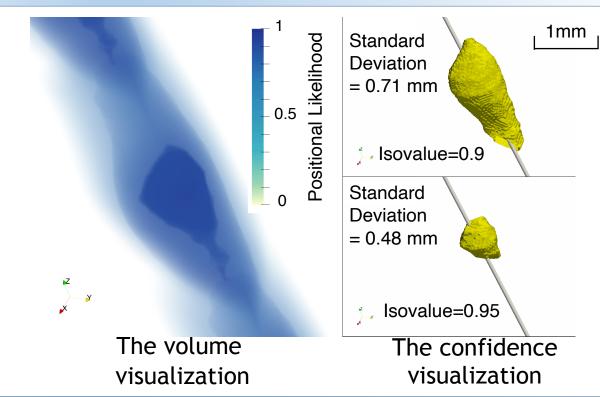
Post-Operative Imaging Uncertainty



- **Given:** A finite-resolution CT scan of implanted DBS electrodes, e.g., the image above captures data on 11 slices.
- Goal: To quantify the spatial uncertainty in DBS electrodes for their finite-resolution imaging and visualize the quantified spatial uncertainty.
- Approach: (a) Compute electrode geometry in closed form, (b) Map electrode geometry to a high-resolution electrode image (with electrodes out of patient brain), (c) Draw low-resolution samples from a high-resolution electrode image, (d) Compare low-resolution samples with the patient image [3].



Electrode-Center Spatial Uncertainty Visualizations



Conclusion

We show that the uncertainty in DBS electrode positions is significant in post-operative imaging, e.g., 0.49 mm average spatial uncertainty for 0.45x 0.45x1 mm³ resolution. Further, we integrate DBS computational modeling pipeline with our electrode uncertainty visualizations for accurate prediction of patient response to therapy.

Acknowledgements

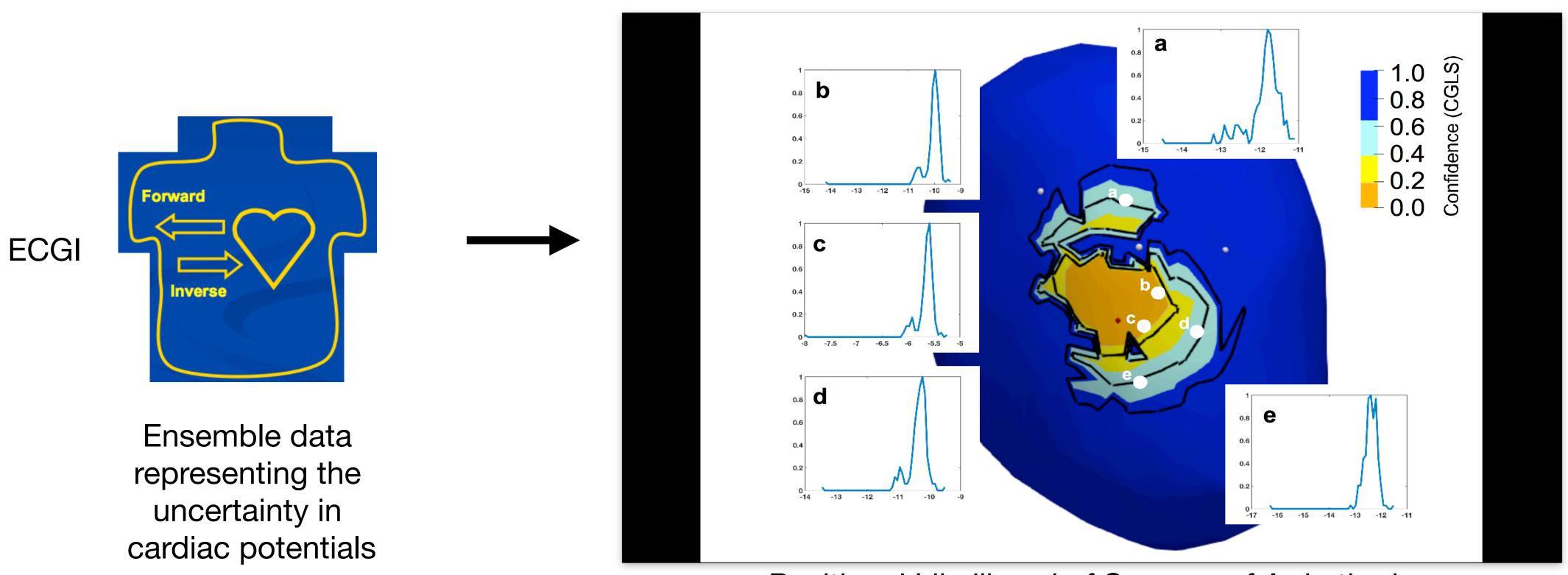
This project is supported in part by the National Institute of General Medical Sciences of the National Institutes of Health under grant number P41 GM103545-18.

References

- [1]: Maciunas RJ; Galloway RL, and Latimer JW. The application accuracy of stereotactic frames. *Neurosurgery*, vol. 35, no. 4, pp. 682-694, 1994.
- [2]: Halpern CH., Danish SF, Baltuch GH, and Jaggi JL. Brain shift during deep brain stimulation surgery for Parkinson's disease. Stereotact Funct Neurosurg, vol. 86, no. 1, pp. 37-43, 2008.
- [3]: Athawale T, Johnson K, Butson CR, and Johnson CR. A statistical framework for visualization of positional uncertainty in deep brain stimulation electrodes. Computer Methods in Biomechanics and Biomedical Engineering: Imaging & Visualization, vol.7, no. 4, pp. 438-449, 2019.

Uncertainty Visualization for Domain-Specific Data

Positional uncertainty in sources of arrhythmia for noisy ECG recordings





Conclusions

- Uncertainty visualizations are important for avoiding misleading interpretations regarding the underlying data
 - Level sets
 - Deep brain stimulation imaging
 - Morse complex visualizations
 - Direct volume rendering
 - Electrocardiography imaging
- Statistical methods for uncertainty quantification

- Monte Carlo vs. Analytical
- Methods for uncertainty visualization
 - Color mapping proportional to the level of confidence/uncertainty
 - Interactive probability distribution queries
 - Derive uncertainty volumes and visualize them using isosurfaces/direct volume rendering



Future Work

- Visualization algorithms, e.g., topological analysis, for uncertain input data
- Uncertainty visualization for domain-specific data
- Machine learning and uncertain data
- Value of uncertainty visualizations (are they informative or confusing to a user?)



Publications

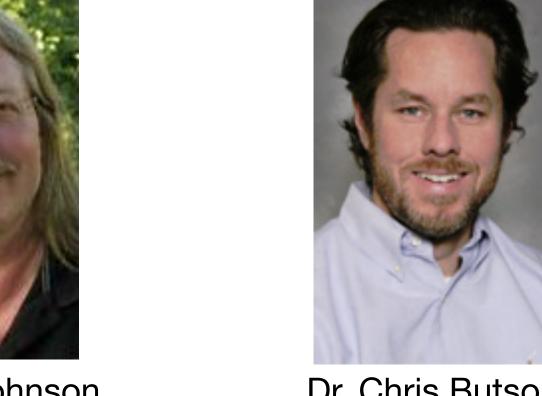
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For any questions, please contact at:

Email: <u>tushar.athawale@gmail.com</u>

